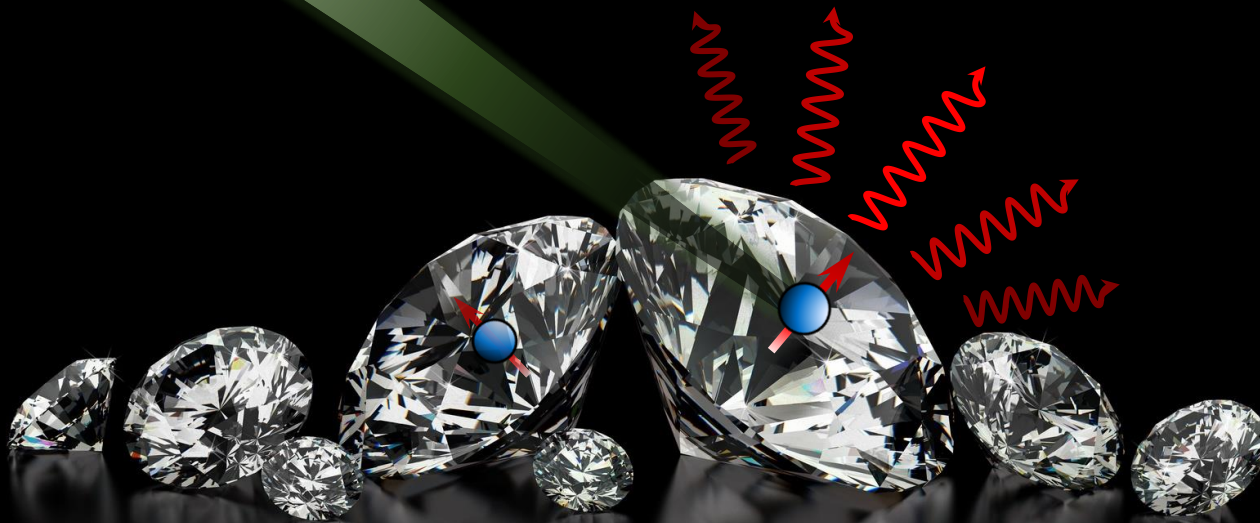


# Introduction to the diamond NV centers focusing on quantum sensing applications



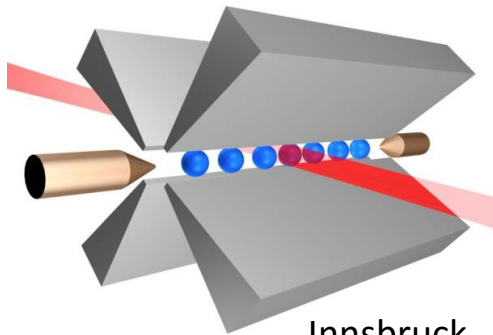
Donghun Lee

Department of Physics, Korea University

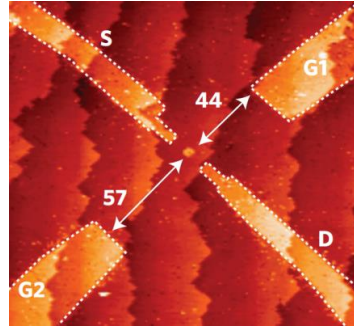
# Toward quantum devices in real life

Quantum devices (applications of quantum systems)

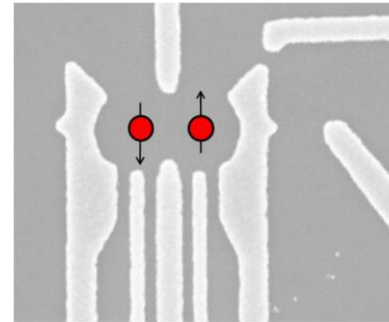
e.g. quantum computers, quantum communications, quantum metrology



Innsbruck



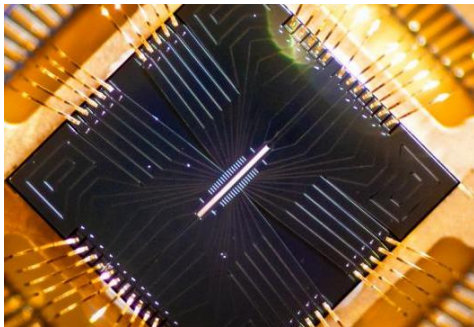
CQC



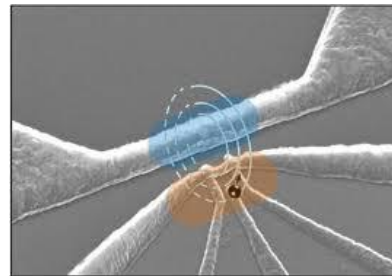
Harvard



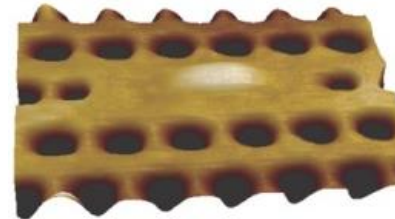
Yale



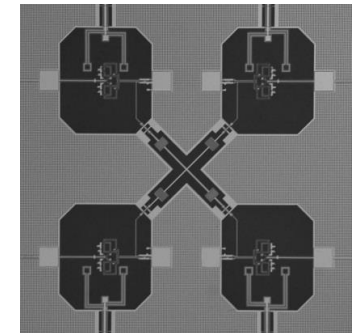
UMD



CQC



ETH Zurich



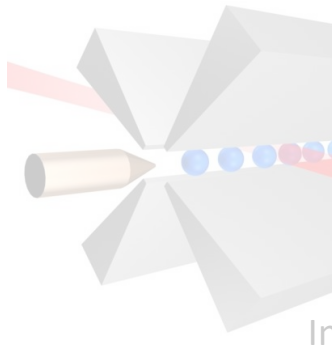
UCSB

- Long spin coherence time (e.g. trapped atoms)
- Fast processing capabilities (e.g. superconducting qubits)
- Scalabilities (e.g. solid-state QDs or defects)
- Interfaces and transducers (e.g. photons, mechanical oscillators)
- ...

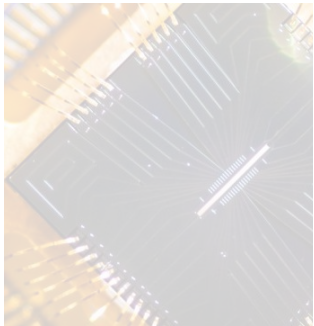
# Toward quantum devices in real life

Quantum devices (applications of quantum systems)

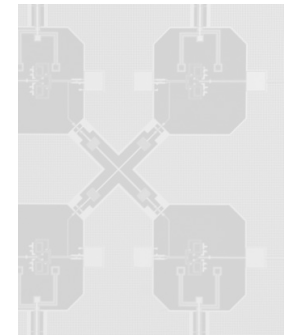
e.g. quantum computers, quantum communications, quantum metrology



Ir



Yale



UCSB

Nitrogen-Vacancy color centers in diamond crystal

“diamond NV centers”

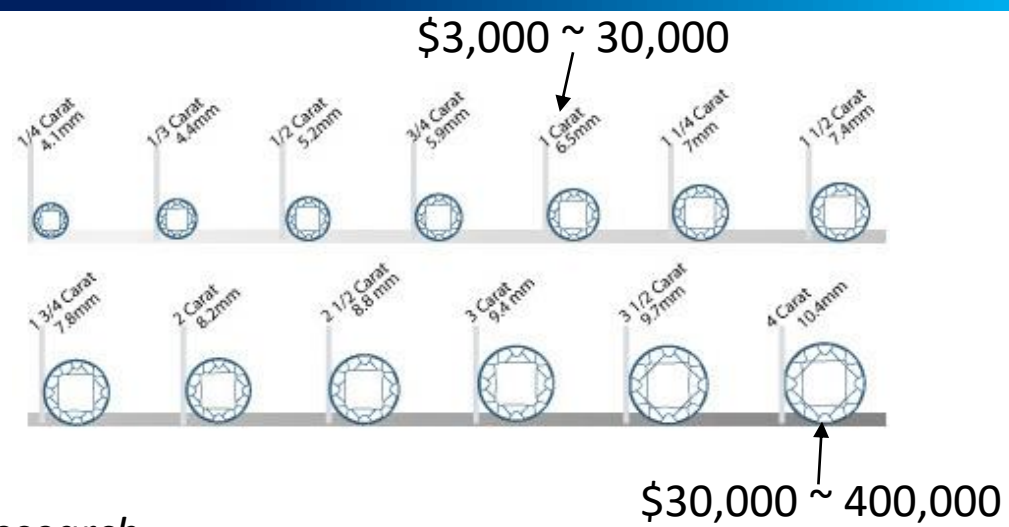
- Lo
- Fa
- Sc
- Int
- ...

ors)

- Basics of the NV center
  - Structure, electronic, optical properties
  - Spin physics, coherence properties
- Applications for quantum metrology
  - Magnetic field sensing
  - Strain field sensing

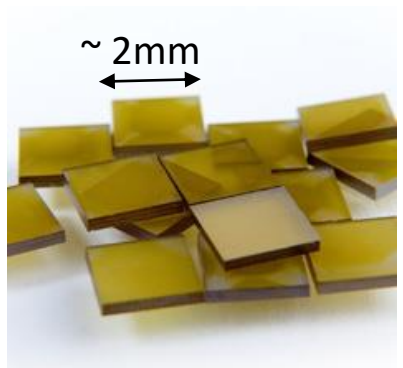
- Basics of the NV center
  - Structure, electronic, optical properties
  - Spin physics, coherence properties
- Applications for quantum metrology
  - Magnetic field sensing
  - Strain field sensing

# Physical structure of diamond and the NV center



## Synthesized single crystal diamond for research

- HPHT (high pressure high temperature) growth (> 50,000 bar, > 1400 °C)
- CVD (chemical vapor deposition) growth
- Nanodiamonds, thin films, bulk crystals...



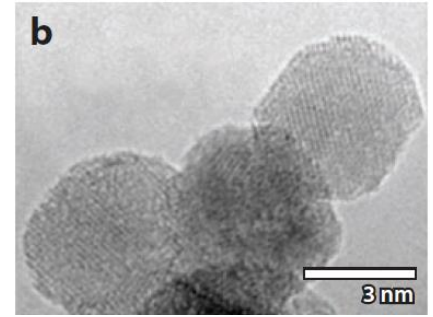
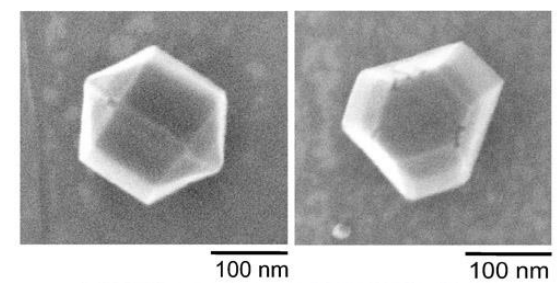
Type Ib diamond:  
~ 100 ppm [N]



Element 6

Type IIa diamond: ~ 1 ppm [N]  
**Electronic grade: < 5 ppb [N]**

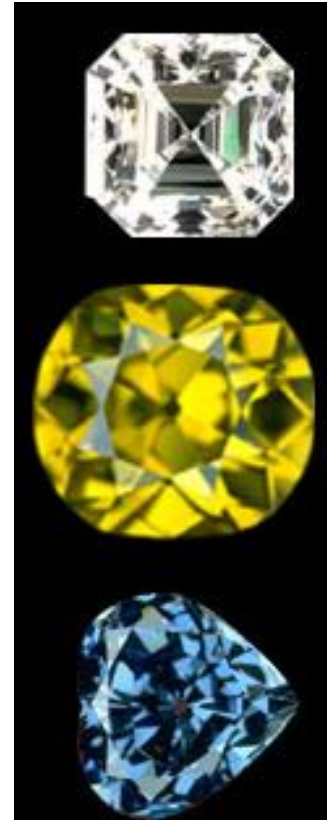
## Nanodiamonds



# Physical structure of diamond and the NV center

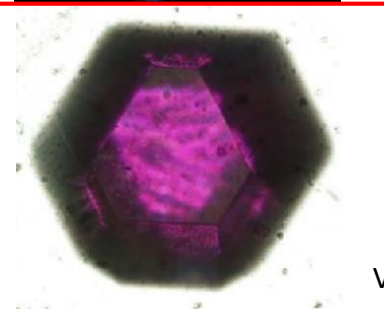
## Color centers in diamonds

- Pure diamond (clear)
- Nitrogen defects (yellow)
- Boron defects (blue)



original-diamonds.com

- Nitrogen-Vacancy(NV) defects (pink)

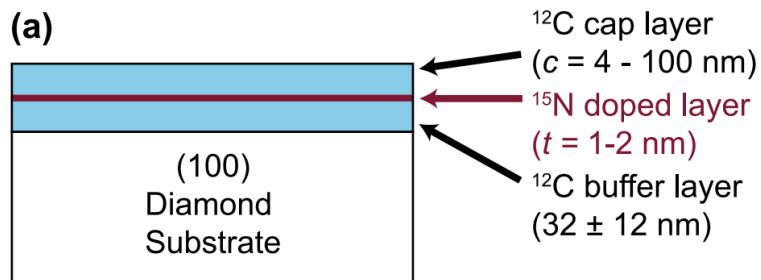


V. M. Acosta Ph.D. thesis (2011)

# Formation of the NV center

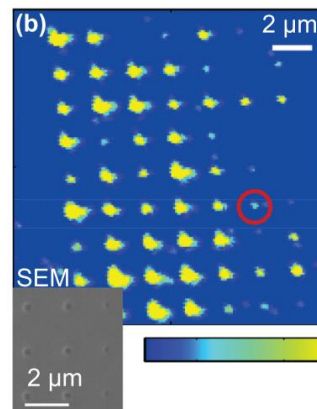
- Natural or as-grown NV centers : longest spin coherence times for bulk NVs
- High density NV formation: electron irradiation ( $\sim$  MeV) and annealing ( $\sim$  800 K)
- Low density NV formation: N implantation ( $\sim$  keV) and annealing ( $\sim$  800 K)
- Position control of NV centers :
  - Depth control: delta-doped CVD growth
  - Lateral position control: masked implantation, TEM irradiation

## Delta-doped CVD growth



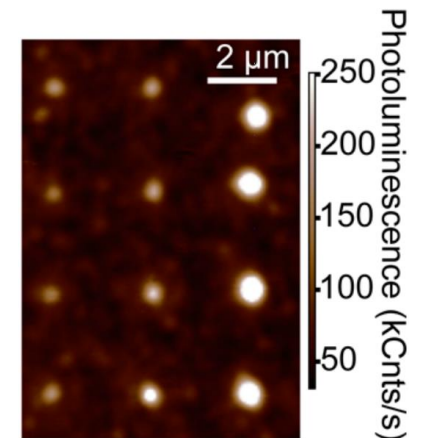
K. Ohno *et al.*, Appl. Phys. Lett. (2012)

## Masked implantation



K. Ohno *et al.*, Appl. Phys. Lett. (2014)

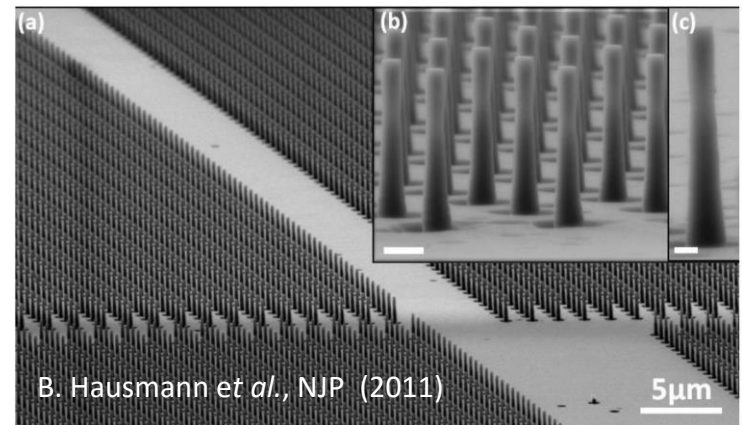
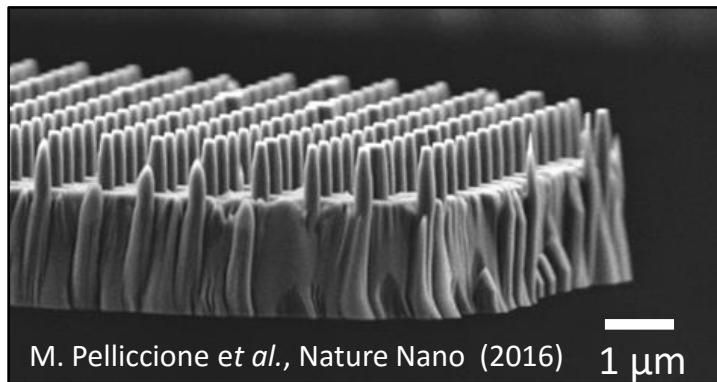
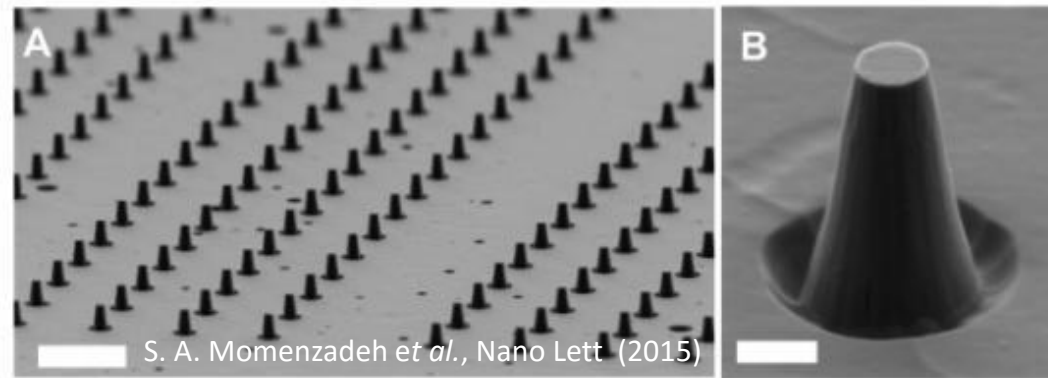
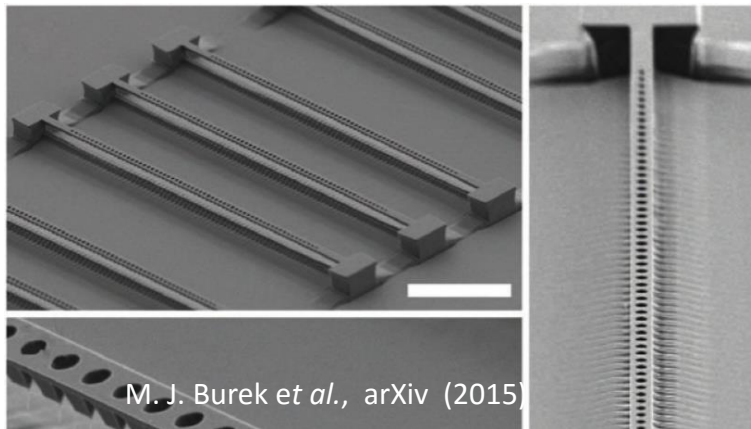
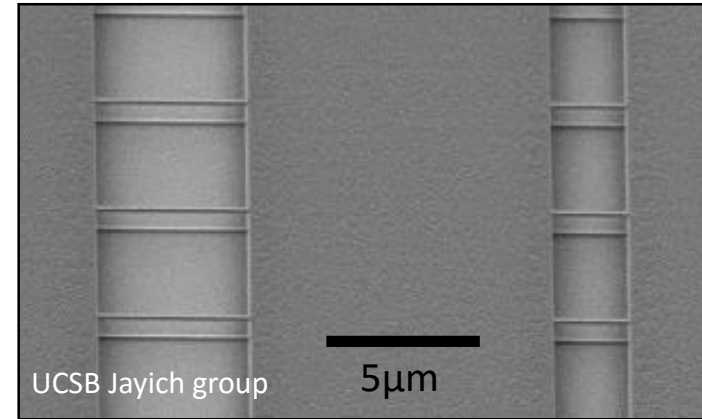
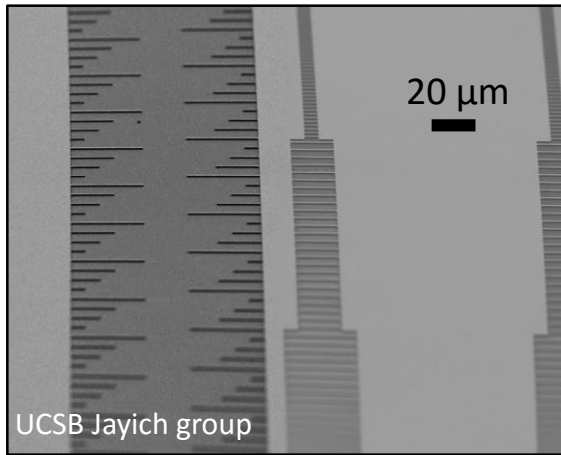
## TEM irradiation



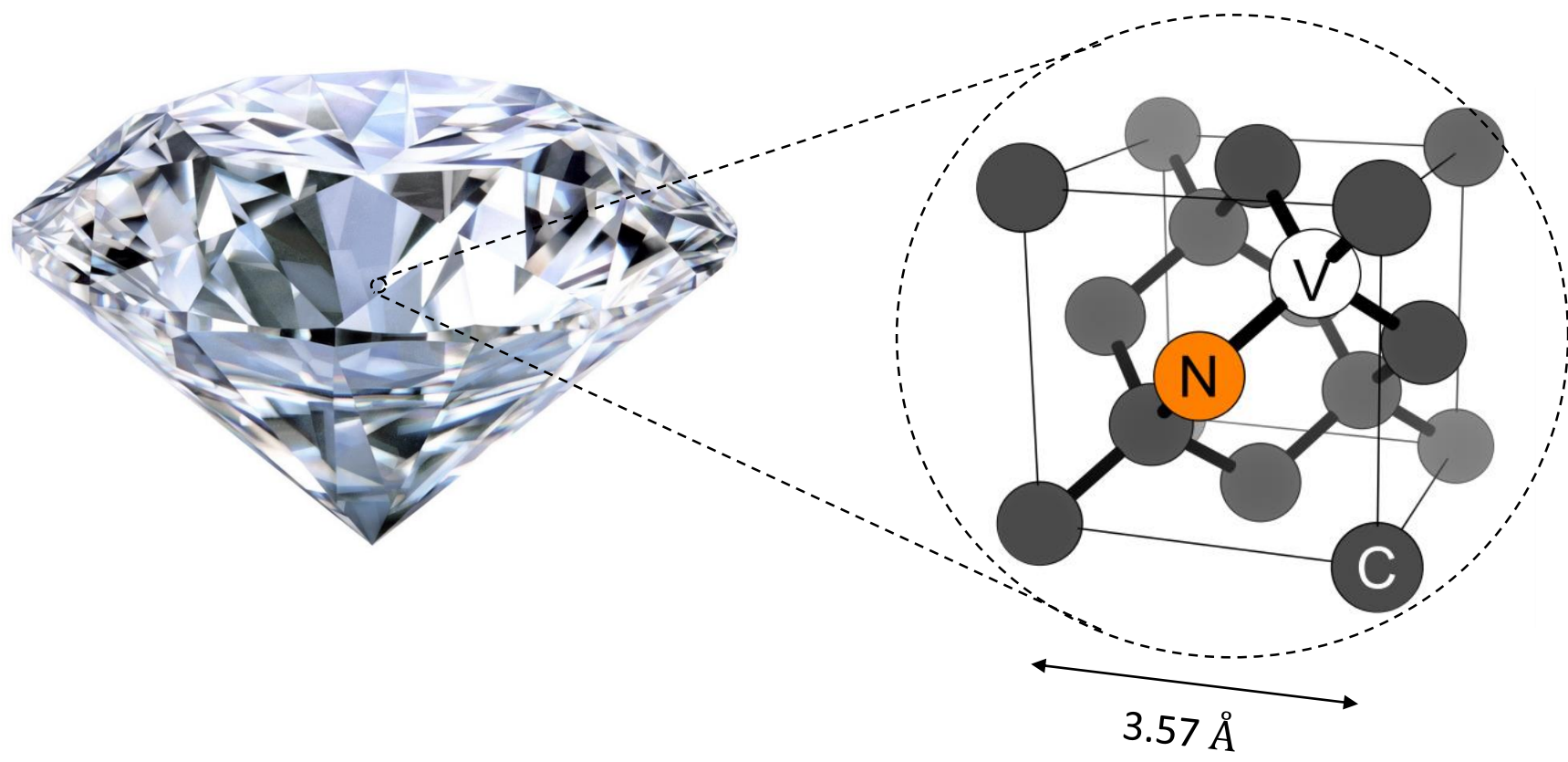
C. A. McLellan *et al.*, Nano Lett. (2016)



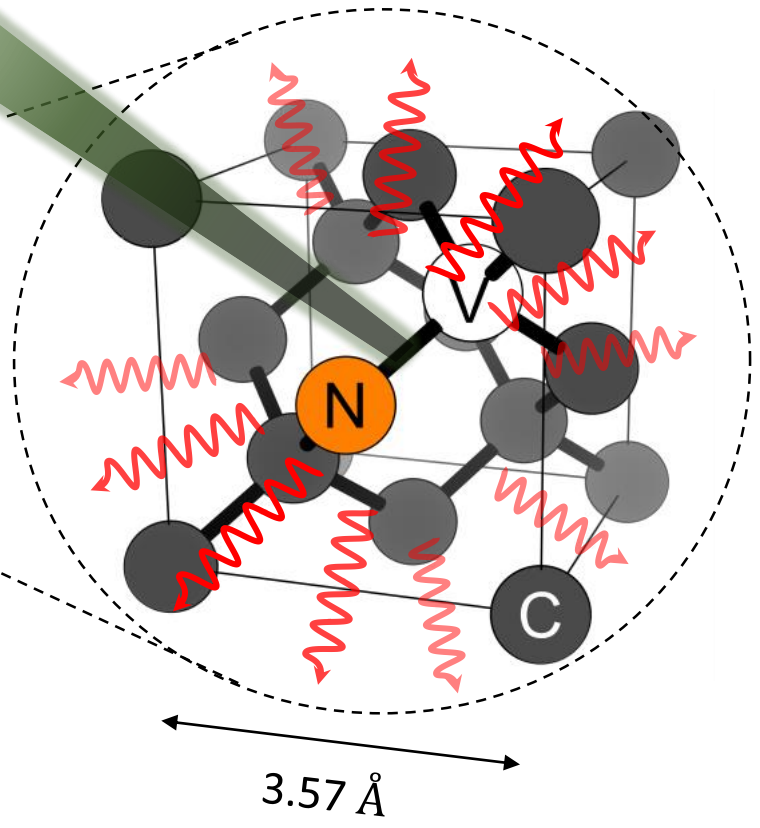
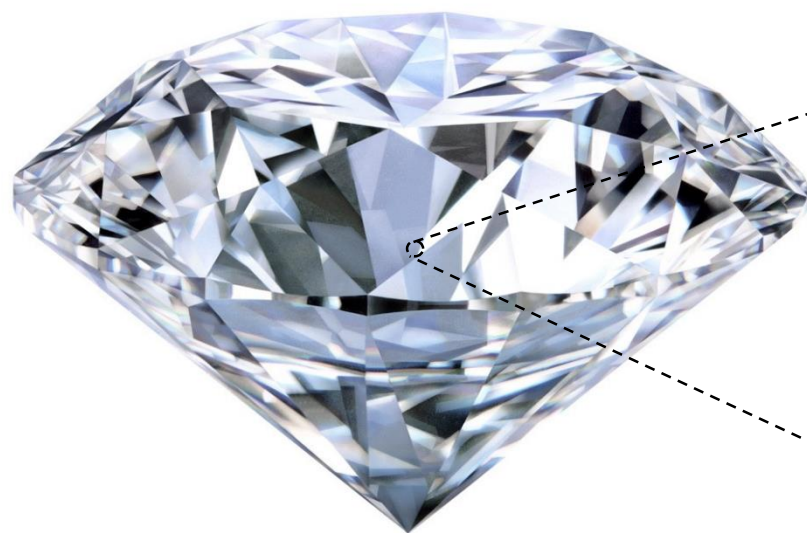
# Fabrication of diamond nanostructures



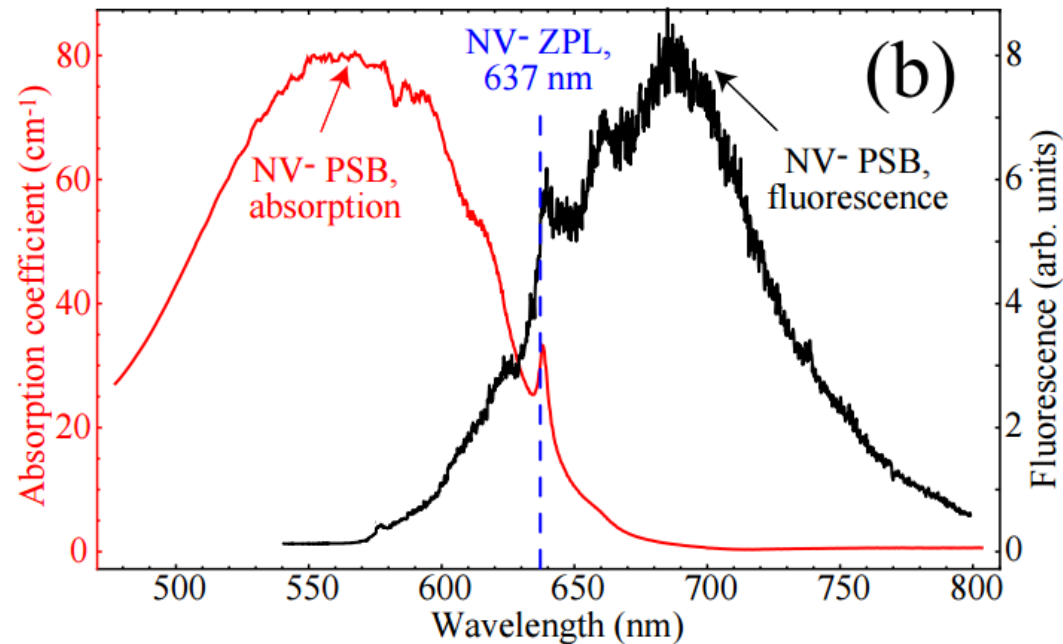
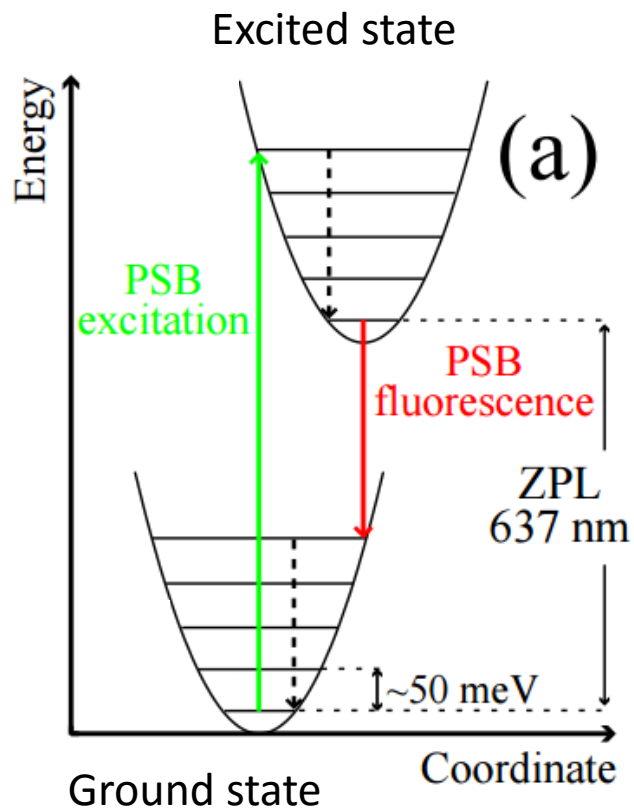
# Optical properties of the NV center



# Optical properties of the NV center



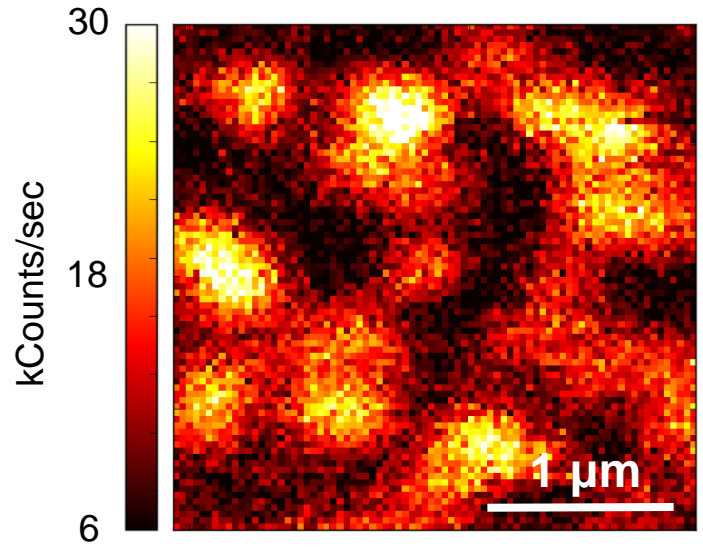
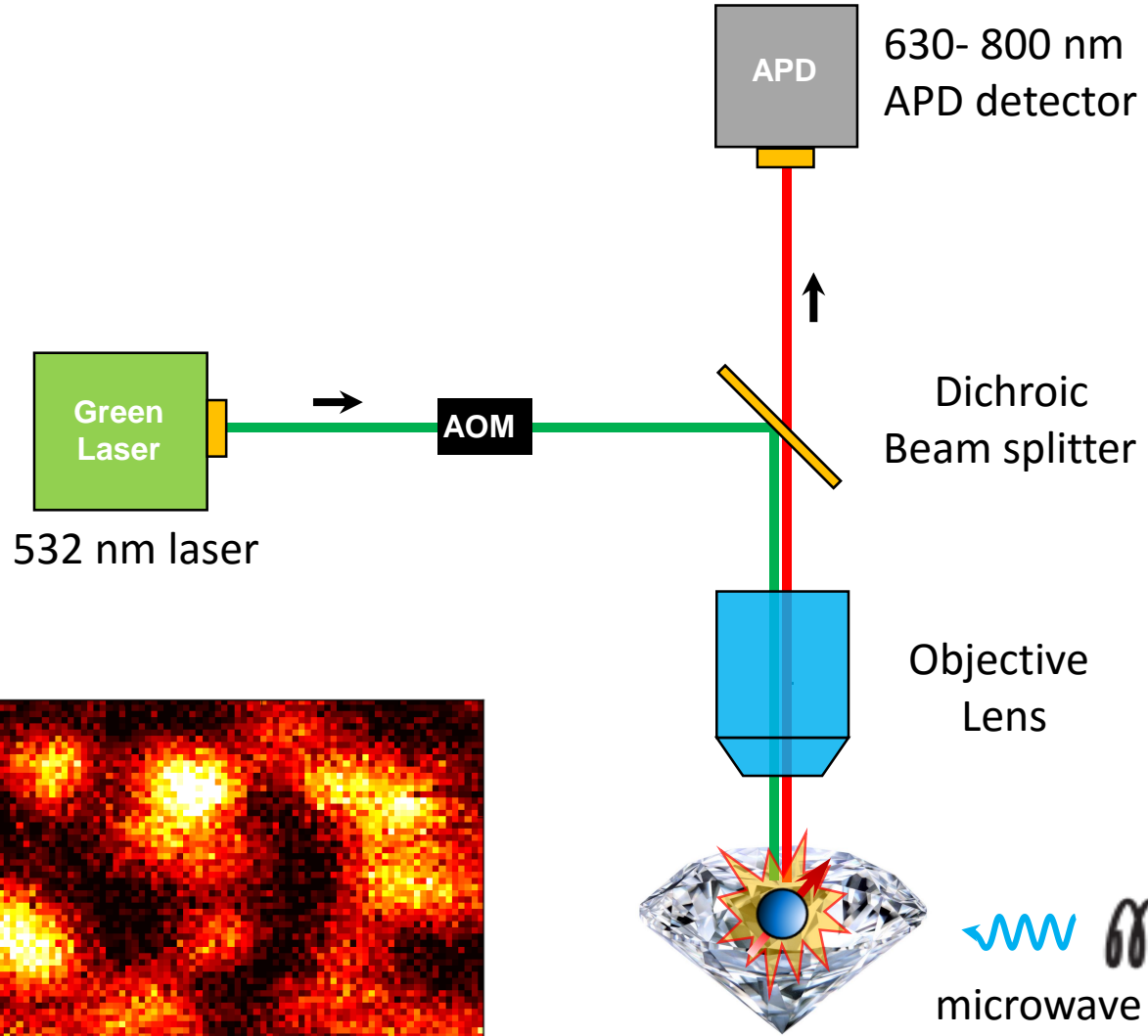
# Optical properties of the NV center



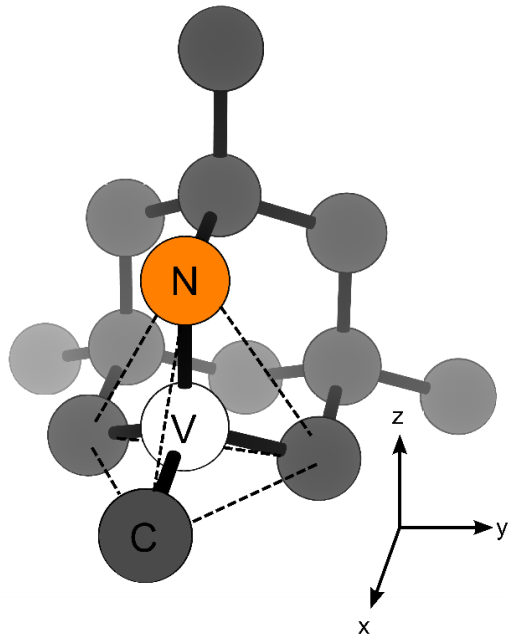
dashed lines : non-radiative decay

Room-temperature optical absorption and fluorescence (excited at 532 nm) spectra from NV<sup>-</sup> center

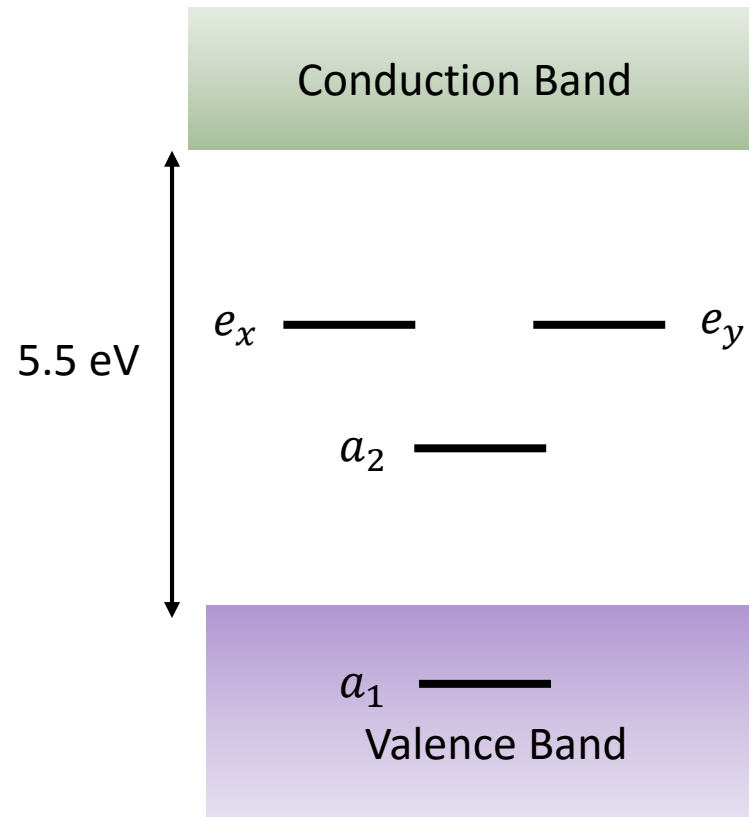
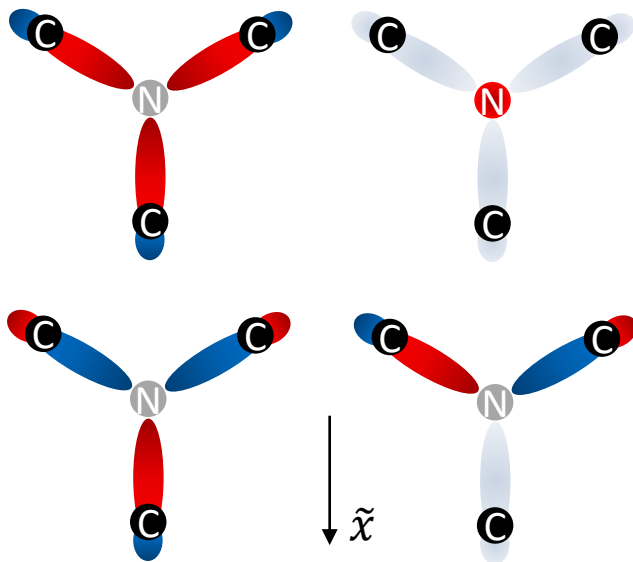
# Experimental setup: confocal optics



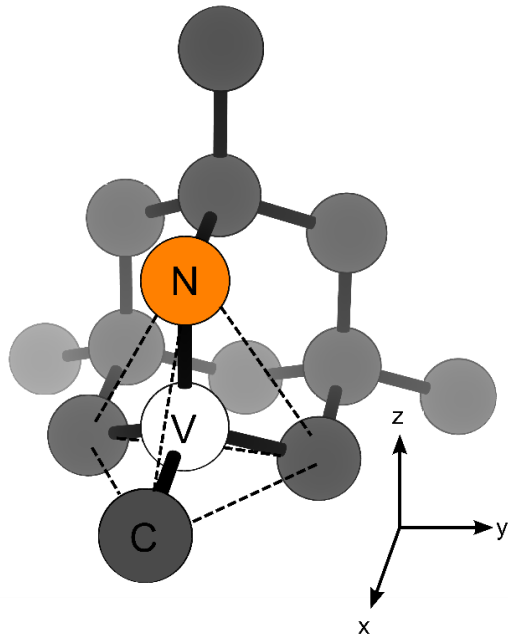
# Electronic properties of the NV center



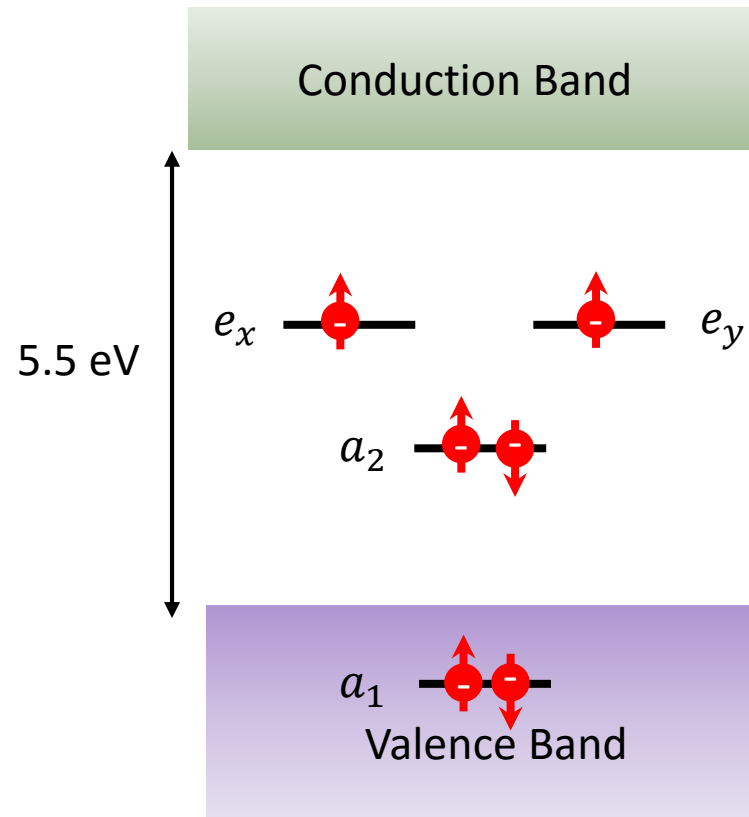
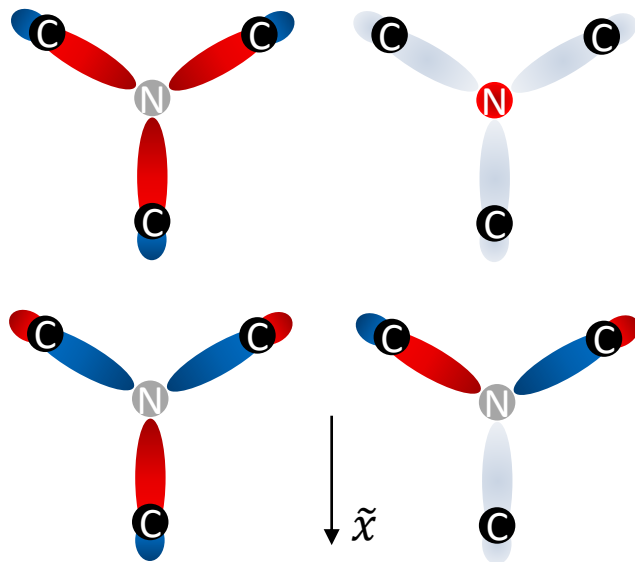
- LCAO (linear combinations of atomic orbitals)  
: four  $sp^3$  dangling bonds
- $C_{3v}$  point group symmetry



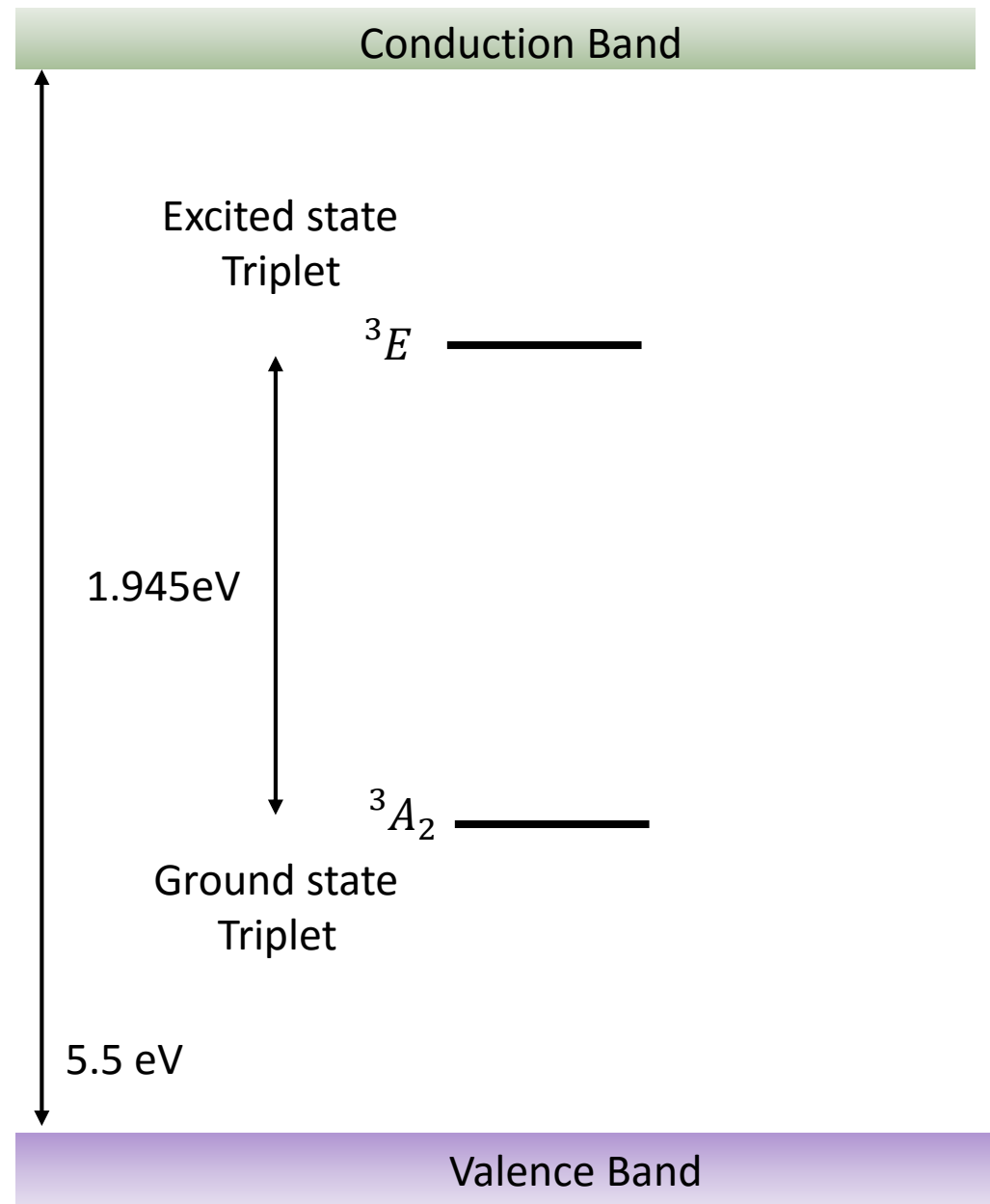
# Electronic properties of the NV center



- LCAO (linear combinations of atomic orbitals)  
: four  $sp^3$  dangling bonds
- $C_{3v}$  point group symmetry
- There are total 6 electron for  $NV^-$   
: 3  $e^-$  from C, 2  $e^-$  from N, 1  $e^-$  from environment
- $S = 1$  (spin triplet) state

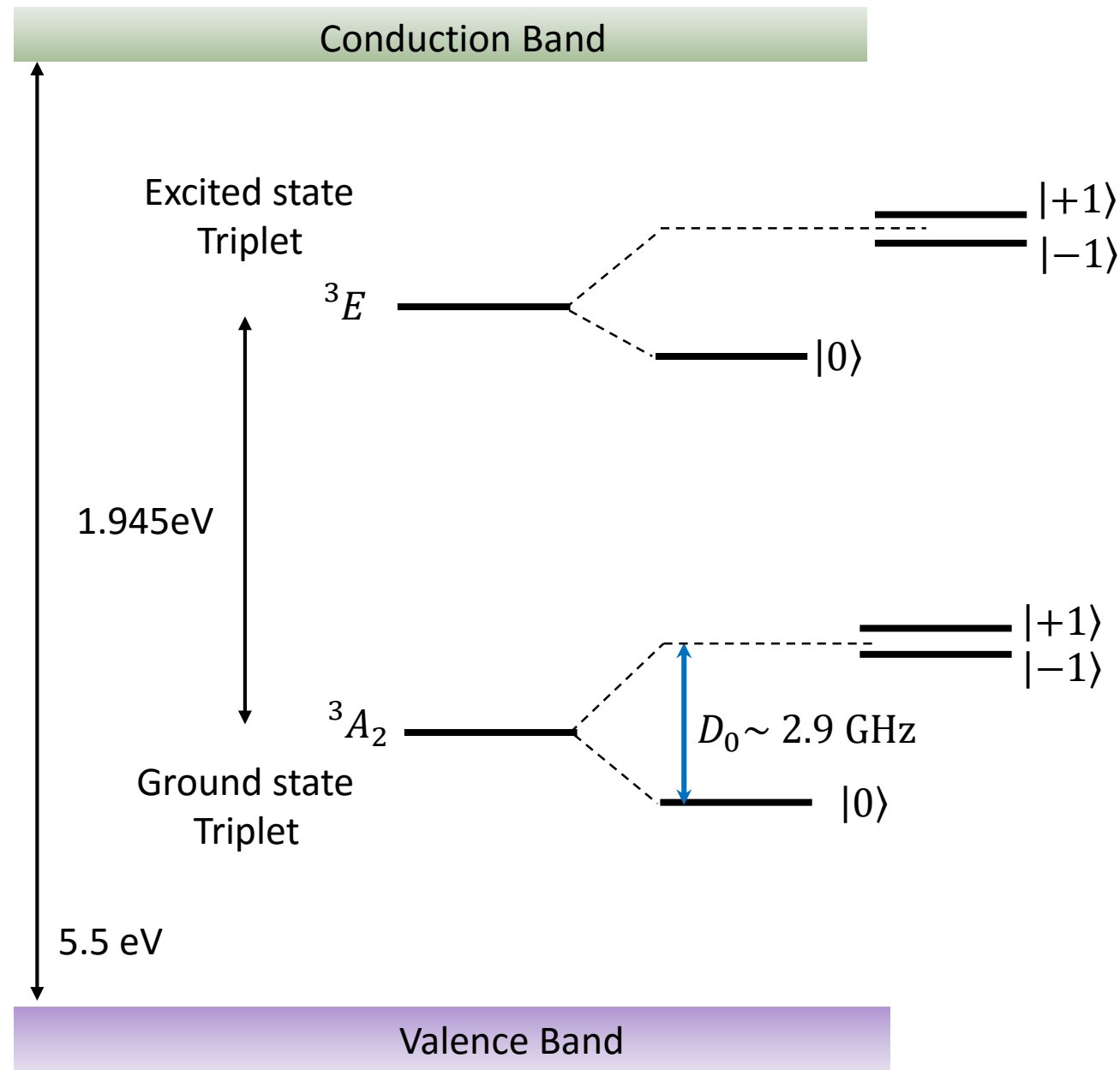


# Electronic properties of the NV center

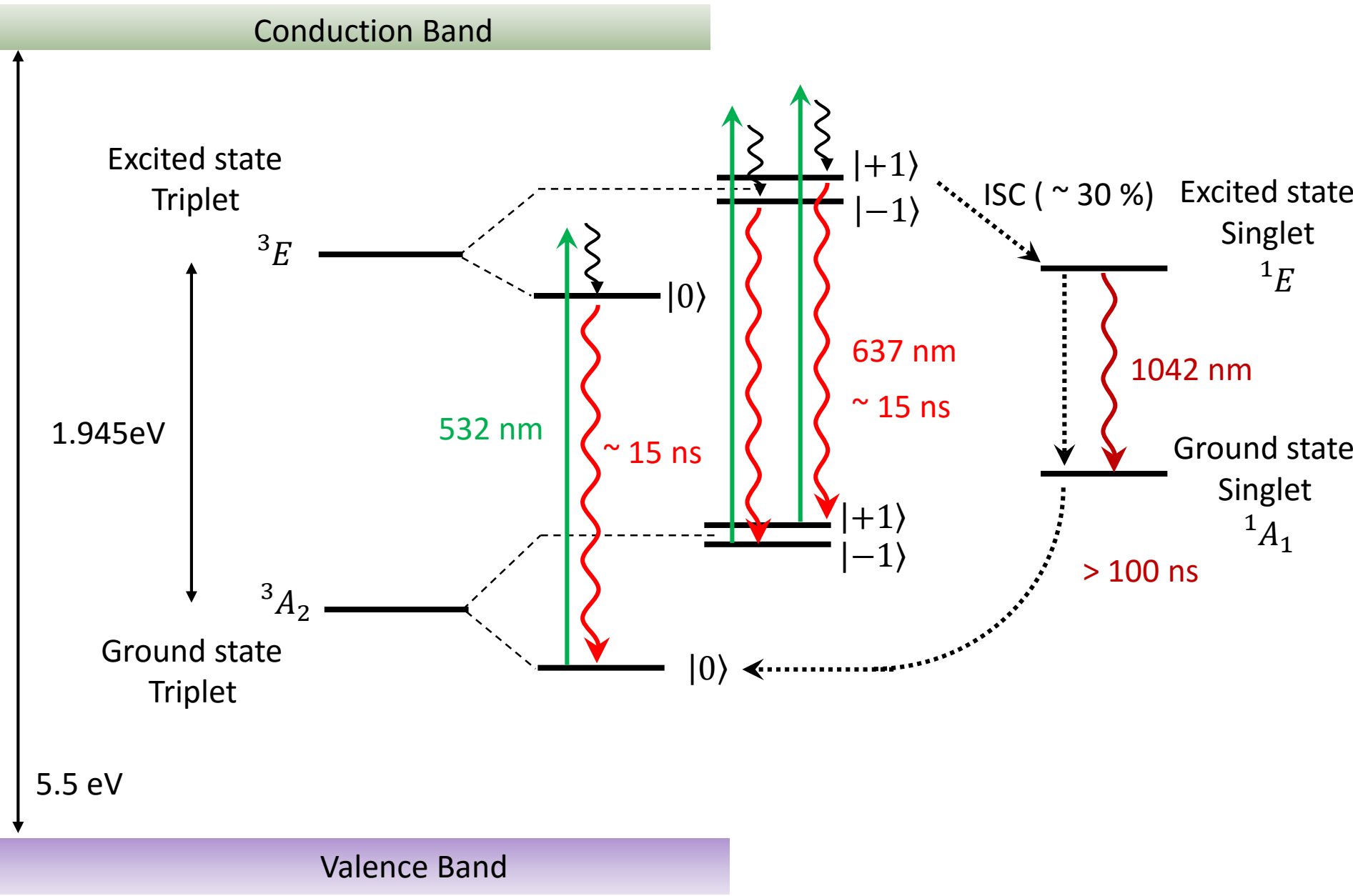




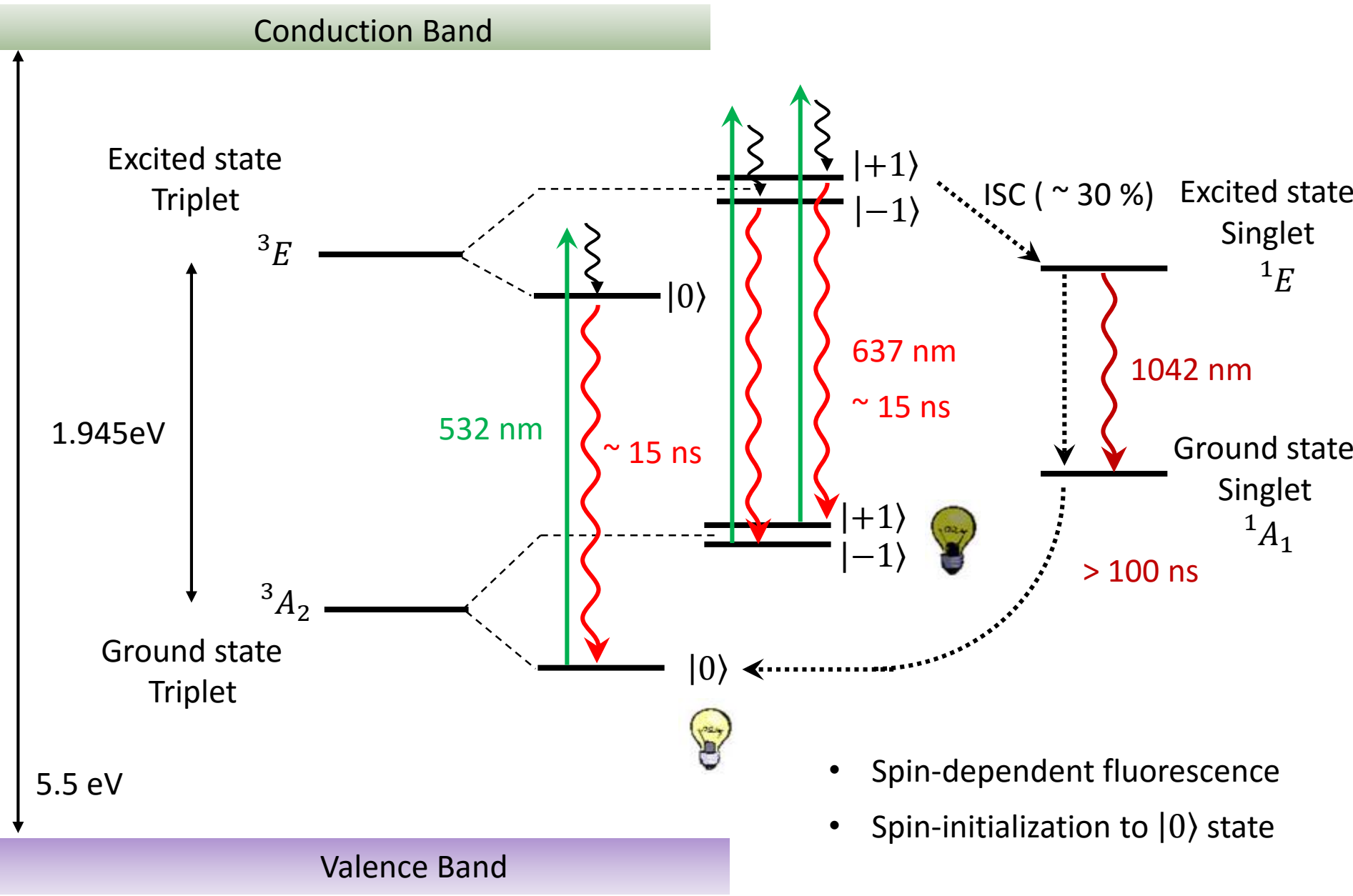
# Electronic properties of the NV center



# Electronic properties of the NV center

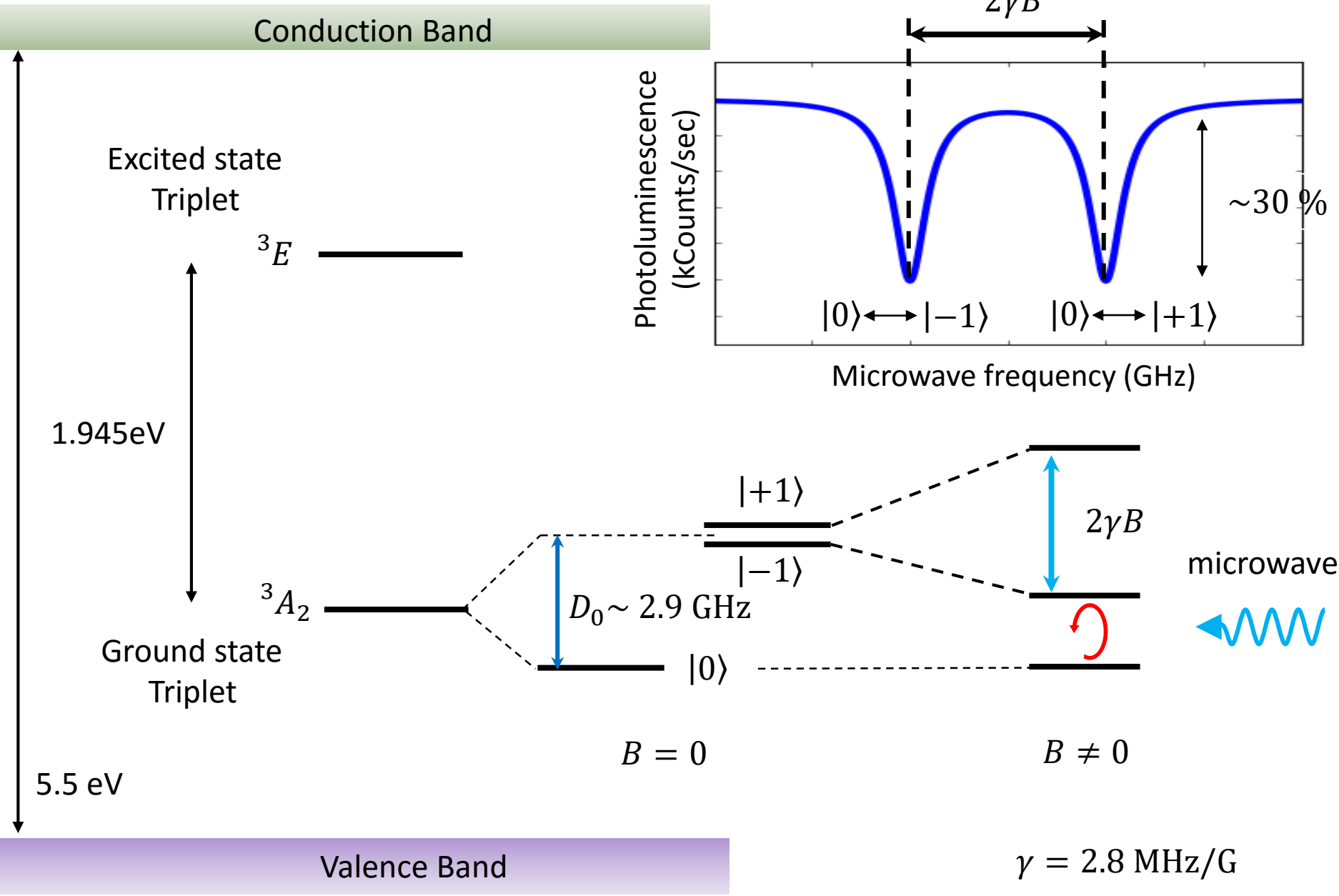


# Electronic properties of the NV center

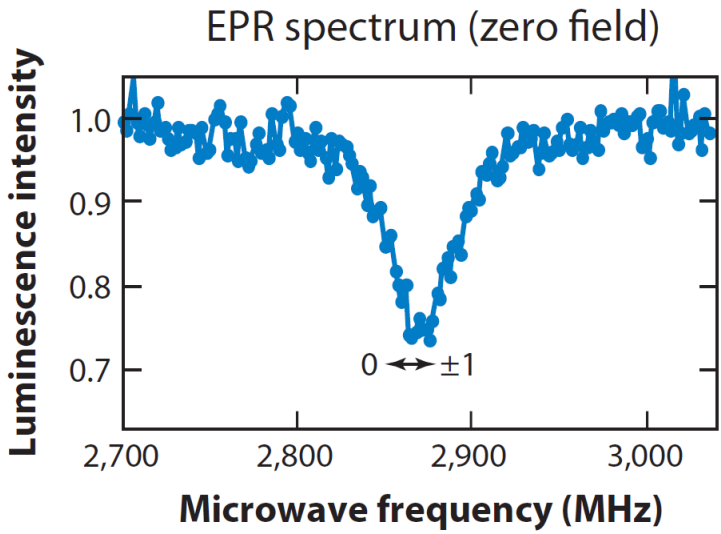


- Spin-dependent fluorescence
- Spin-initialization to  $|0\rangle$  state

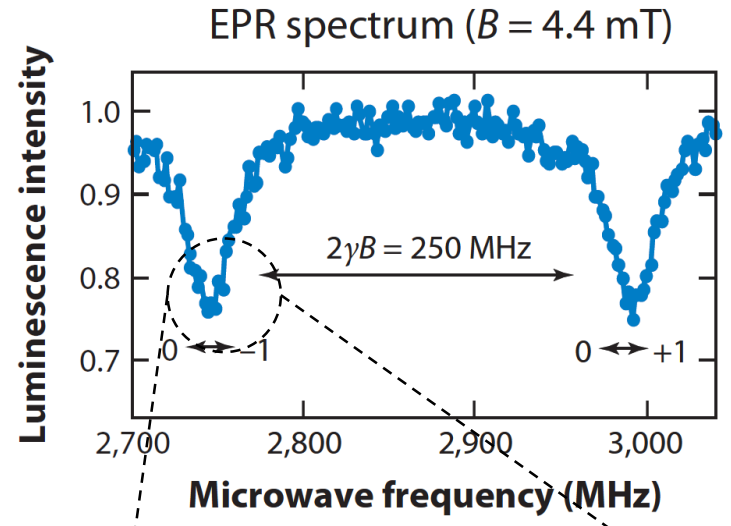
# Electronic properties of the NV center



# Electronic properties of the NV center



R. Schirhagl *et al.*, Annu. Rev. Phys. Chem. (2014)



Hyperfine interaction with  $^{14}\text{N}$  ( $I = 1$ )

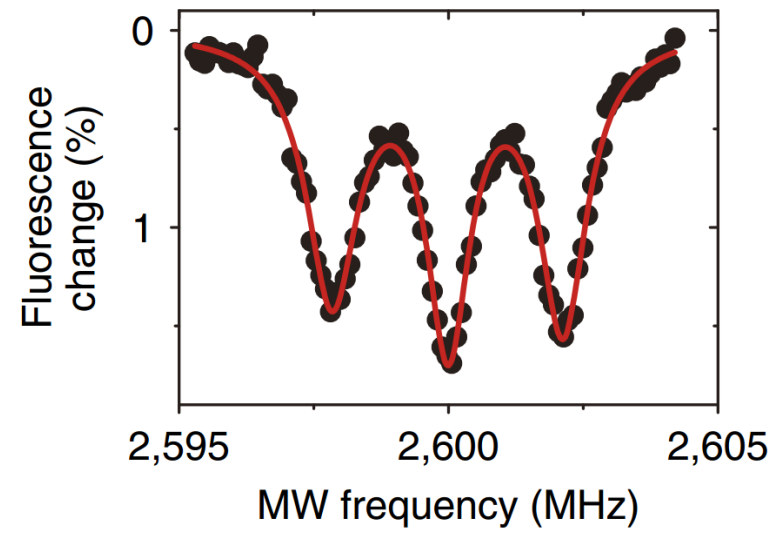
## Ground-state Hamiltonian for NV center

zero-field splitting    Magnetic field    Hyperfine interaction

$$H = D_0 S_z^2 + \gamma \mathbf{S} \cdot \mathbf{B} + \mathbf{S} \cdot \mathbf{A}_N \cdot \mathbf{I}_N$$

$$+ \underline{d_z E_z S_z^2 + d_{xy} [E_x (S_x S_y + S_y S_x) + E_y (S_x^2 - S_y^2)]}$$

Electric or strain field



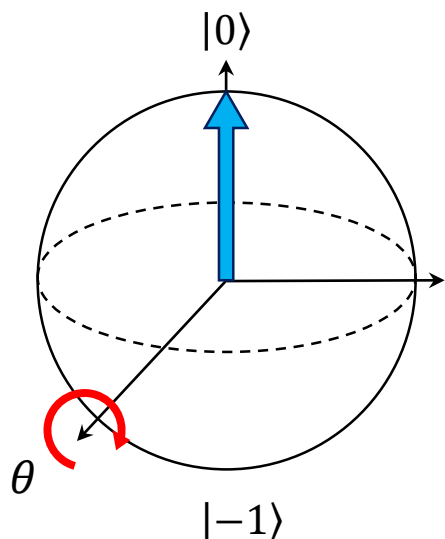
- Basics of the NV center
  - Structure, electronic, optical properties
  - Spin physics, coherence properties
- Applications for quantum metrology
  - Magnetic field sensing
  - Strain field sensing

# Spin physics and coherence properties of the NV center

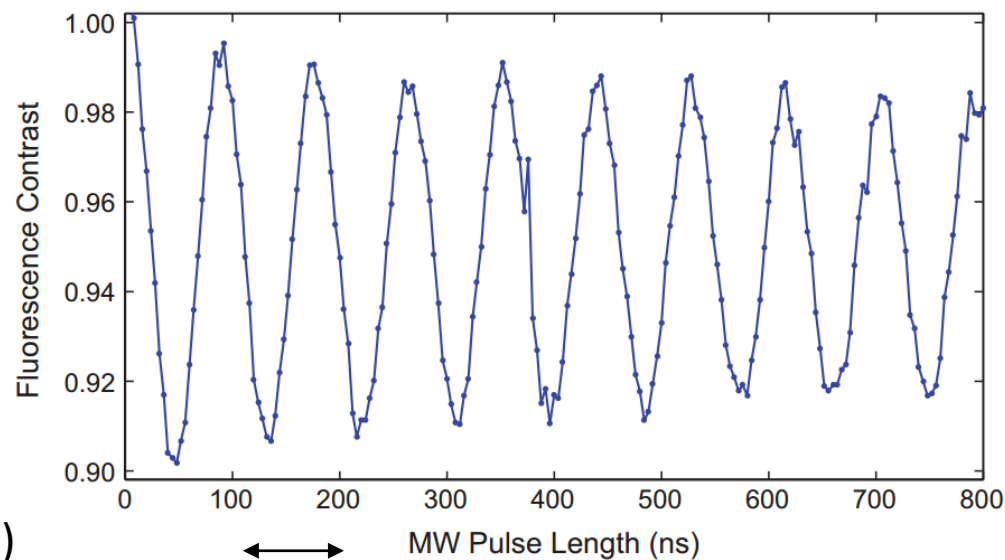
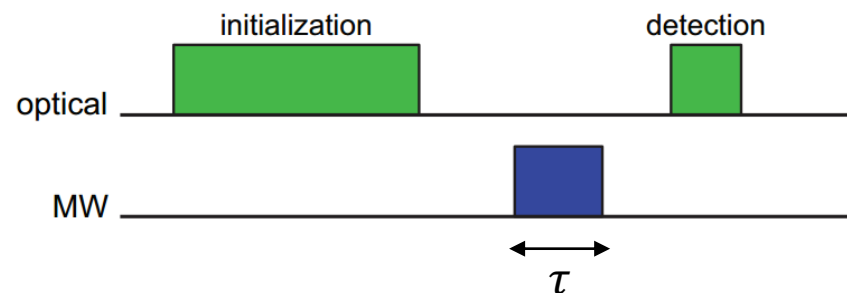
- $T_1$  : spin-lattice relaxation time measured by population decay
- $T_2$  : spin-spin dephasing time measured by Hahn echo or decoupling sequences
- $T_2^*$  : inhomogeneous dephasing time measured by free induction decay

## Rabi nutations

e.g.  $|0\rangle \leftrightarrow |-1\rangle$  spin transition



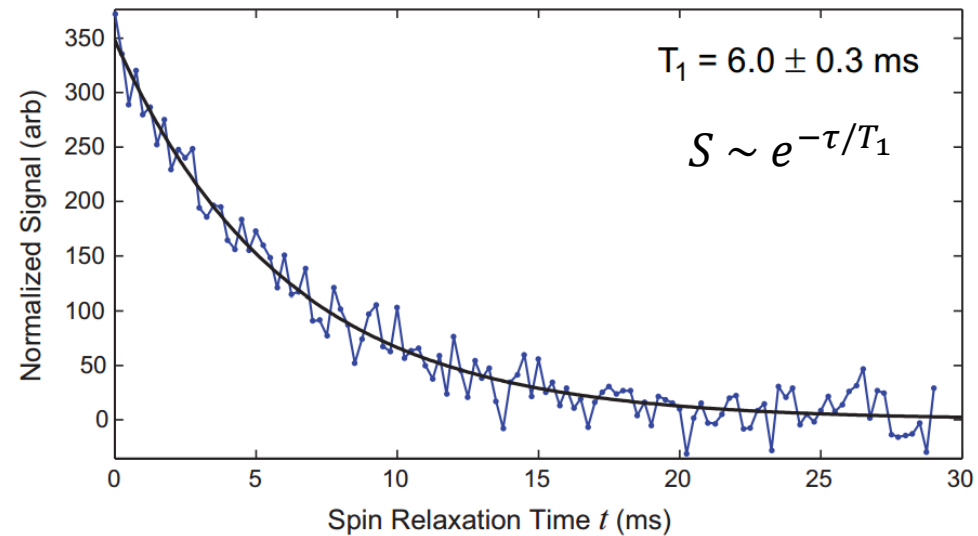
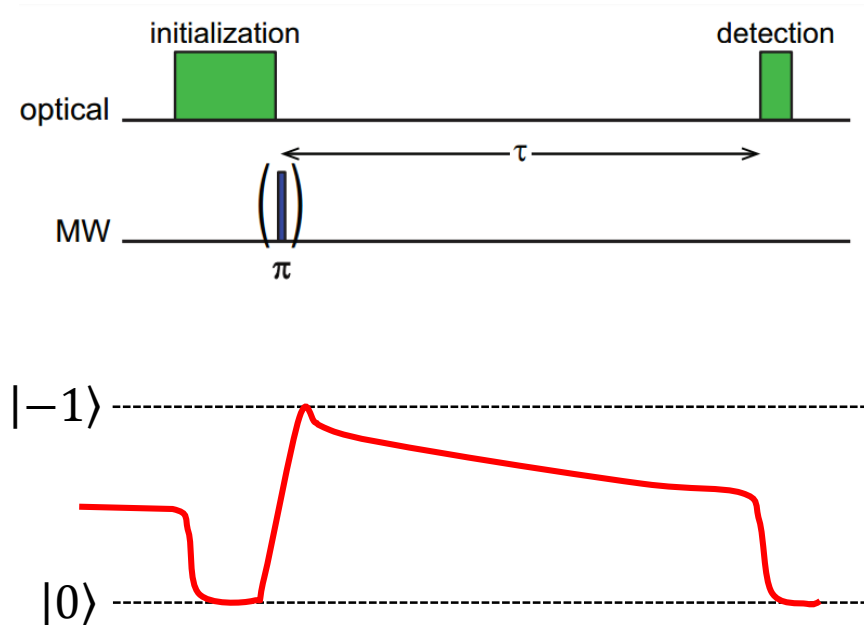
e.g.  $\theta = \pi$  ( $\pi$  pulse),  $\theta = \pi/2$  ( $\pi/2$  pulse)



$$\text{Rabi frequency} : \Omega \propto \sqrt{I_{MW}}$$

# Spin physics and coherence properties of the NV center

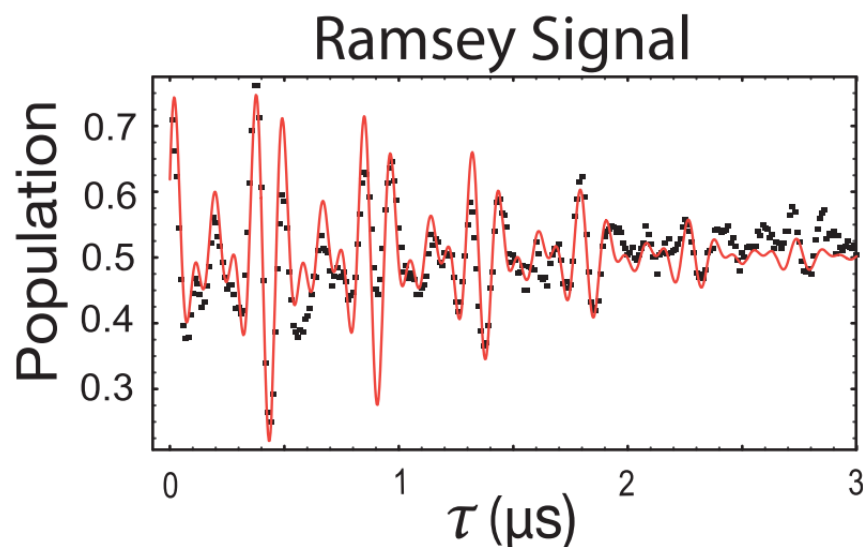
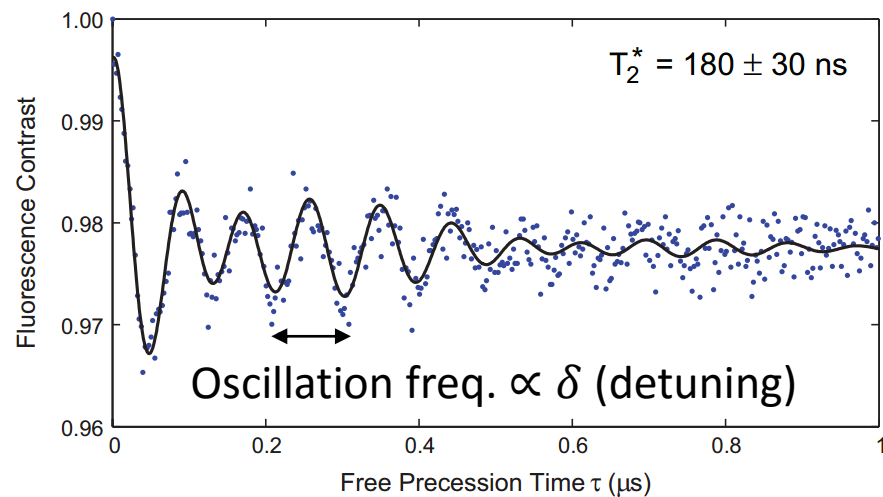
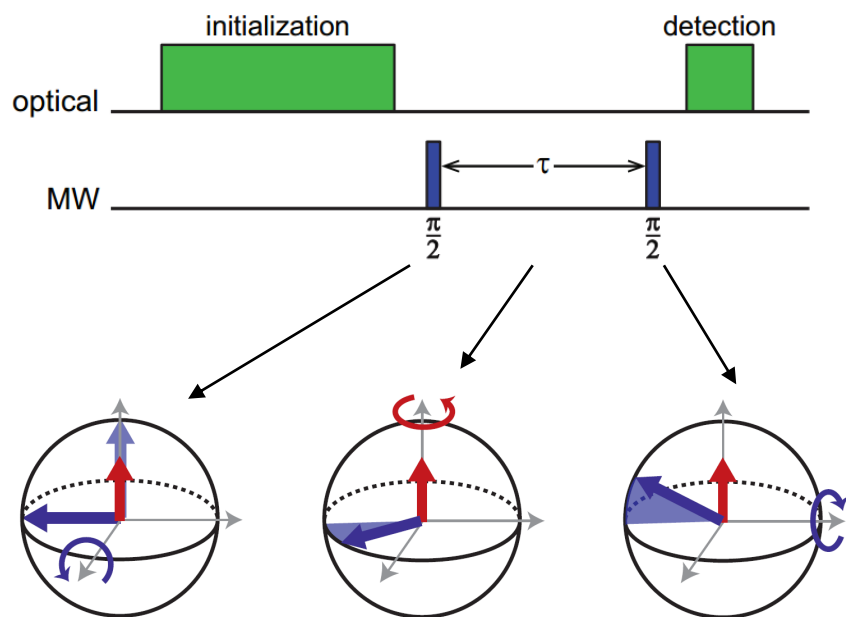
- $T_1$  : spin-lattice relaxation time measured by population decay





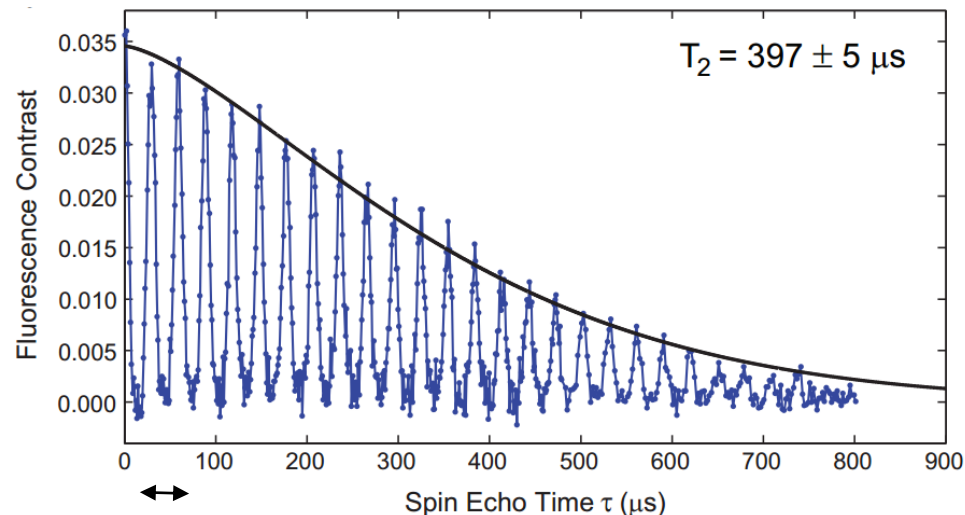
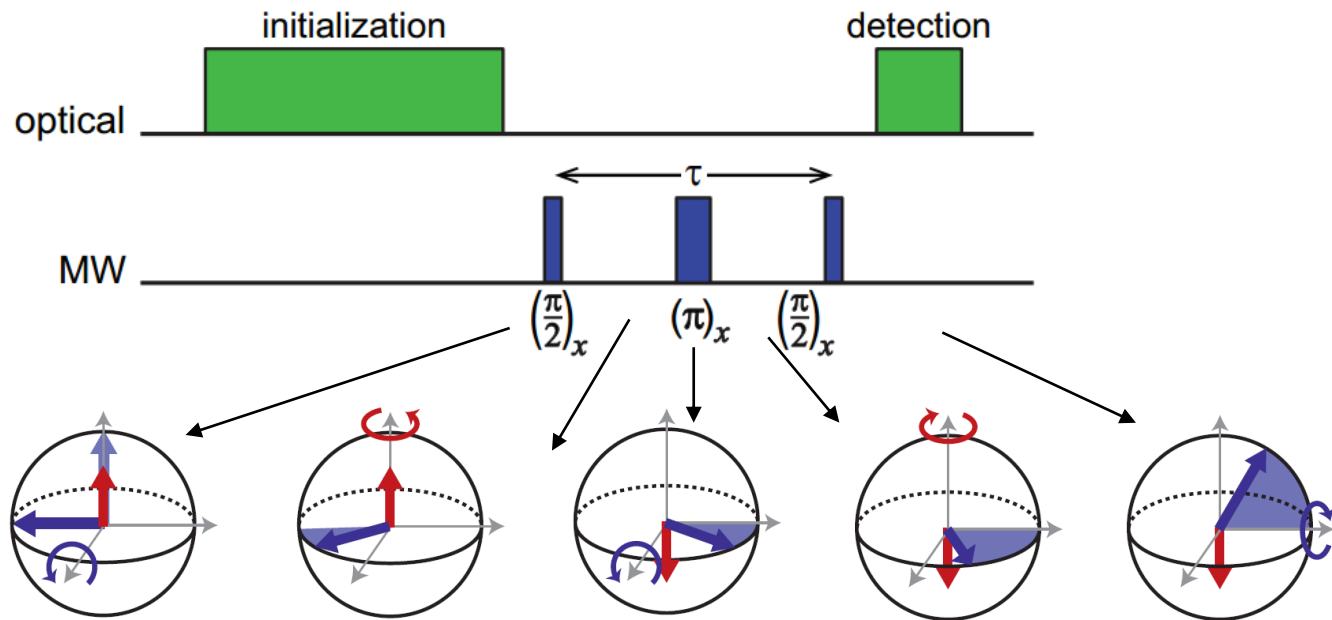
# Spin physics and coherence properties of the NV center

- $T_2^*$ : inhomogeneous dephasing time measured by Ramsey sequences



# Spin physics and coherence properties of the NV center

- $T_2$  : spin-spin dephasing time measured by Hahn echo or decoupling sequences



Larmor precession of  $^{13}\text{C}$  nuclear spins ( $I = 1/2$ )

# Unique properties of the NV center

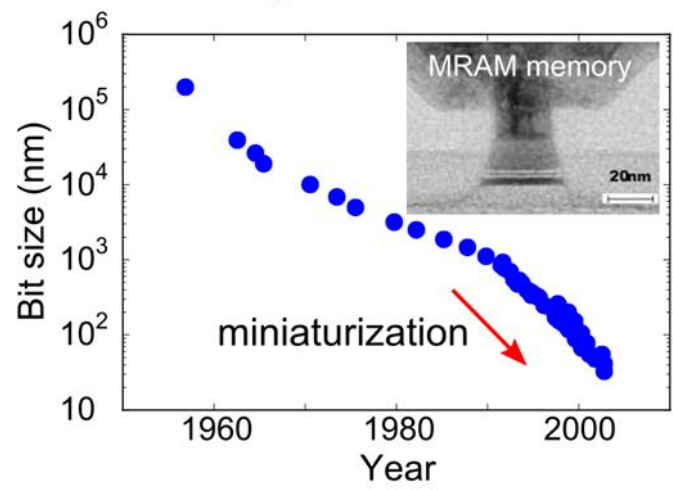
- Spin qubits (or artificial atoms) in solid-state material (e.g. wide band gap, low spin-orbit coupling, large Debye temperature)
- Atomic-scale defect for high spatial resolution imaging
- Optical initialization and readout of spin state
- Long coherence times at even room temperature ( $T_2 > \text{ms}$ )
- Fast spin control and qubit gates ( $\sim \text{ns}$ )
- Operates from cryogenic temperatures to ambient
- Chemically stable, non-toxic and bio-friendly
- Optically stable (free from photobleaching)
- High field sensitivity e.g. magnetic, electric, strain field, temperature

Property	Sensitivity	Property	Sensitivity
Magnetic field	$< 1 \text{ nT/Hz}^{1/2}$	Strain field	$< 10^{-7} \text{ /Hz}^{1/2}$
Electric field	$< 100 \text{ Vcm}^{-1} \text{ /Hz}^{1/2}$	Temperature	$< 0.1 \text{ K/Hz}^{1/2}$

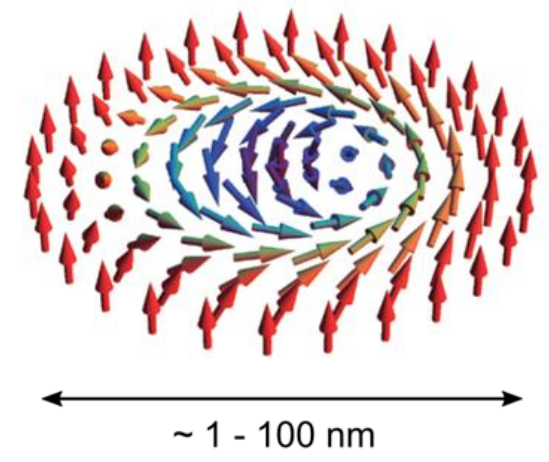
- Basics of the NV center
  - Structure, electronic, optical properties
  - Spin physics, coherence properties
- Applications for quantum metrology
  - Magnetic field sensing
  - Strain field sensing

# Magnetic field sensing with high sensitivity and high spatial resolution

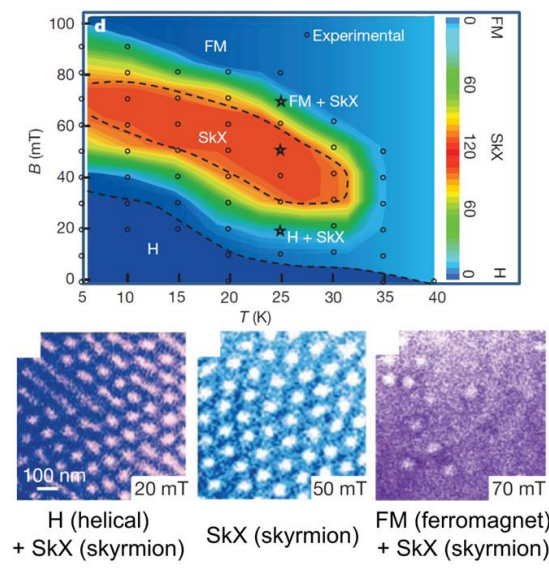
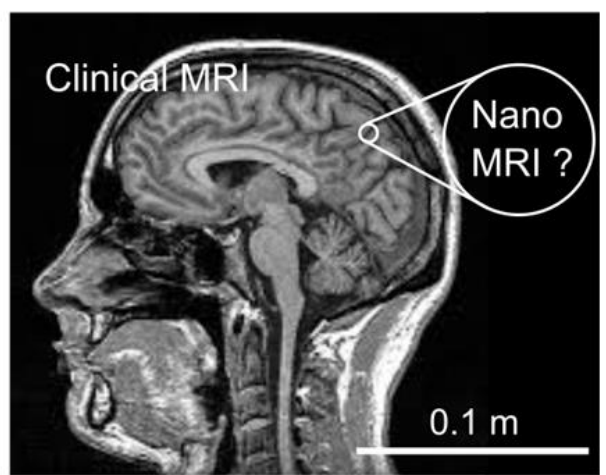
## Magnetic information



## Skyrmion

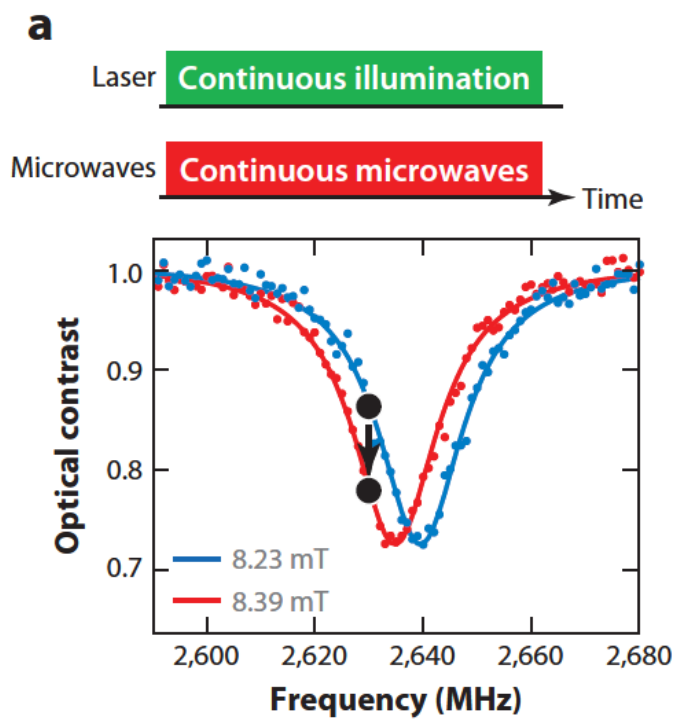


## Biomedicine

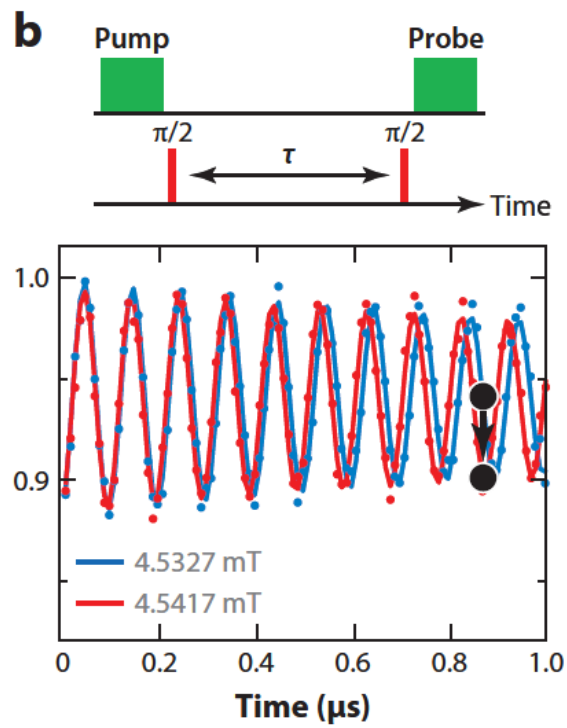


# Magnetic field sensing: detecting schemes of DC field

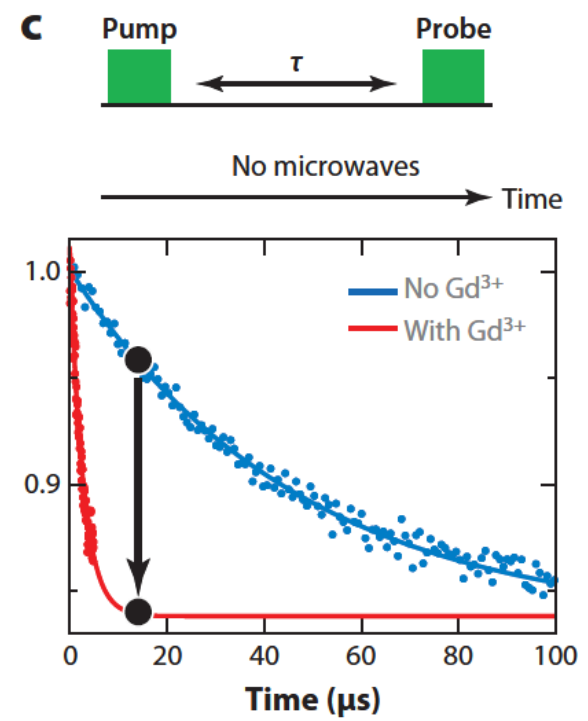
## CW ESR method



## Pulsed ESR method e.g. Ramsey sequences



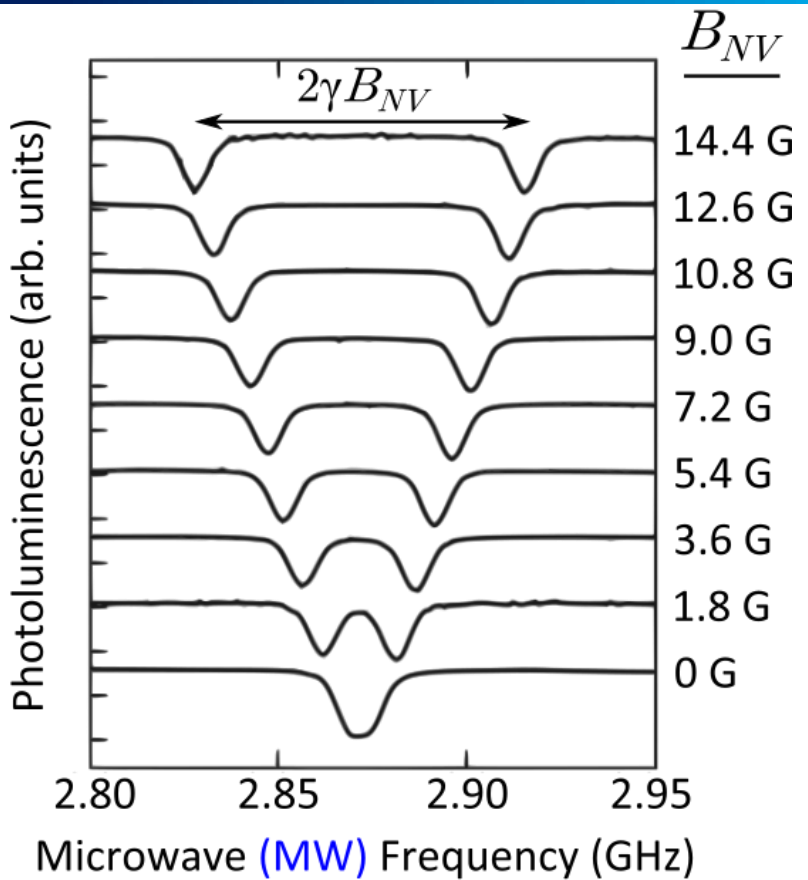
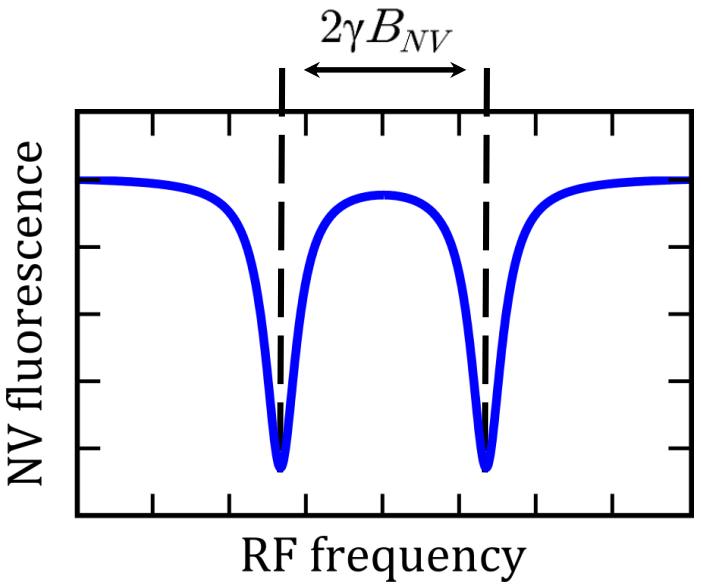
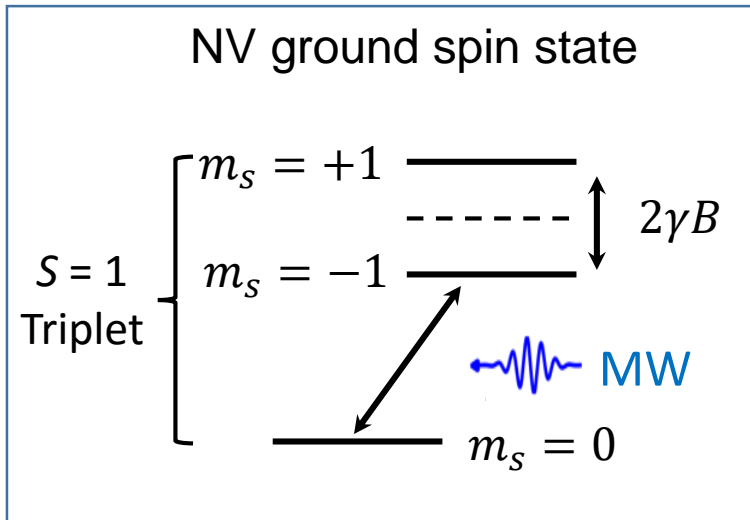
## $T_1$ relaxometry



Oscillation frequency  
 $\propto \delta$  (detuning)

# Magnetic field sensing: detecting schemes of DC field

## CW ESR method



$$\eta_{DC} = \delta B_{min} \sqrt{t} \approx \frac{\Delta f \sqrt{t}}{\gamma C \sqrt{I_0}}$$

measurement time

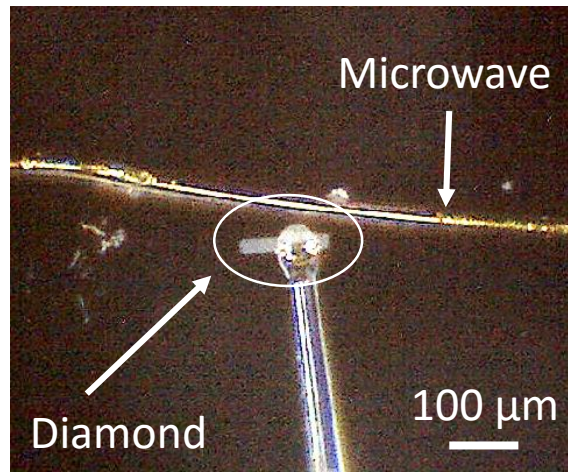
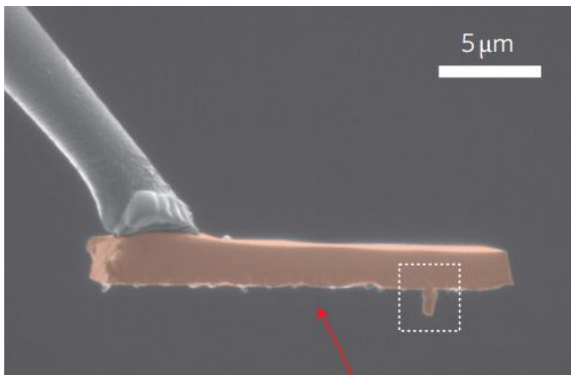
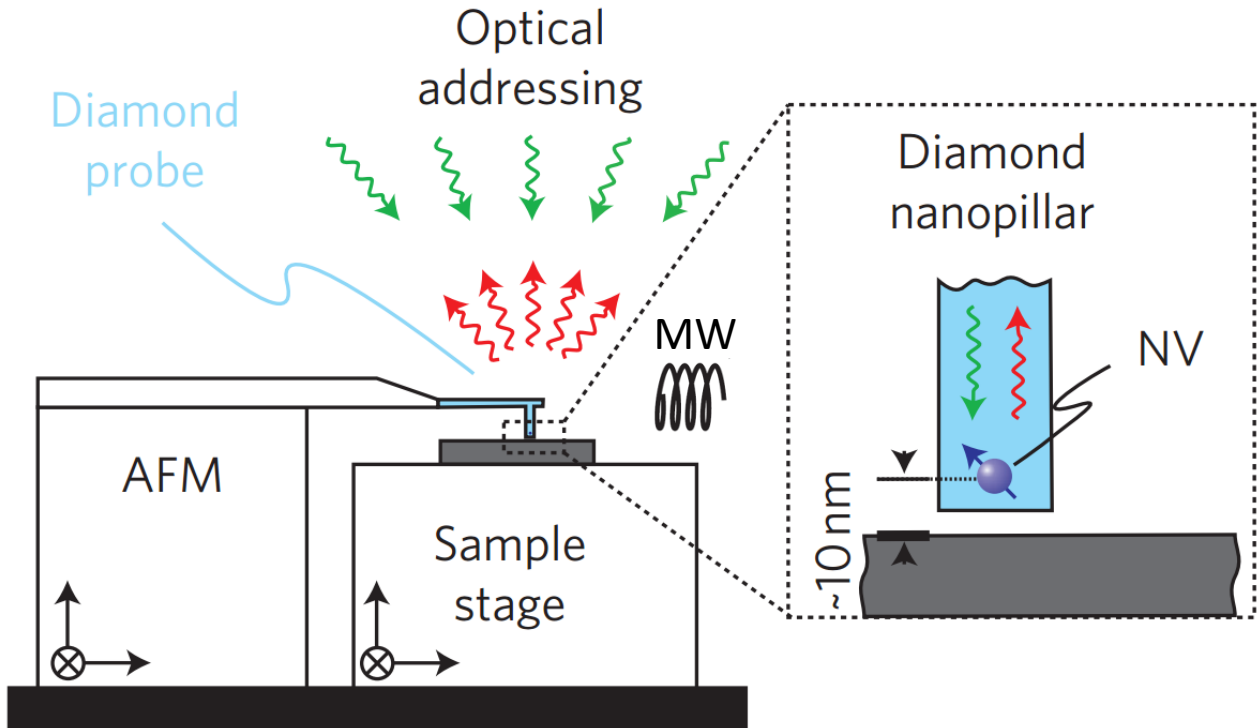
linewidth

$\gamma \approx 2.8 \text{ MHz/G}$

$C \approx 20 - 30\%$

Photon count rate

# Example of DC field imaging with scanned probes

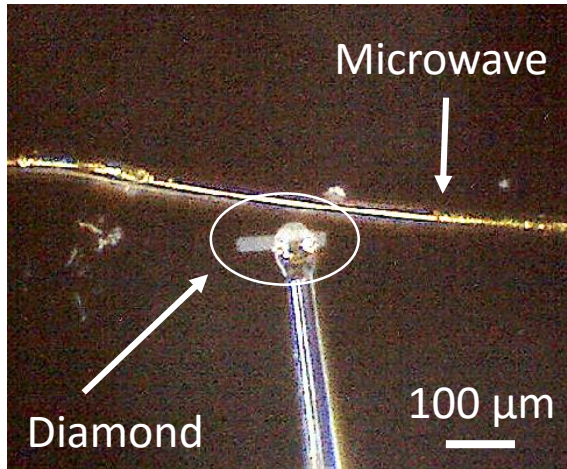


UCSB setup

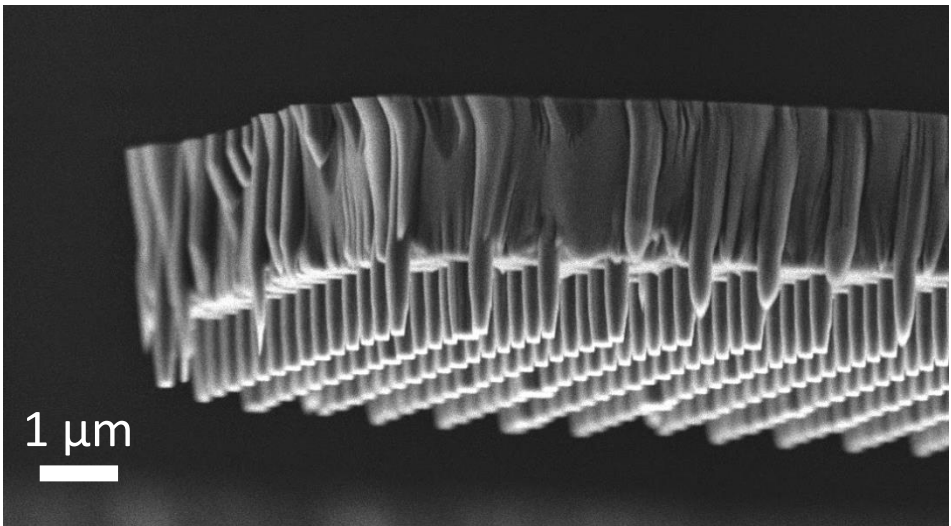
P. Malentinsky *et al.*, Nature Nanotechnology (2012)



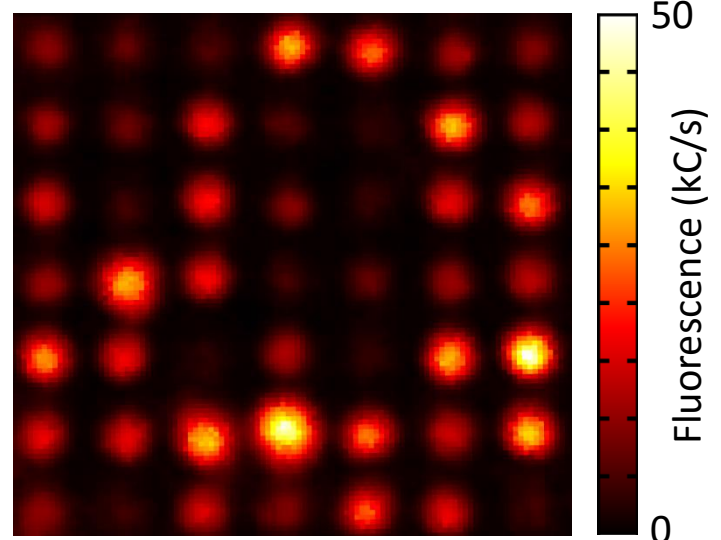
# Example of DC field imaging with scanned probes



UCSB setup

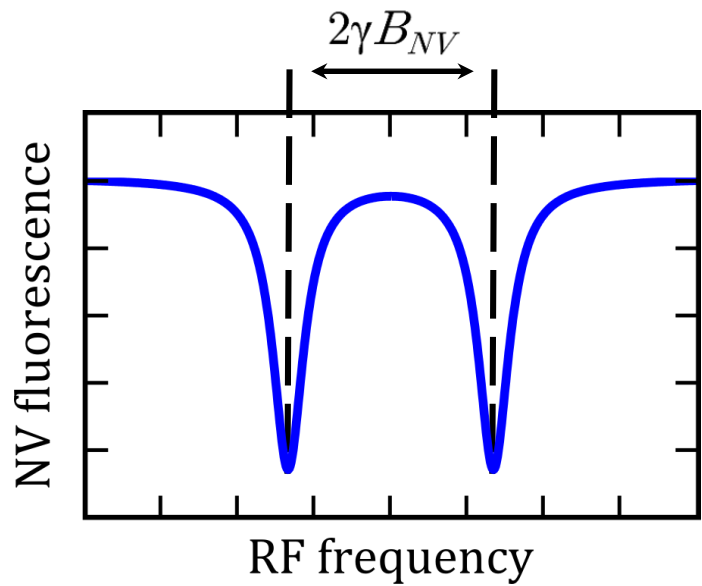


Confocal scan (30 μW @ 532 nm)

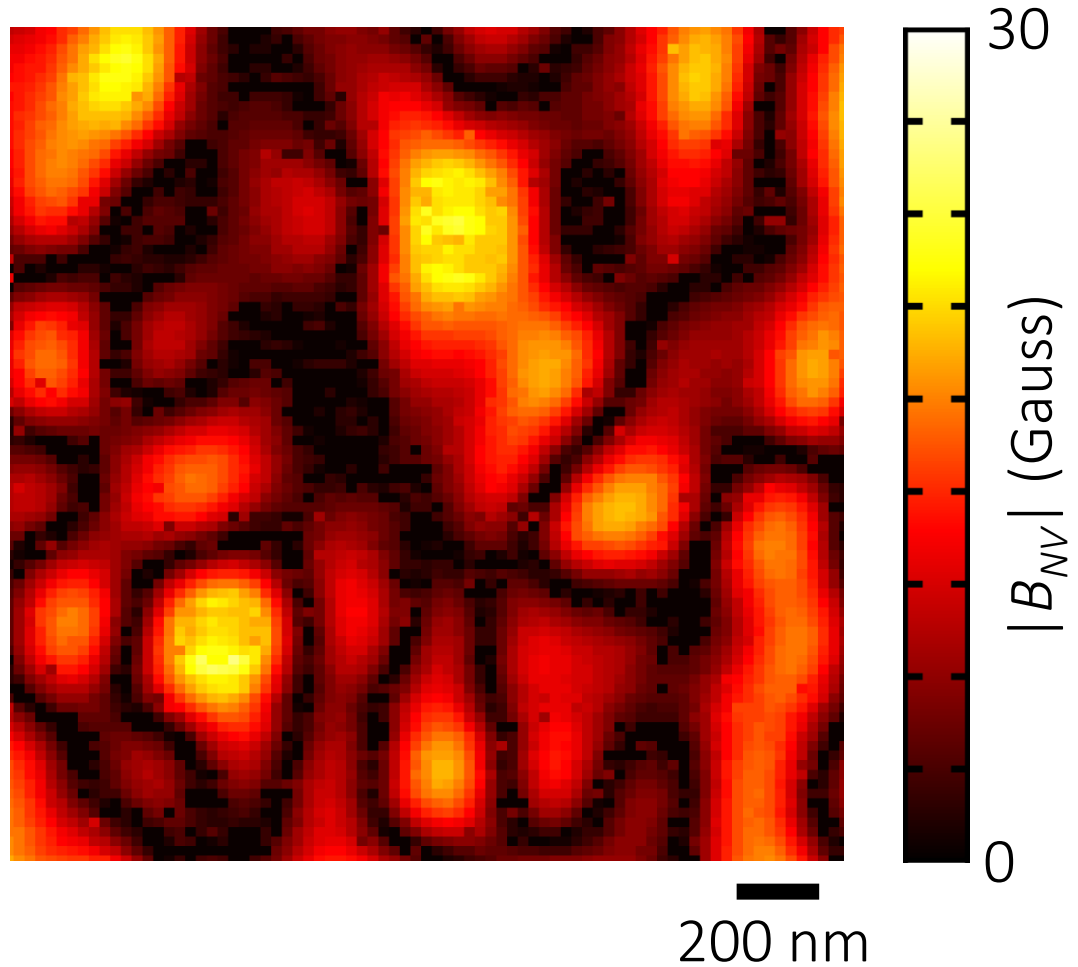


- Single crystal diamond cantilevers fabricated with pillars to aid in photon collection
- NV depth ~ 20 nm, on average 1 NV per pillar
- These cantilevers are then attached to custom tuning fork probes for force sensing

# Example of DC field imaging: hard disk



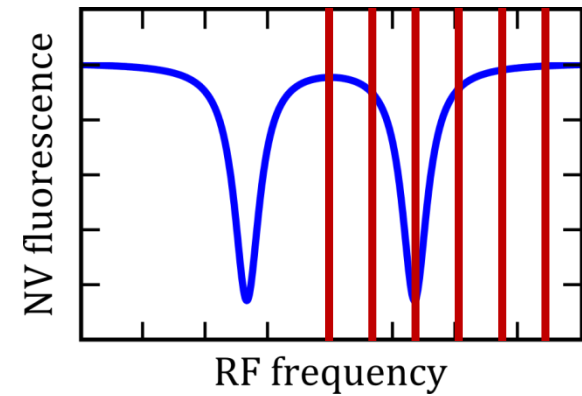
30  $\mu$ W @ 532 nm  
2 seconds per pixel



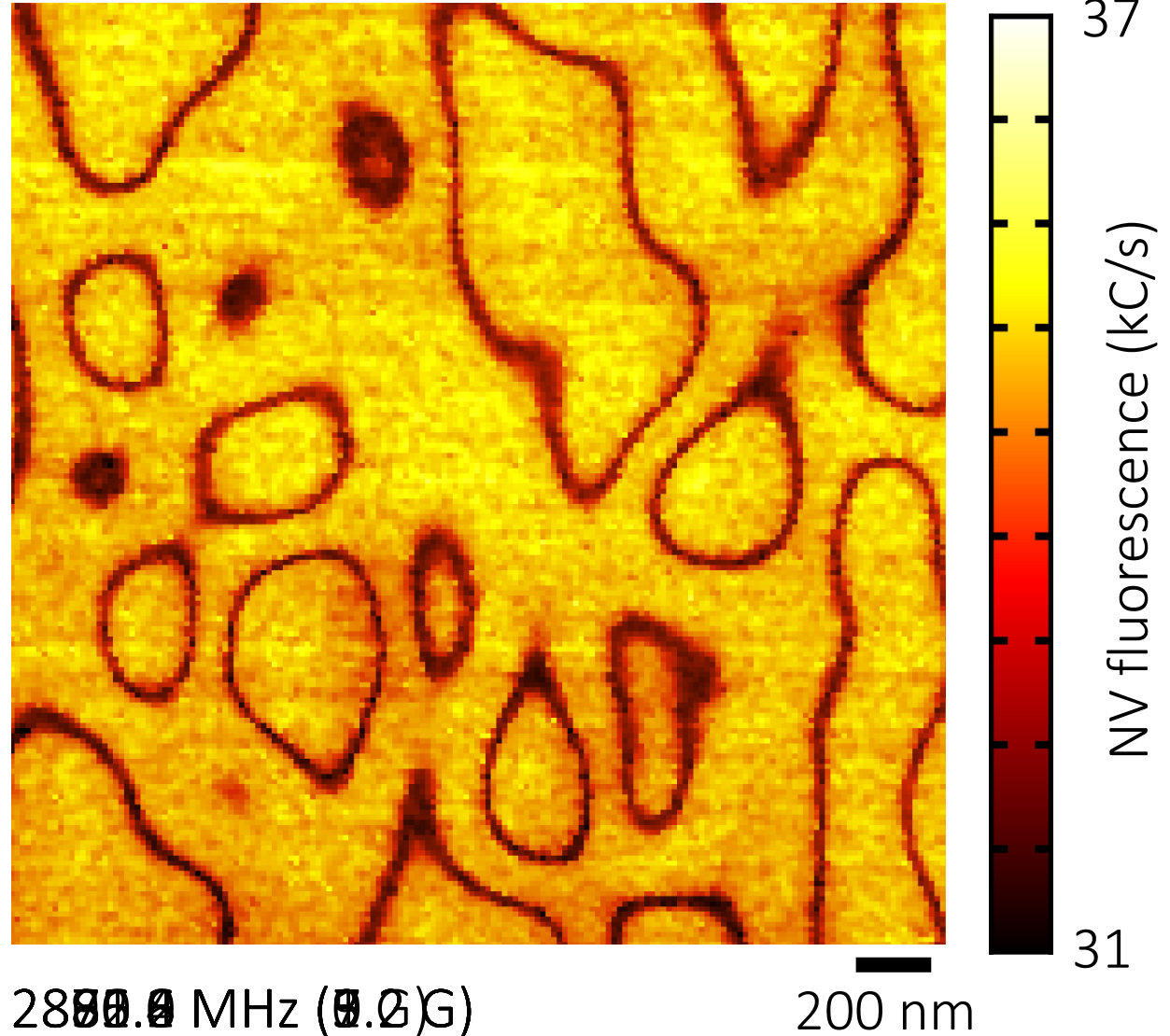
DC field sensitivity: 0.32 G/ $\nu$ Hz, dynamic range: 30 Gauss

# Example of DC field imaging: hard disk

Alternate method: Use a fixed RF frequency to trace out magnetic field contours.

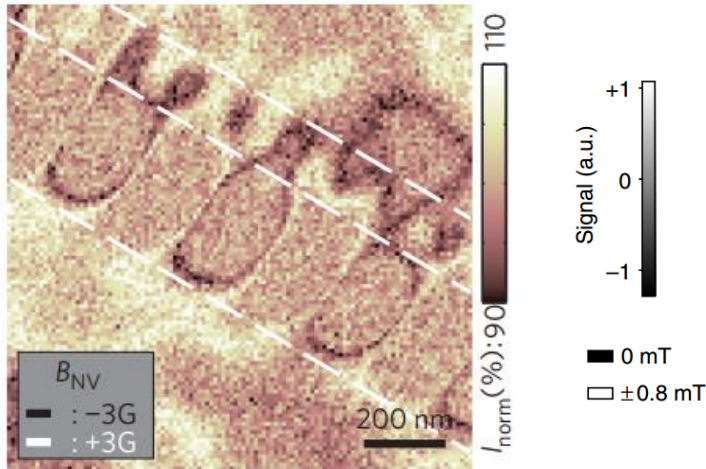


30  $\mu$ W @ 532 nm  
0.1 seconds per pixel  
DC sensitivity: 0.03 G/ $\sqrt{\text{Hz}}$   
Dynamic range: 1 Gauss



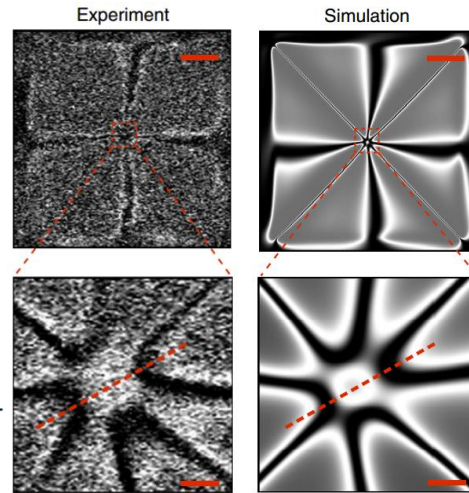
# More examples of DC field imaging

## Hard disk



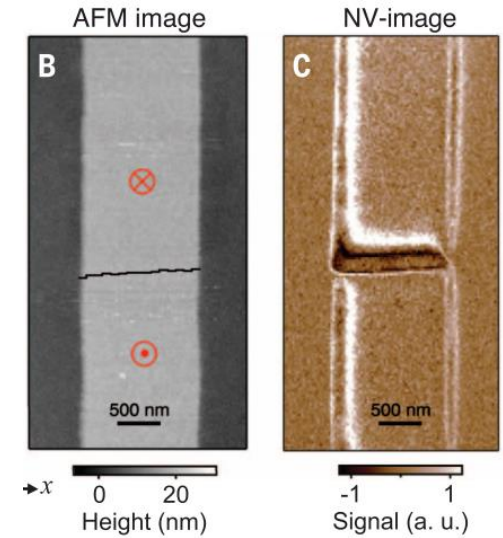
P. Malentinsky *et al.*, Nature Nanotechnology (2012)

## Magnetic vortex



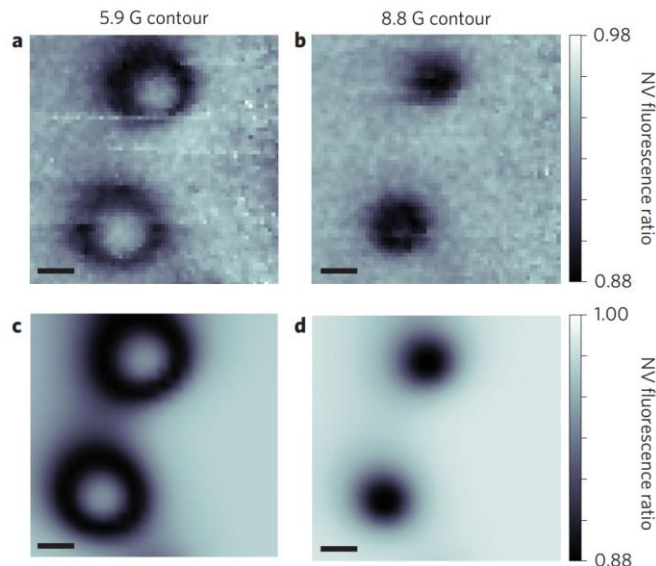
L. Rondin *et al.*, Nature Communications (2013)

## Domain wall



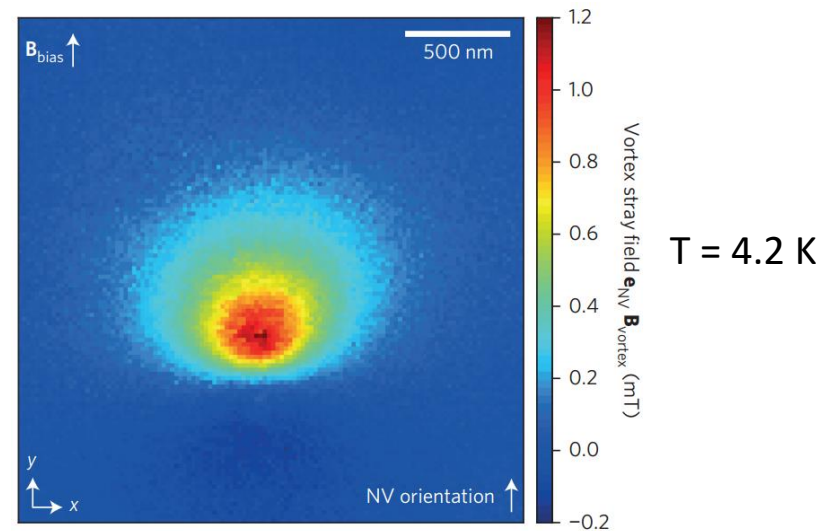
J. P. Tetienne *et al.*, Science (2014)

## Superconducting vortices in $\text{BaFe}_2(\text{As}_{0.7}\text{P}_{0.3})_2$



M. Pelliccione *et al.*, Nature Nanotechnology (2016)

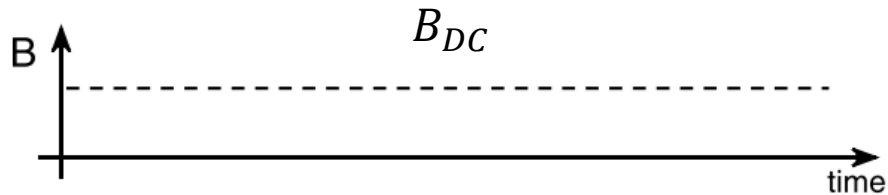
## Superconducting vortex in YBCO



L. Thiel *et al.*, Nature Nanotechnology (2016)

# Magnetic field sensing: detecting schemes of DC field

Pulsed ESR method e.g. Ramsey sequences  $\frac{\pi}{2} - \tau - \frac{\pi}{2}$



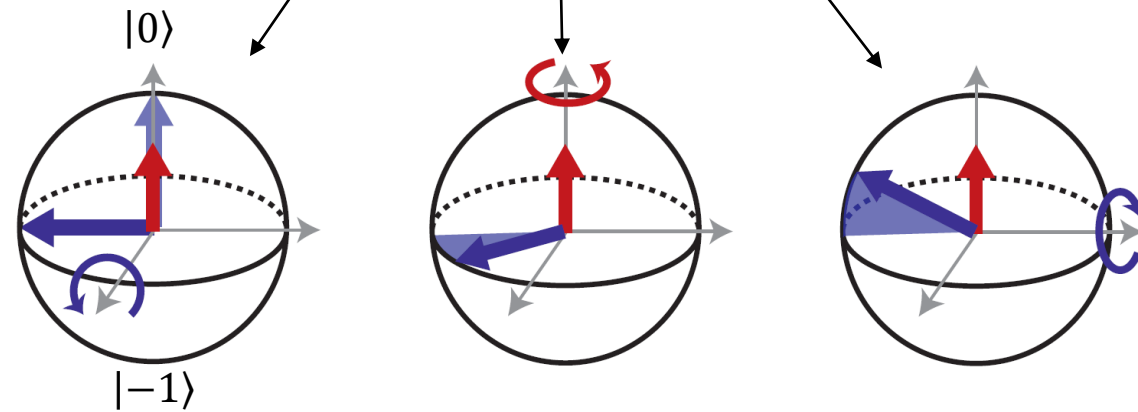
Photon shot-noise limited DC field sensitivity

$$\eta_{DC} \approx \frac{1}{\gamma} \frac{1}{C \sqrt{I_0}} \frac{1}{\sqrt{T_2^*}}$$

$T_2^*$ : inhomogeneous dephasing time

$$\eta_{DC} \sim 10 \text{ nT}/\sqrt{\text{Hz}}$$

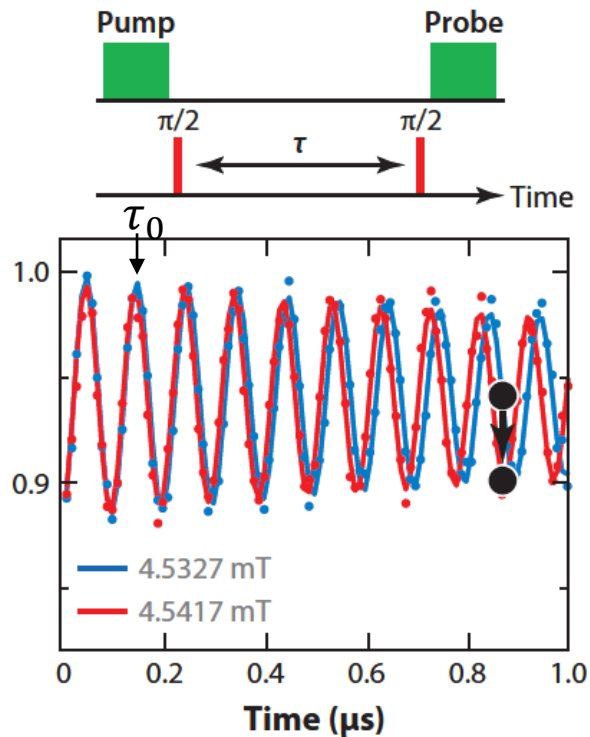
$$(T_2^* \sim 100 \mu\text{s})$$



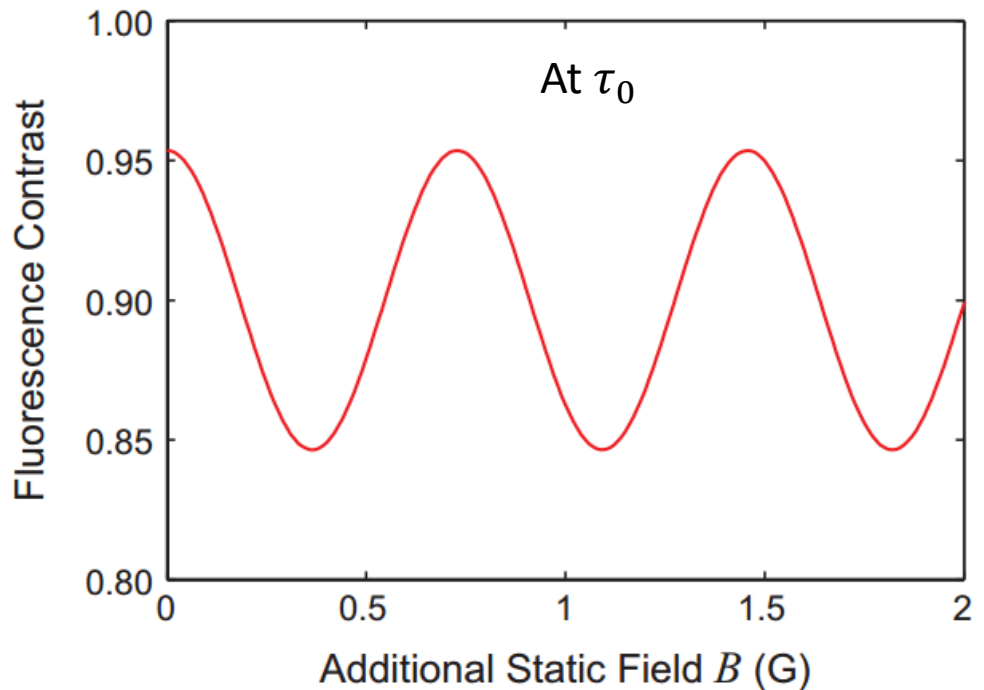
$$|\psi\rangle = \frac{1}{\sqrt{2}} (|0\rangle + |-1\rangle)$$

$$|\psi\rangle = \frac{1}{\sqrt{2}} (|0\rangle + e^{i\phi} |-1\rangle) \quad \phi = \gamma B_{DC} \tau$$

# Magnetic field sensing: detecting schemes of DC field



R. Schirhagl *et al.*, *Annu. Rev. Phys. Chem.* (2014)



Photon signal :

$$S = \frac{a+b}{2} + \frac{a-b}{2} \cos(\phi) = \frac{a+b}{2} + \frac{a-b}{2} \cos(\gamma B_{DC} \tau)$$

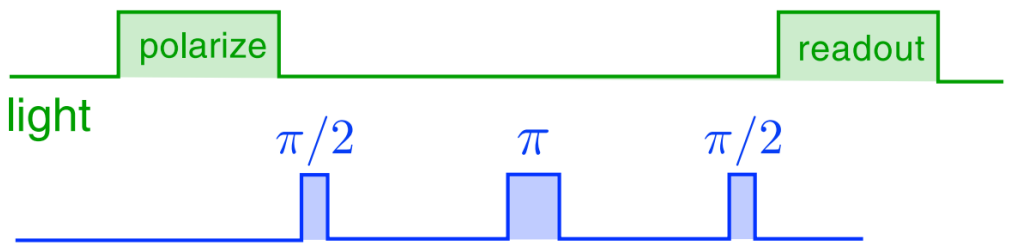
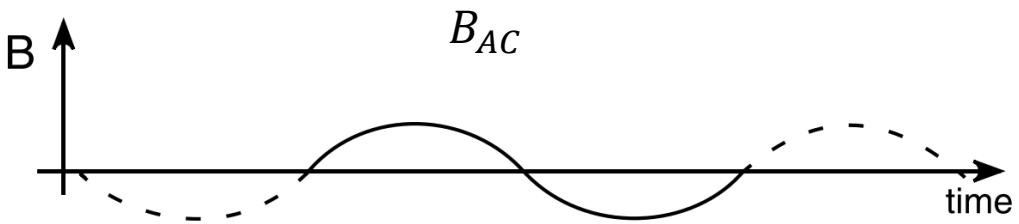
$a$  : number of photons at  $\phi = 0$

$b$  : number of photons at  $\phi = \pi$

# Magnetic field sensing: detecting schemes of AC field

Advanced pulse method e.g. Hahn echo sequence

$$\frac{\pi}{2} - \tau - \pi - \tau - \frac{\pi}{2}$$



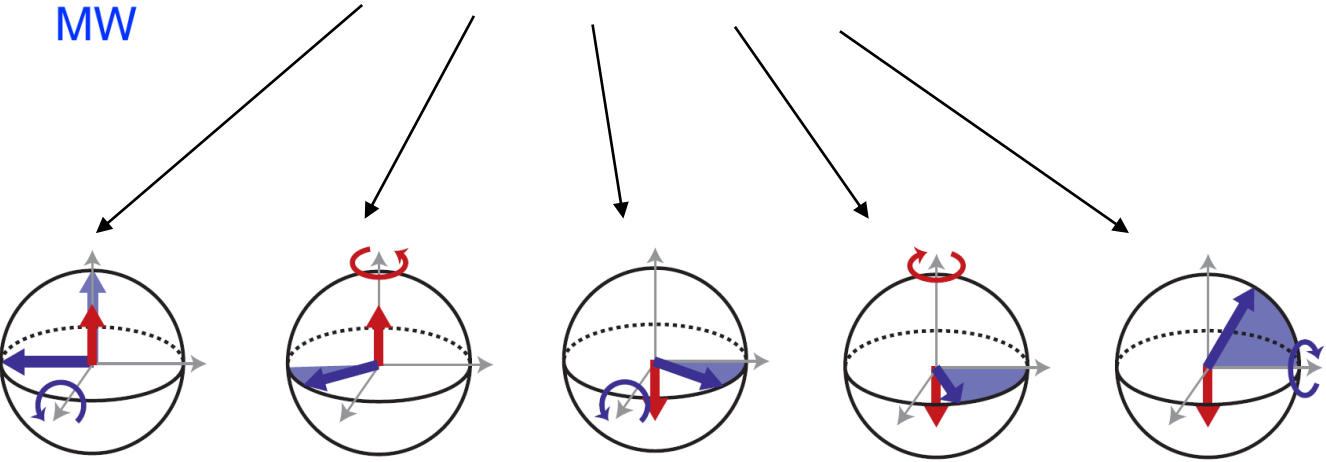
AC field sensitivity

$$\eta_{AC} \approx \frac{1}{\gamma} \frac{1}{C\sqrt{I_0}} \frac{1}{\sqrt{T_2}}$$

$T_2$  : dephasing time

$$\eta_{AC} \sim 1 \text{ nT}/\sqrt{\text{Hz}}$$

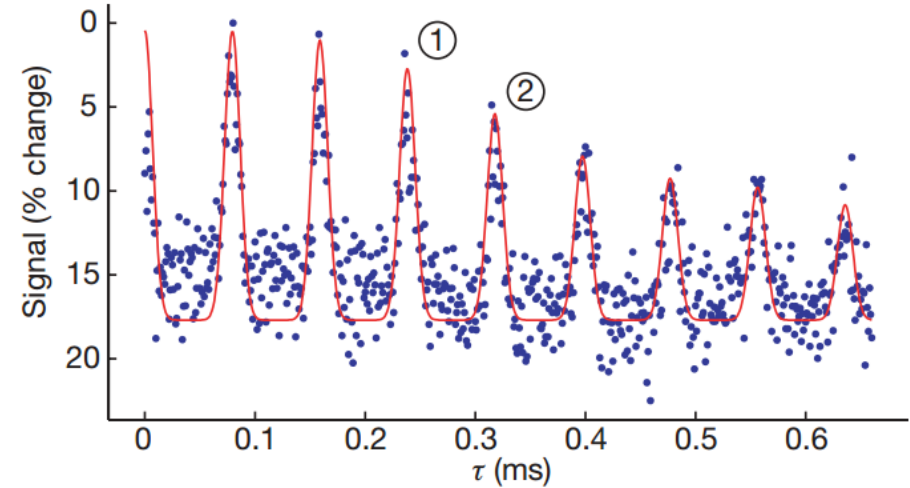
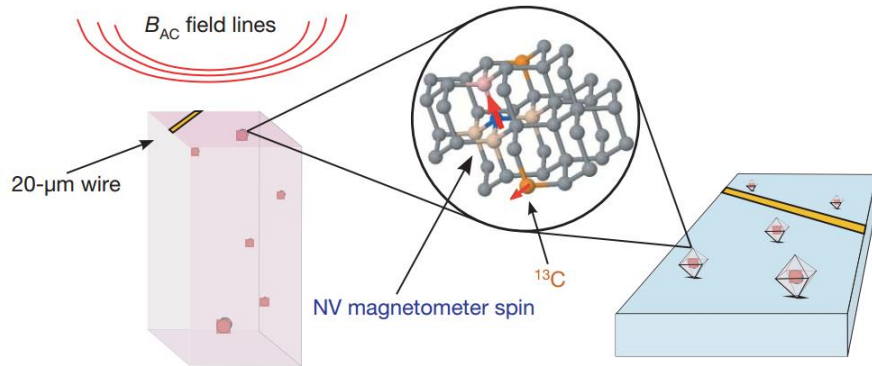
( $T_2 \sim 1 \text{ ms}$ )



$$\phi = 4\gamma B_{AC}\tau$$

L. Rondin *et al.*, Rep. Prog. Phys. (2014)  
 S. Hong *et al.*, MRS Bulletin (2013)

# Magnetic field sensing: detecting schemes of AC field

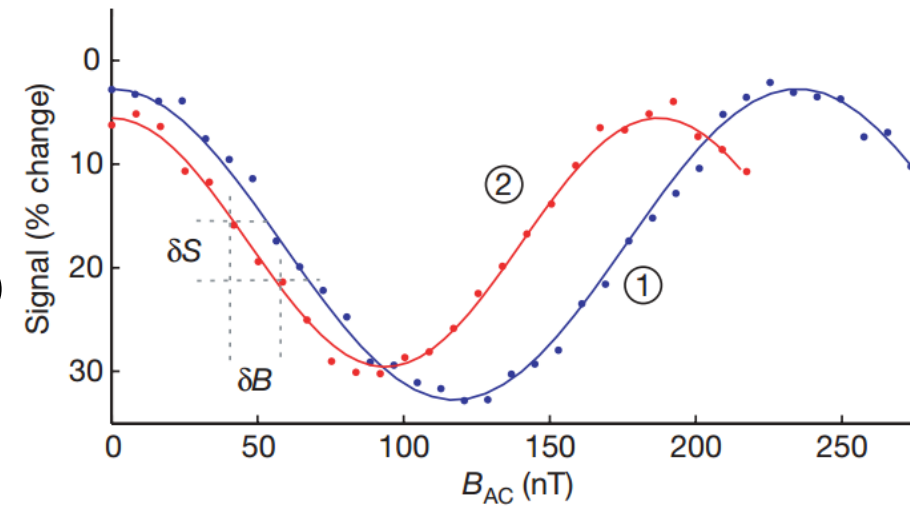


Photon signal :

$$S = \frac{a+b}{2} + \frac{a-b}{2} \cos(\phi) = \frac{a+b}{2} + \frac{a-b}{2} \cos(4\gamma B_{AC} \tau)$$

$a$  : number of photons at  $\phi = 0$

$b$  : number of photons at  $\phi = \pi$

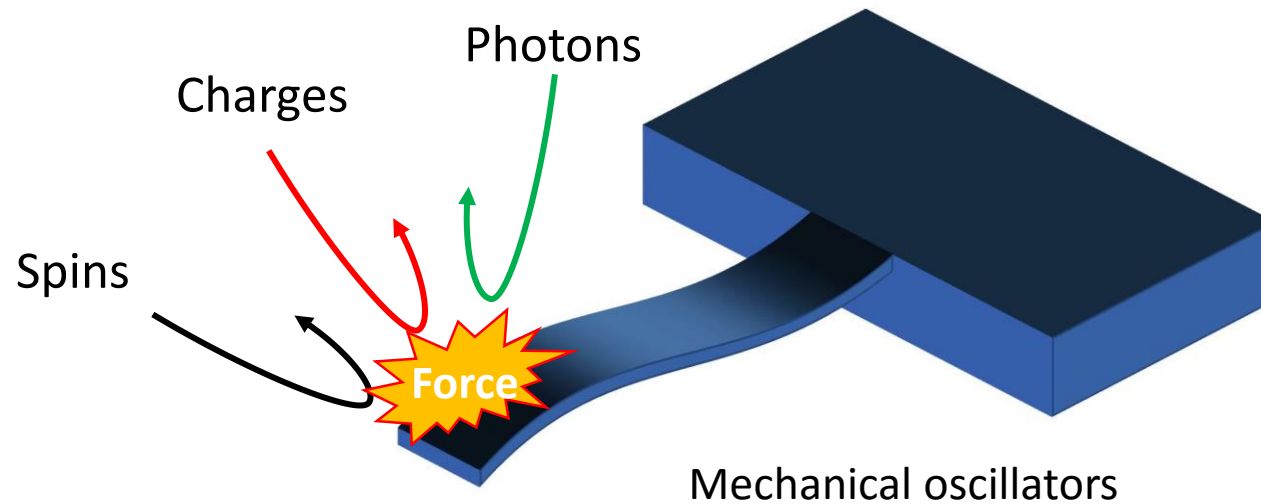


$$\eta_{AC} \sim 30 \text{ nT}/\sqrt{\text{Hz}}$$

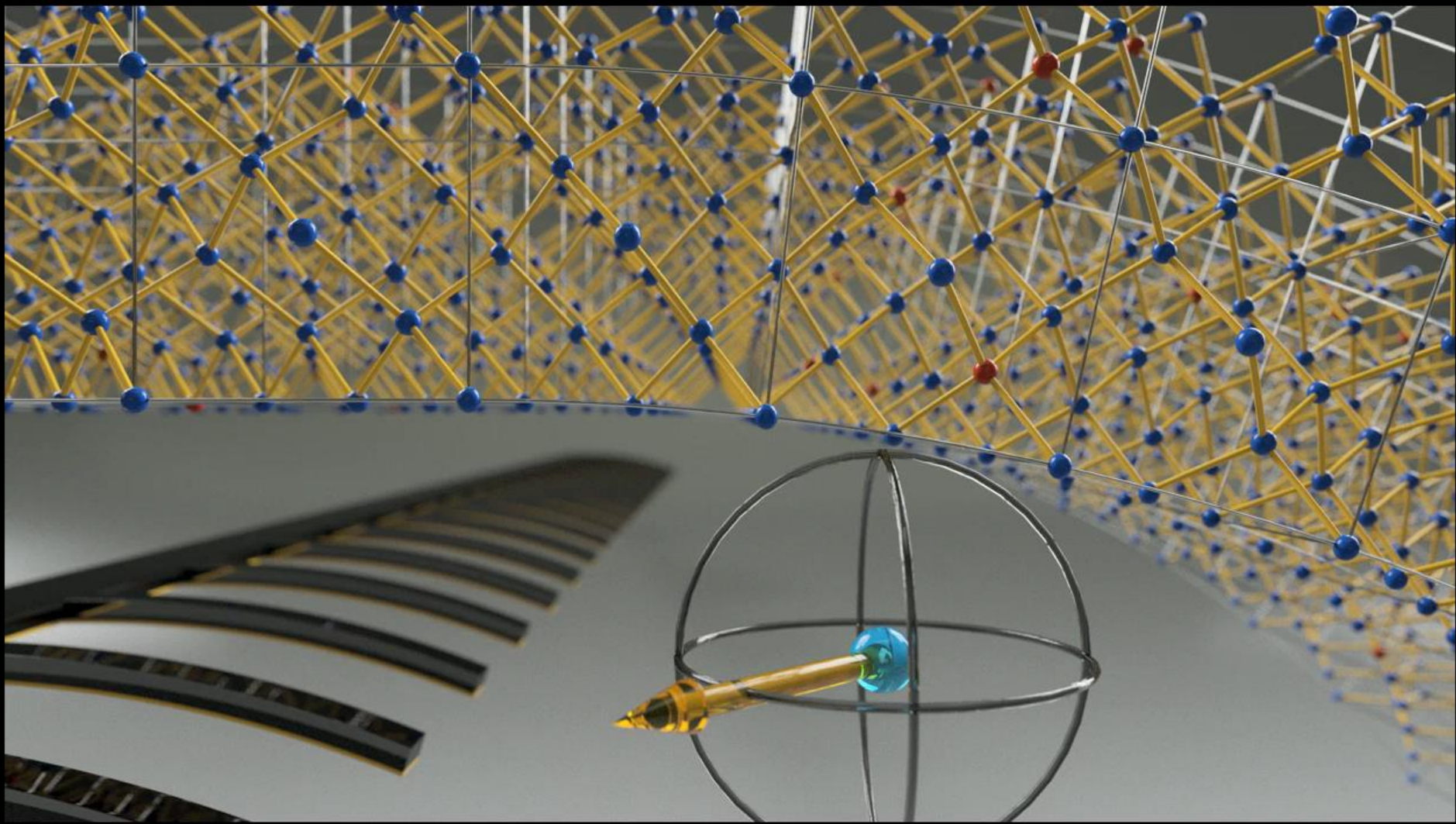


- Basics of the NV center
  - Structure, electronic, optical properties
  - Spin physics, coherence properties
- Applications for quantum metrology
  - Magnetic field sensing
  - Strain field sensing

# Strain field sensing with high sensitivity

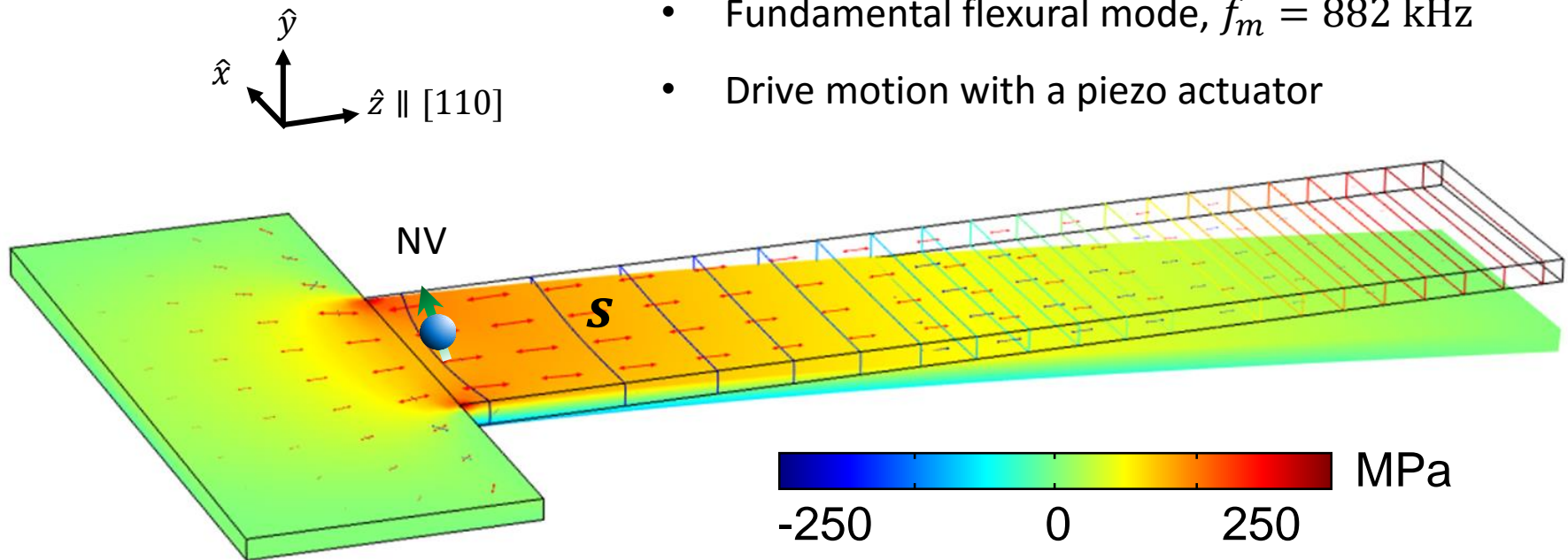


- Quantum sensors for force, mass, displacement, acceleration...
- Universal interface in quantum networks
- Quantum measurements in macroscopic mechanical object



# Strain field sensing

- Simulated stress profile of our cantilever (COMSOL)
- $60 \mu\text{m} \times 15 \mu\text{m} \times 1.1 \mu\text{m}$ , NV depth = 51.5 nm
- Fundamental flexural mode,  $f_m = 882 \text{ kHz}$
- Drive motion with a piezo actuator

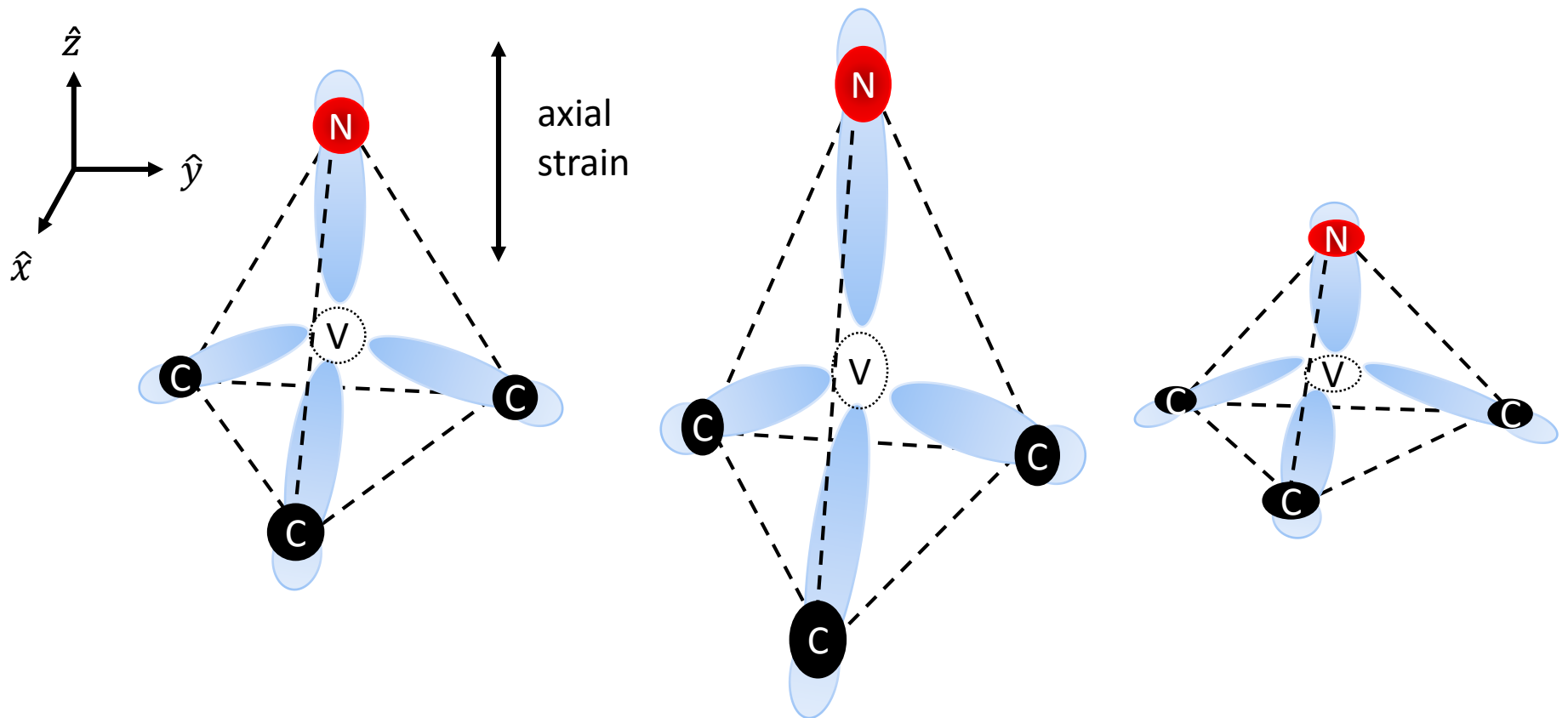


Strain tensor

$$\varepsilon = \begin{pmatrix} -\nu s & 0 & 0 \\ 0 & -\nu s & 0 \\ 0 & 0 & s \end{pmatrix}$$

$s$  : strain along cantilever axis  
 $\nu$  : Poisson ratio, 0.11

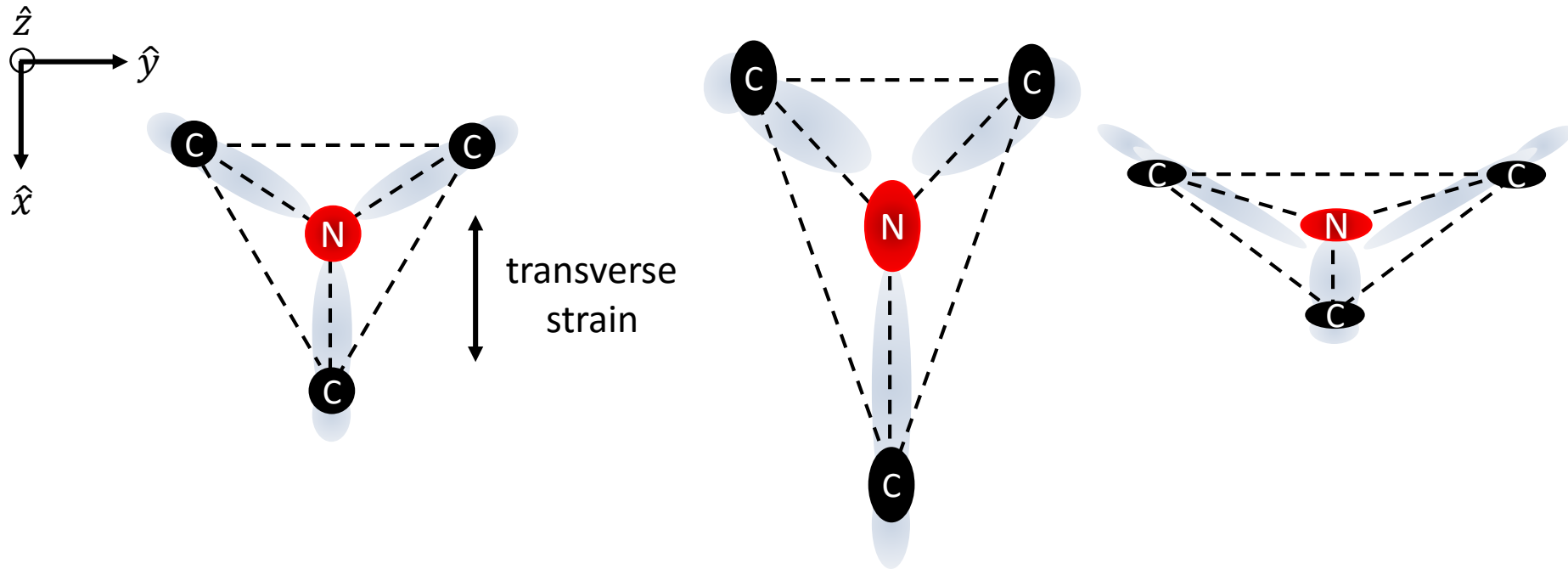
# Strain field sensing



Energy levels change followed by  $C_{3v}$  symmetry group

- axial strain: uniform shift of all energy levels

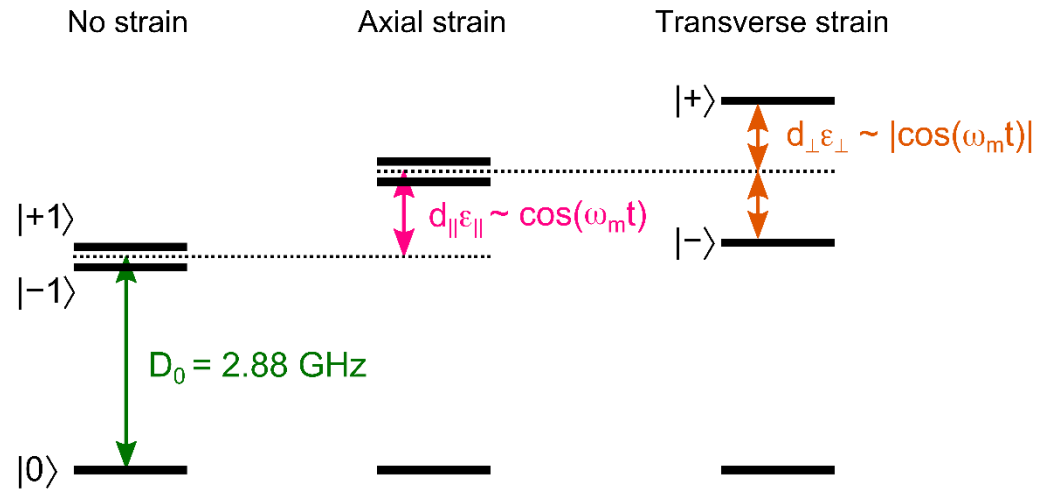
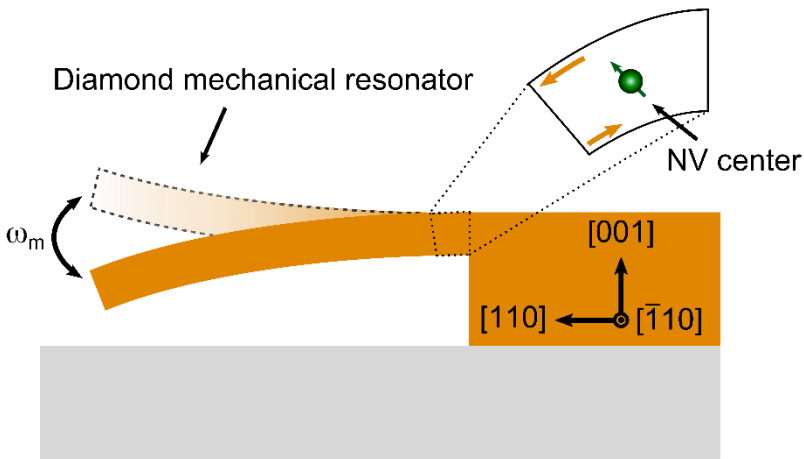
# Strain field sensing



Energy levels change followed by  $C_{3v}$  symmetry group

- axial strain: uniform shift of all energy levels
- transverse strain: split and mix of energy levels (orbitals along  $\hat{x}$  and  $\hat{y}$ )

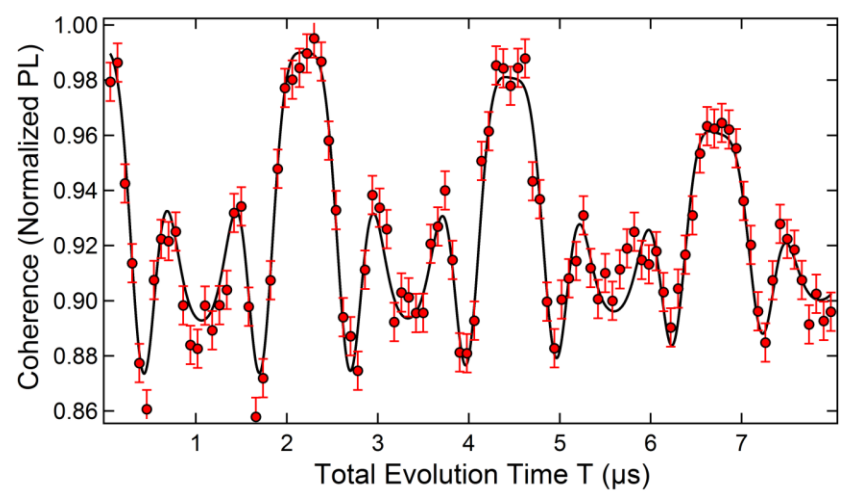
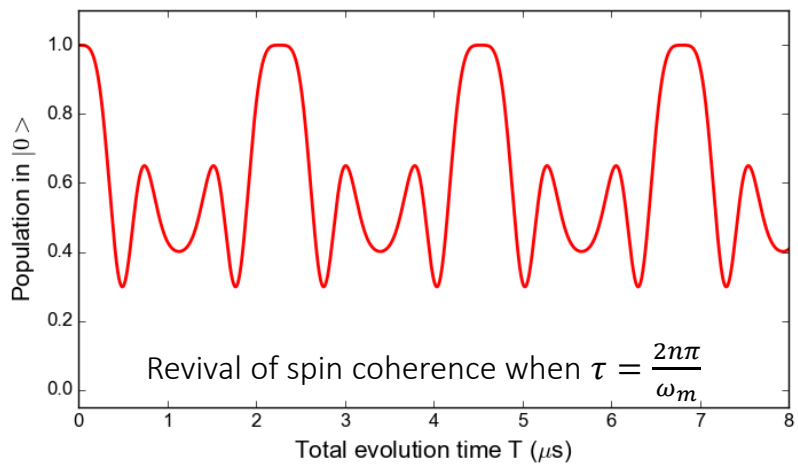
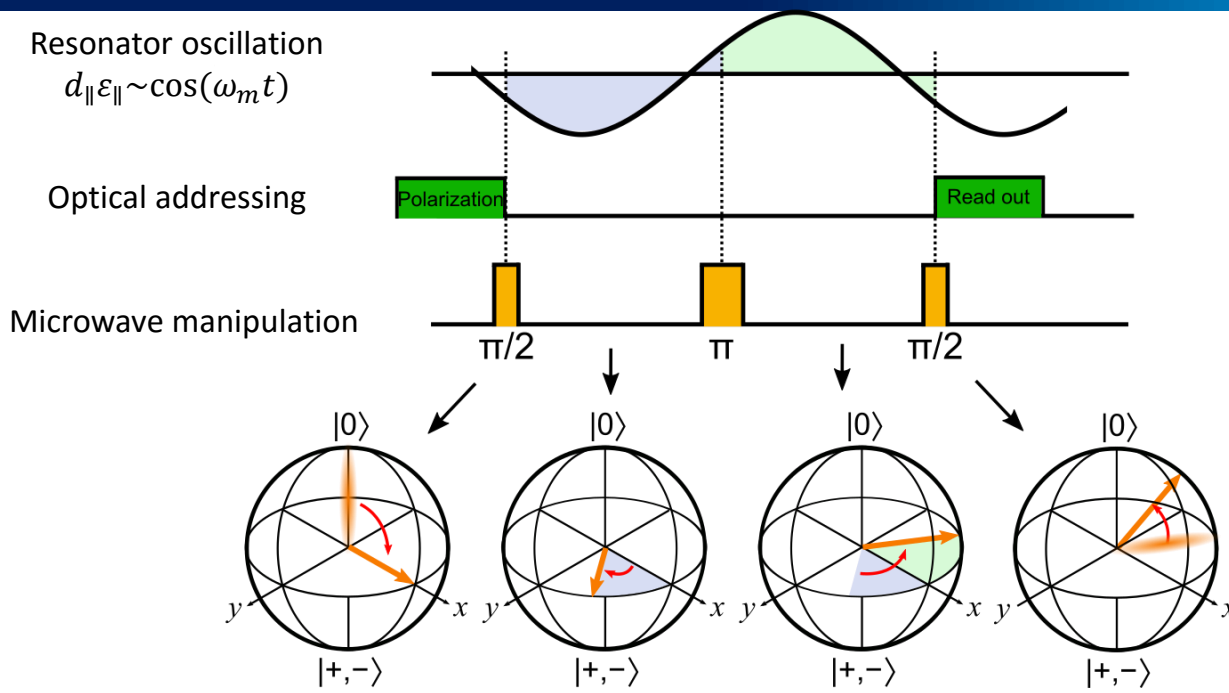
# Ground state Hamiltonian and energy level change



$$E_{\pm}(s) = D_0 + d_{\parallel}\epsilon_{\parallel} \pm \sqrt{(\gamma_{NV}B_z)^2 + (d_{\perp}\epsilon_{\perp})^2}$$

- AC parallel strain modulates at mechanical frequency
- AC perpendicular strain modulates at twice mechanical frequency

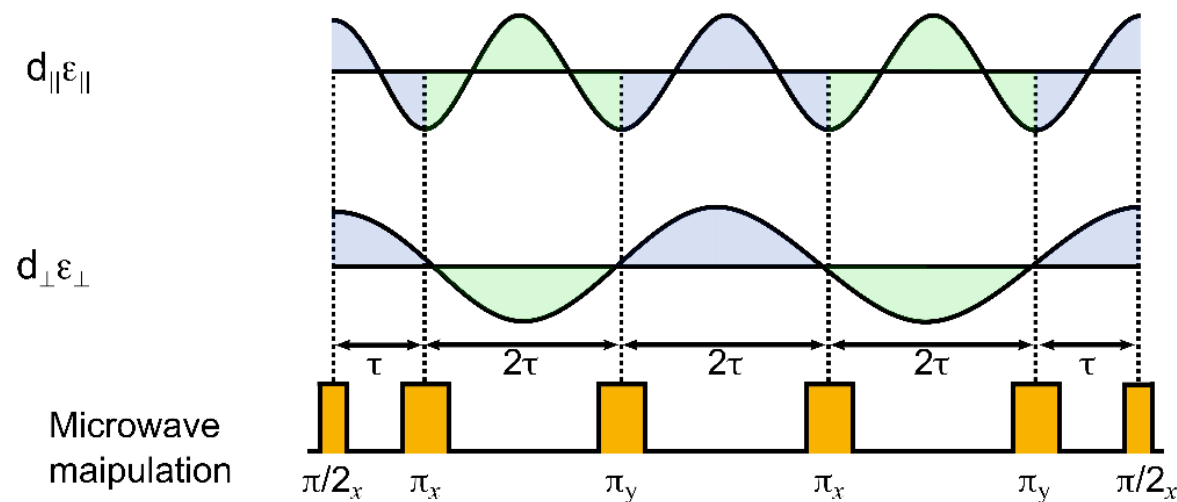
# Axial strain detection with Hahn echo pulse sequence



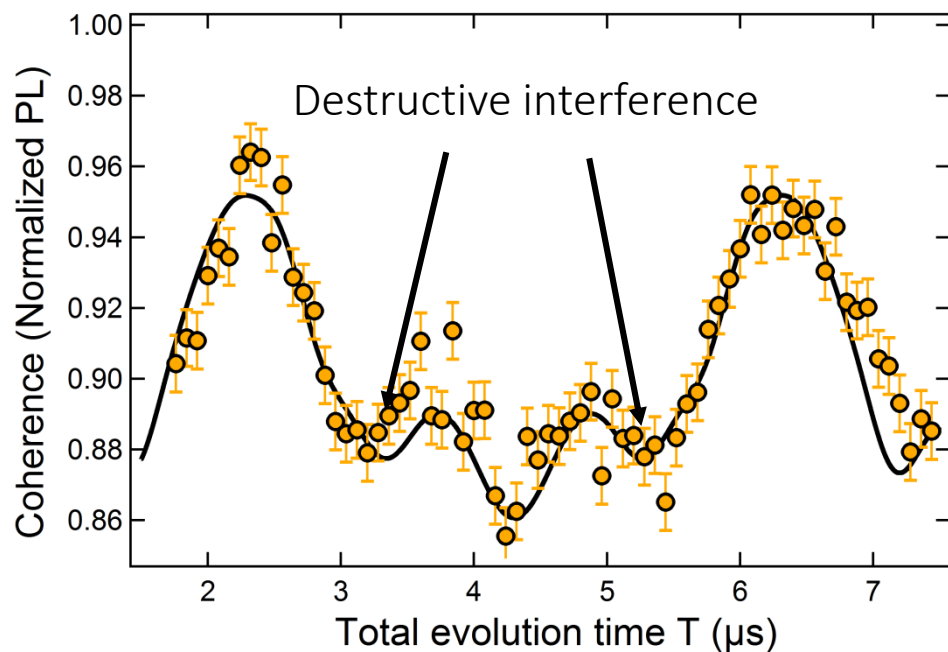
$$d_{\parallel} = 13.4 \pm 0.8 \text{ GHz/strain}$$



# Transverse strain detection with XY-4 pulse sequence



- XY-4 pulse sequence used
- Interference between axial strain ( $\sim \omega_m$ ) and transverse strain ( $\sim 2\omega_m$ )



$$d_{\perp} = 21.5 \pm 0.8 \text{ GHz/strain}$$

- Basics of the NV center
  - Structure, electronic, optical properties
  - Spin physics, coherence properties
- Applications for quantum metrology
  - Magnetic field sensing
  - Strain field sensing
- Other applications (next time ?)