



**Condensed Matter Seminar  
(Korea University)**

**Doping in semiconductors &  
New magnetic phase transitions in P-doped metallic Si**

**2016. 03. 23.**

**임 현식**

**동국대학교, 물리반도체과학부**



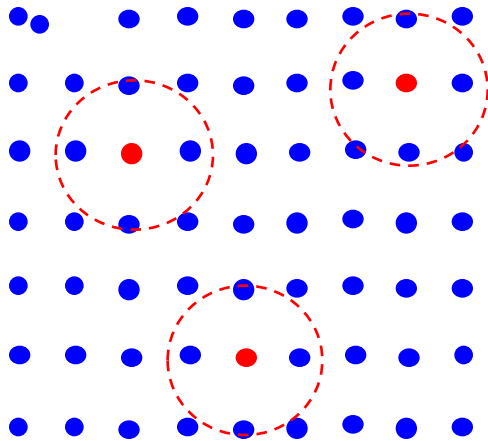
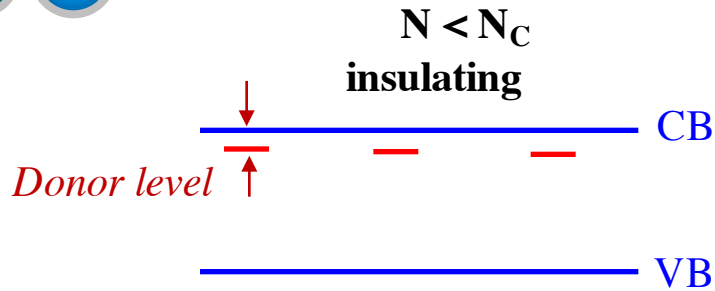
## Brief introduction

- Doping in semiconductors: Metal insulator transition (MIT)
- Single-particle DOS gap near the MIT region

## Results and discussion

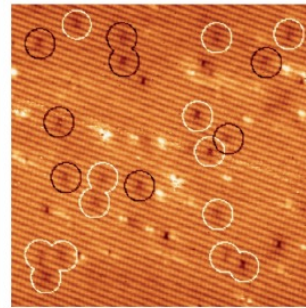
- **Novel quantum phases and quantum phase transitions**  
*in quasi-degenerate metallic Si:P*

# Impurity band in P-doped silicon (Si:P)

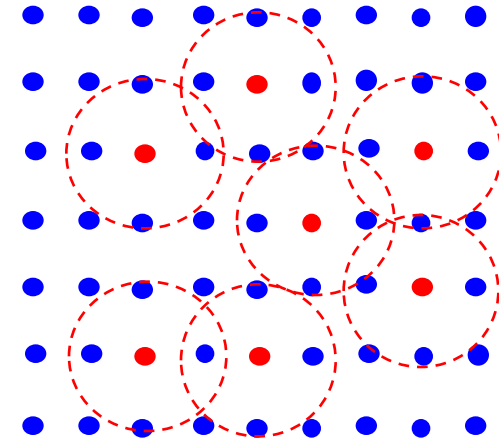
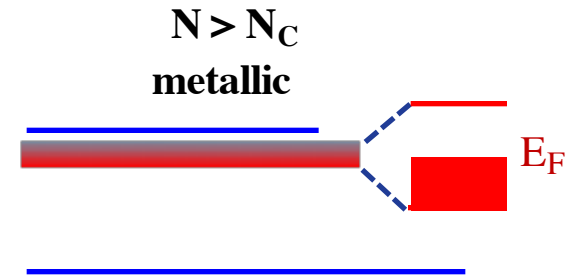


**Isolated impurity level**

Localized moments



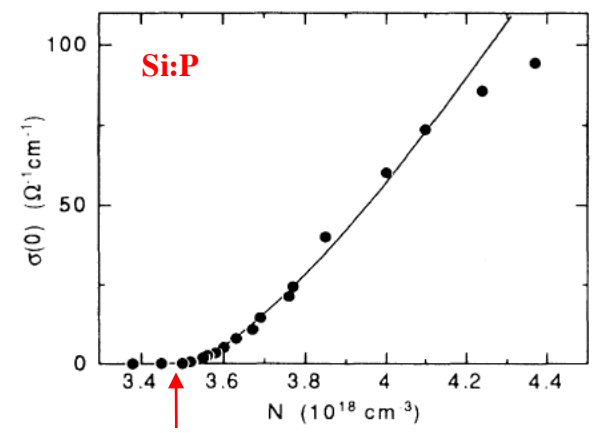
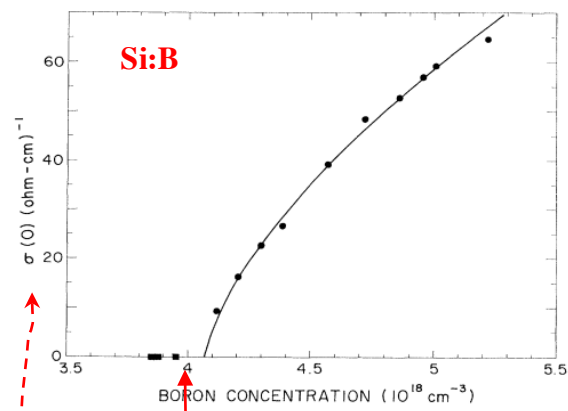
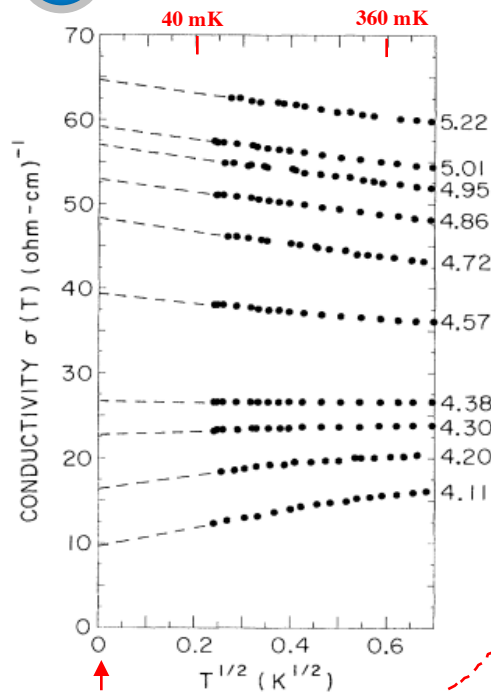
Si:P ( $6 \times 10^{19}/\text{cm}^3$ )



**Impurity band**

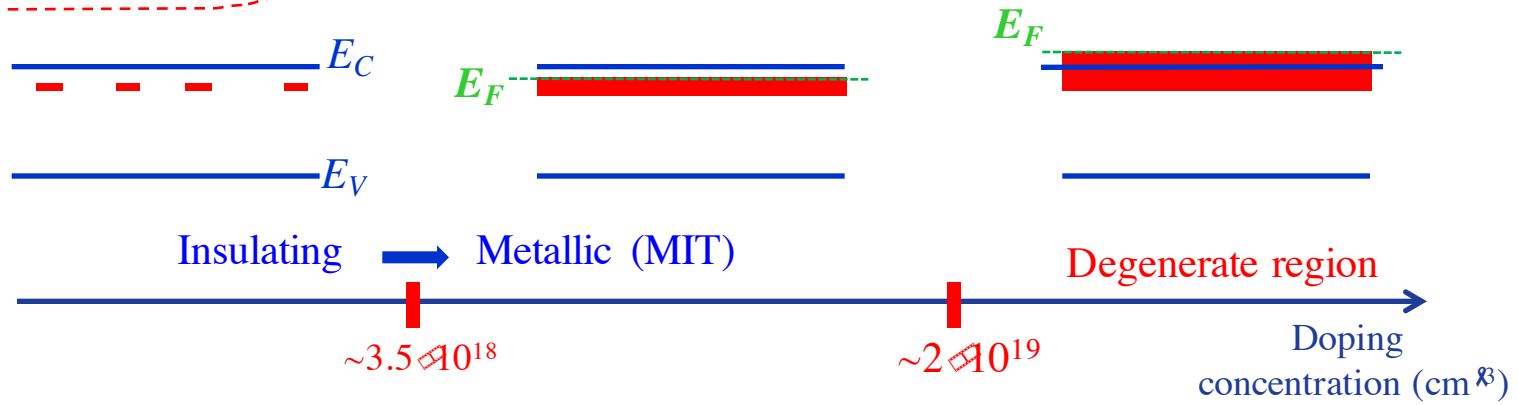
Disorder  
Coulomb correlations

# Metal Insulator Transition (MIT) in Si



**Critical concentration for MIT**

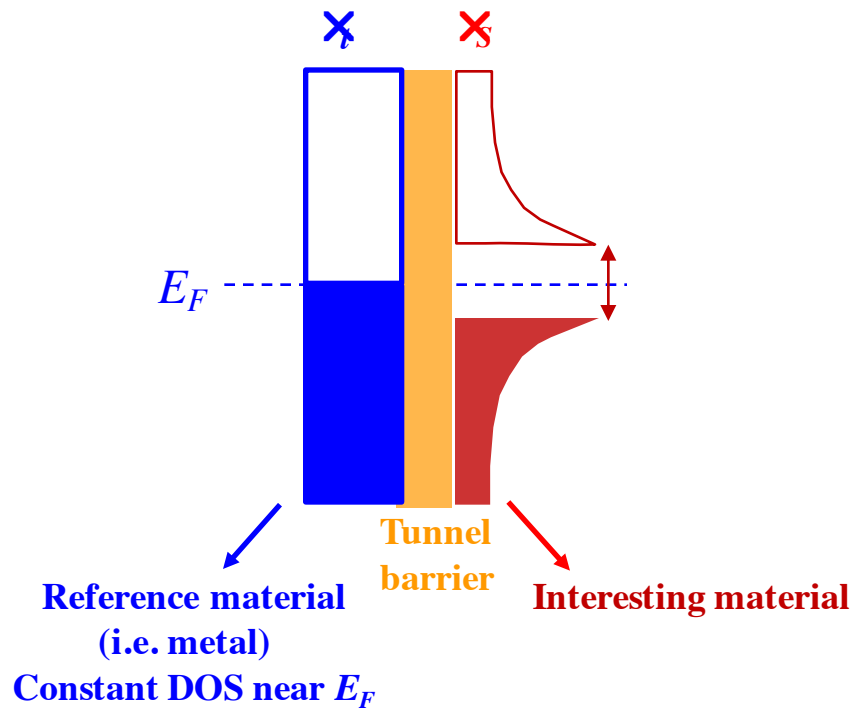
$\sigma(0)$



# Tunneling DOS spectroscopy

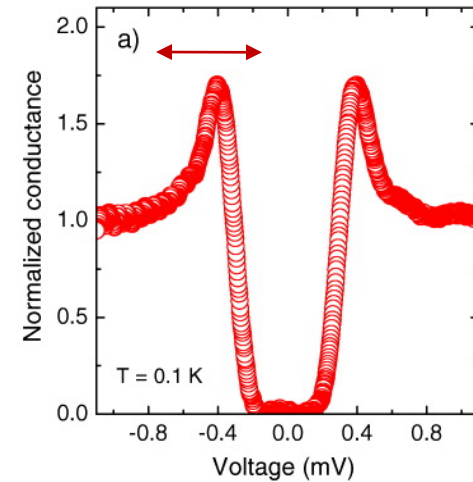
## Tunneling current

$$I \propto \int_0^{eV} \rho_s(E) \rho_t(-eV + E) dE$$



## Tunneling conductance $\propto$ DOS

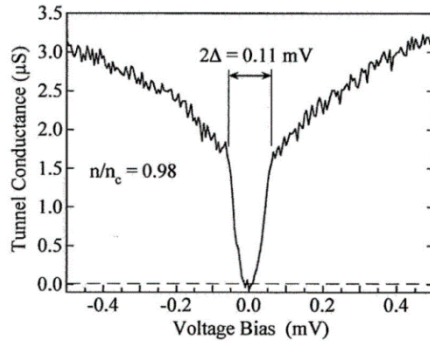
$$\frac{dI}{dV} \propto \rho_s(E_F - eV)$$



# DOS gap in Si:B

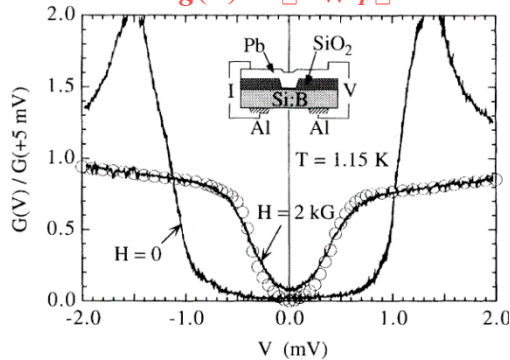
## Gap in the single particle DOS in Si:B (p-type) near the MIT

(*e-e* interaction and disorder)



Efros & Shklovskii: Coulomb gap  
(Soft gap)

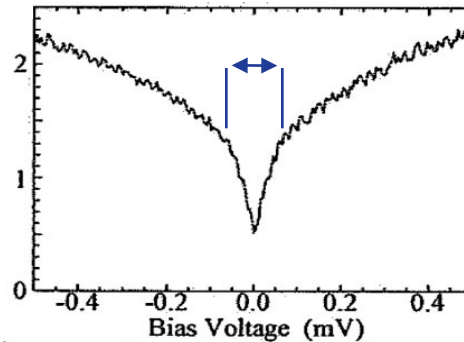
$$g(E) \propto |E - E_F|^{2.5}$$



*Insulating side*

Altshuler, Aronov, McMillan:  
Zero-bias anomaly (ZBA)

$$g(E) \propto g(0) \propto |E|^{0.5}$$



*Metallic side*

$3.4 \times 10^{18}$  for Si:B (MIT)

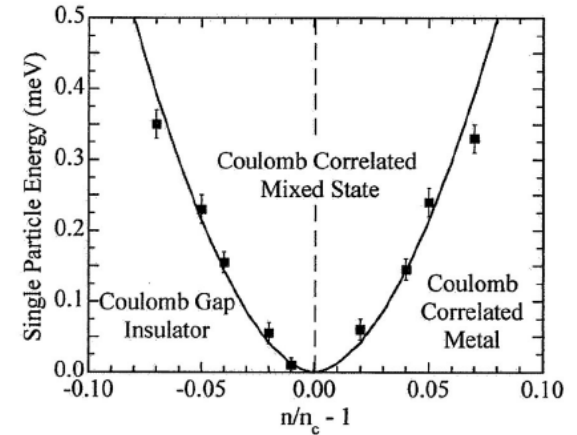


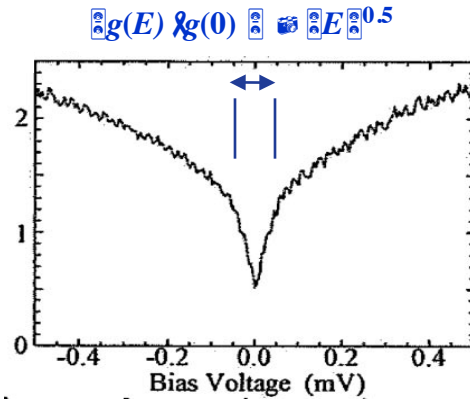
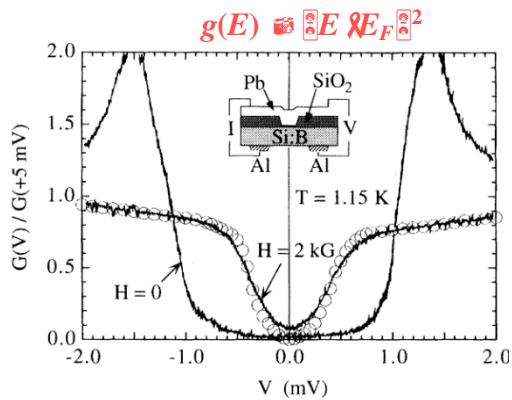
FIG. 4. Zero temperature phase diagram of Coulomb correlations through the MIT in the single-particle energy vs reduced density plane. The data points plotted are  $\Delta$  for insulators and  $\Delta'$  for metals. The blue curve is a guide-to-the-eye representation of the phase boundary  $\epsilon^* (|n/n_c - 1|)$ . As drawn,  $\epsilon^* \sim |n/n_c - 1|^\gamma$  with  $\gamma = 1.7$ , but any value of  $\gamma$  between 1.5 and 2 can yield a reasonable fit.

# Something new in the quasi-degenerate metallic region?

Non-magnetic

Efros & Shklovskii: Coulomb gap  
(Soft gap)

Altshuler, Aronov, McMillan:  
Zero-bias anomaly (ZBA)



*Insulating side*

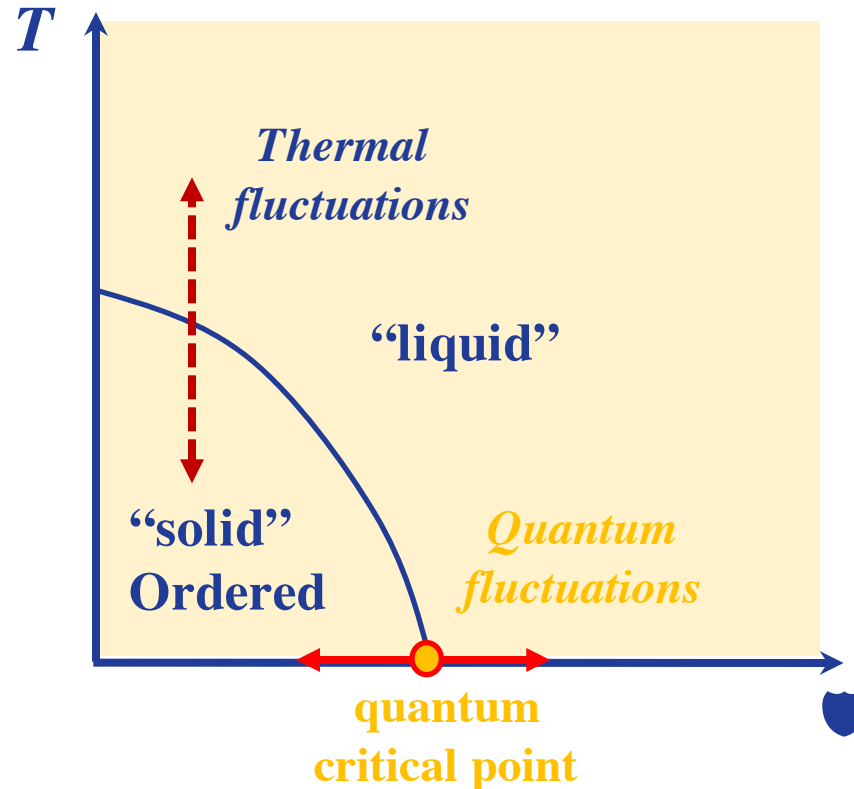
*Metallic side*

**Interesting comment:**

**The single-particle DOS in Si:P (n-type) has not been reported yet.**

# Quantum Phase Transition (QPT)

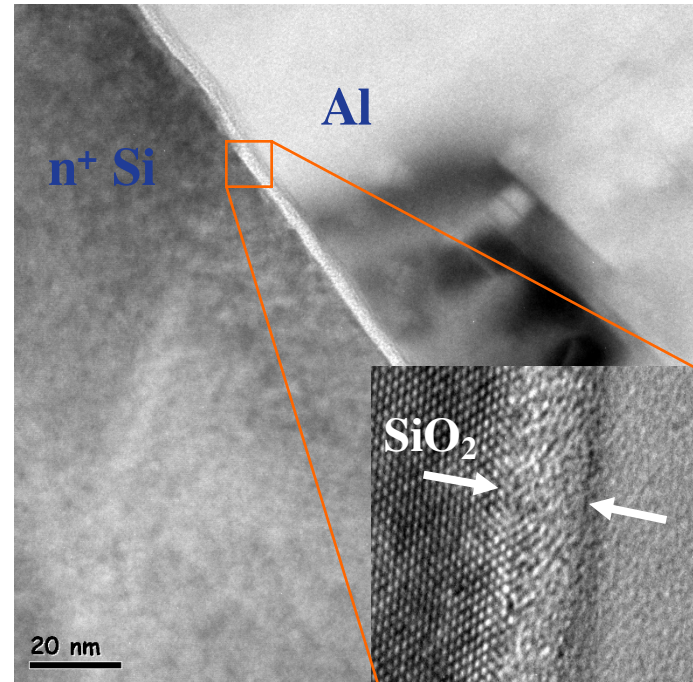
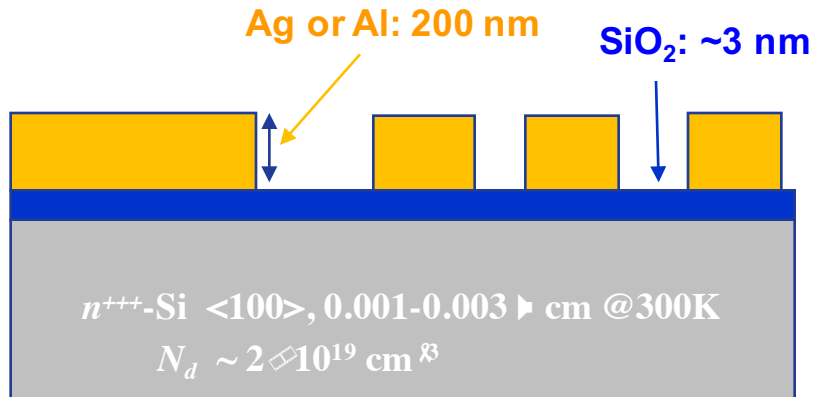
Phase transition between different phases of matter at absolute zero temperature ( $T$ ) by varying a physical parameter ( $\heartsuit B, P$  or composition, etc).



In this work, different phases of Si:P are assessed by measuring the DOS as a function of  $B$  at various temperatures.



# Tunneling devices

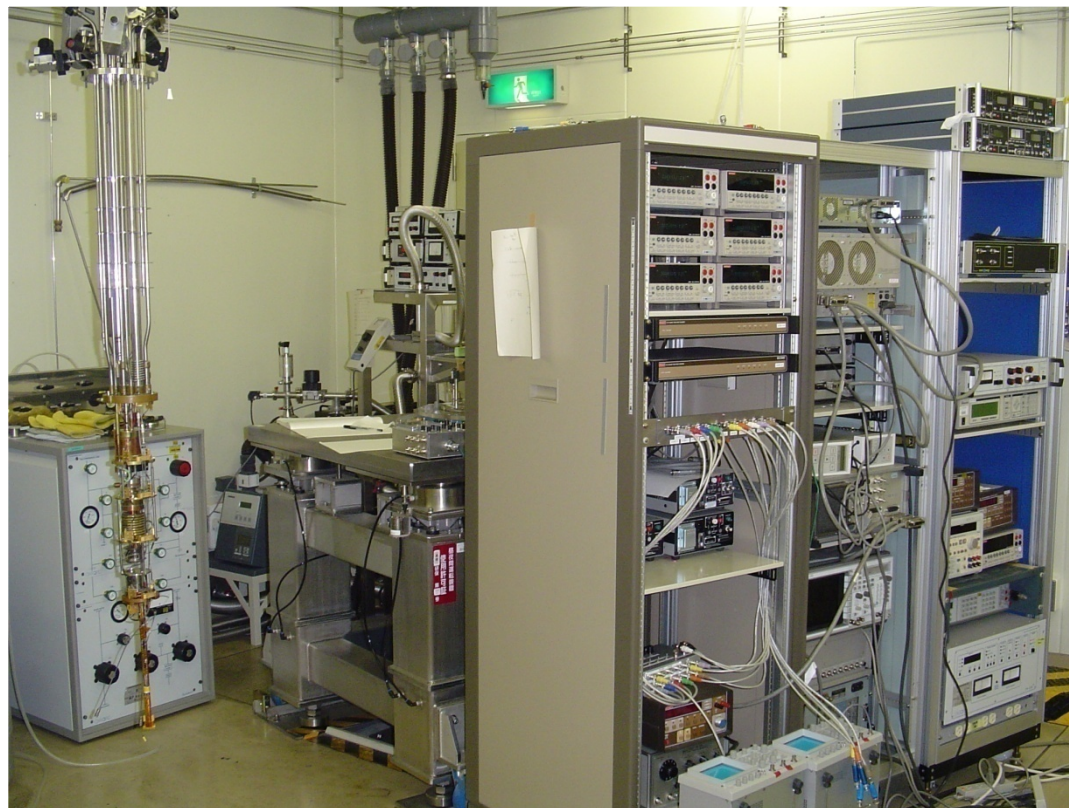
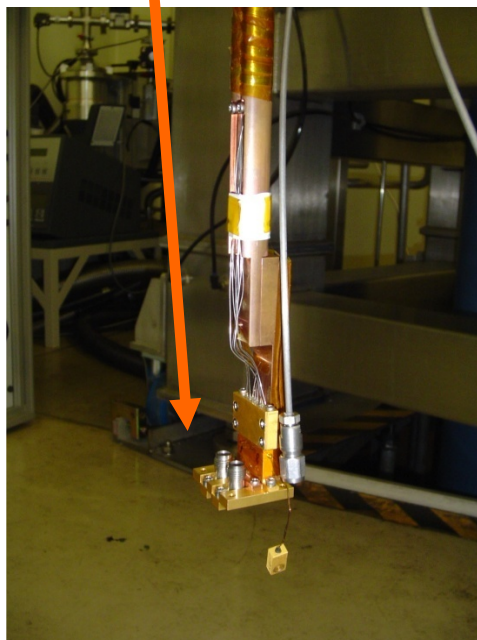
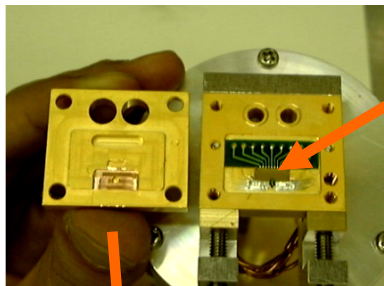


**Oxidation:**

O<sub>2</sub>: 100 Pa, Substrate T: 1000 °C, 17 min

# Transport measurement at dilution temperatures

@ NEC/RIKEN (Japan) & KRISS (Korea)



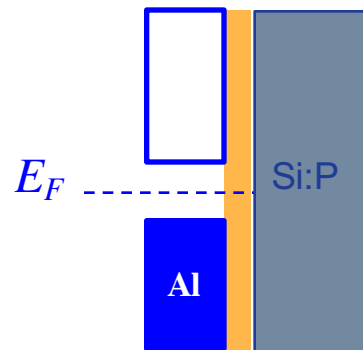
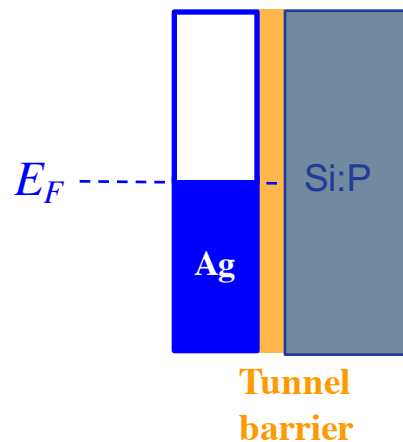


## Tunneling DOS spectroscopy in quasi-degenerate P-doped silicon (Si:P)

Two different samples: Ag-SiO<sub>2</sub>-Si:P & Al-SiO<sub>2</sub>-Si:P

Metal @ 30 mK

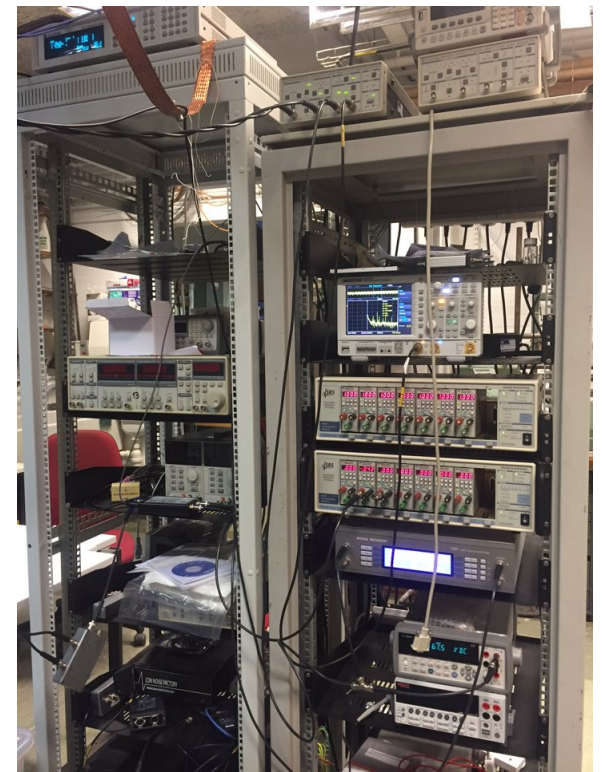
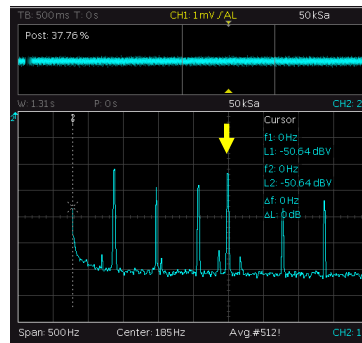
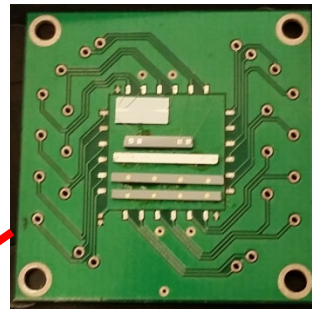
Superconductor below 1.2 K

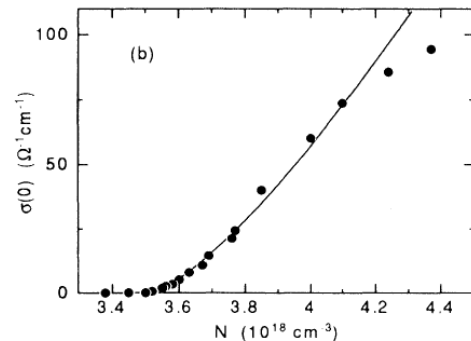
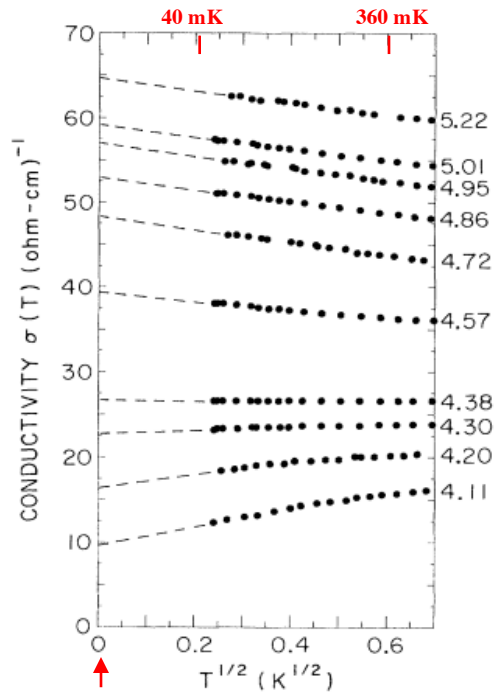


Novel magnetic quantum phases & Magnetic field driven quantum phase transition

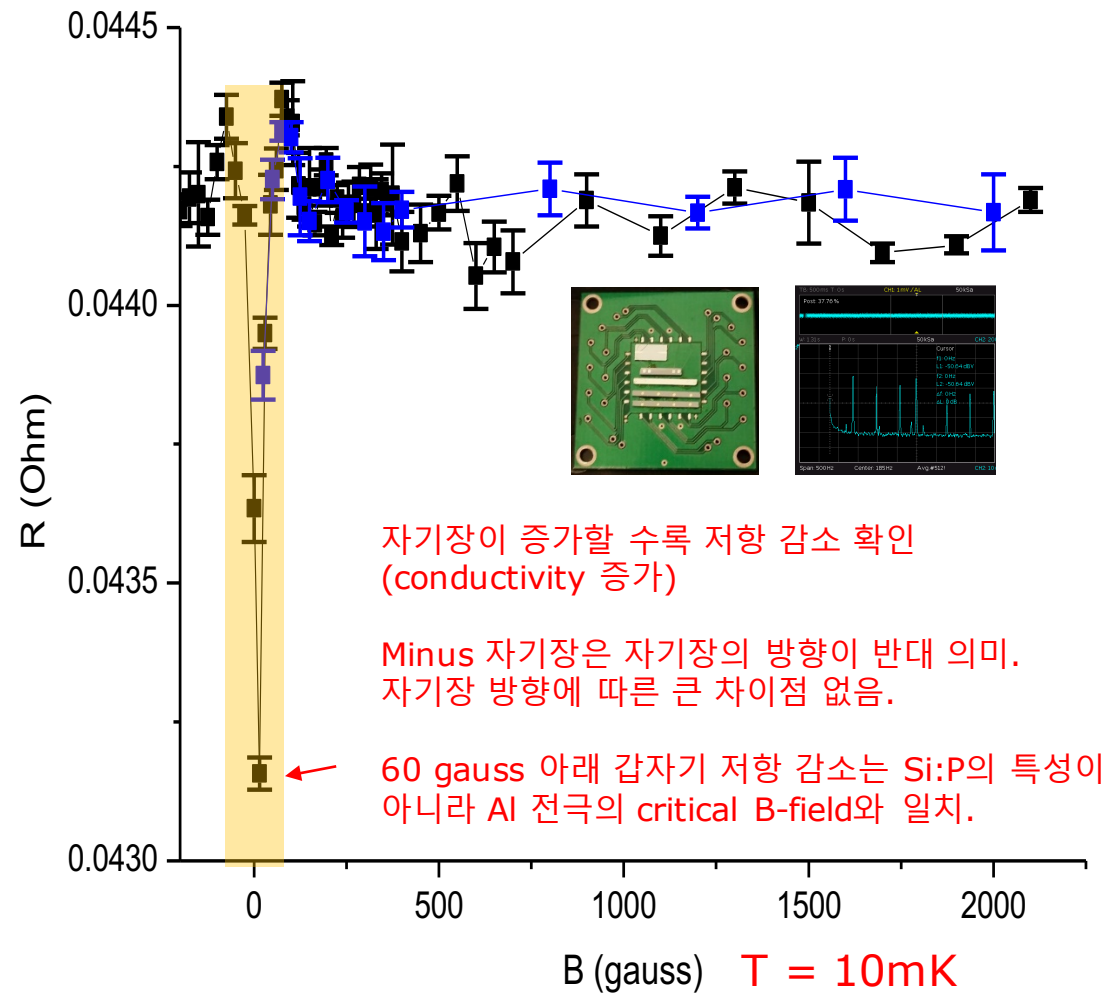


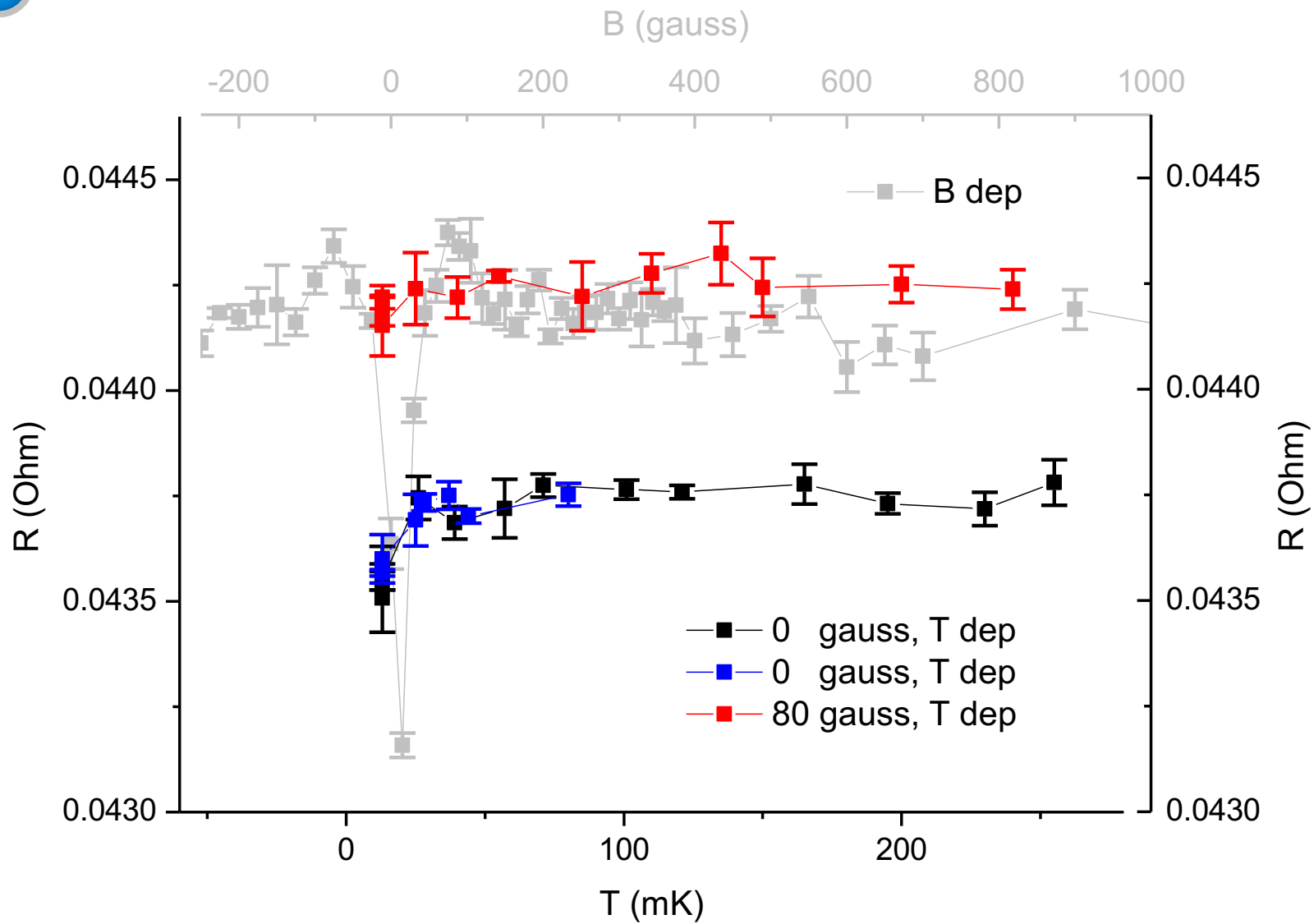
## 4 points conductance measurements @ Quantum technology center at Lancaster Univ.



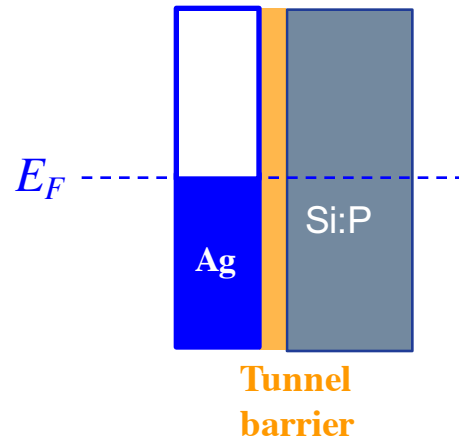


## Bulk conductivity for Si:P ( $> 10^{19}/\text{cm}^3$ )

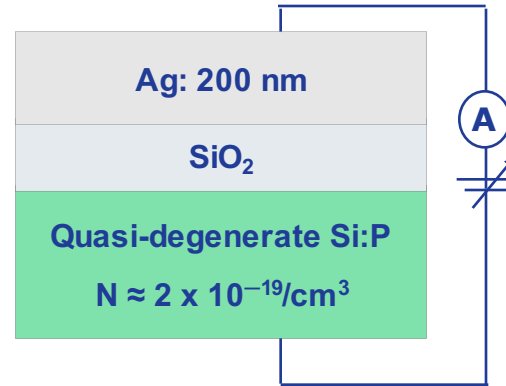
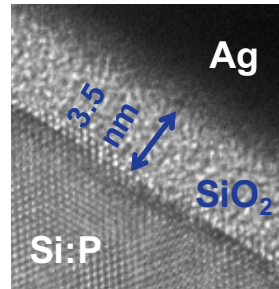




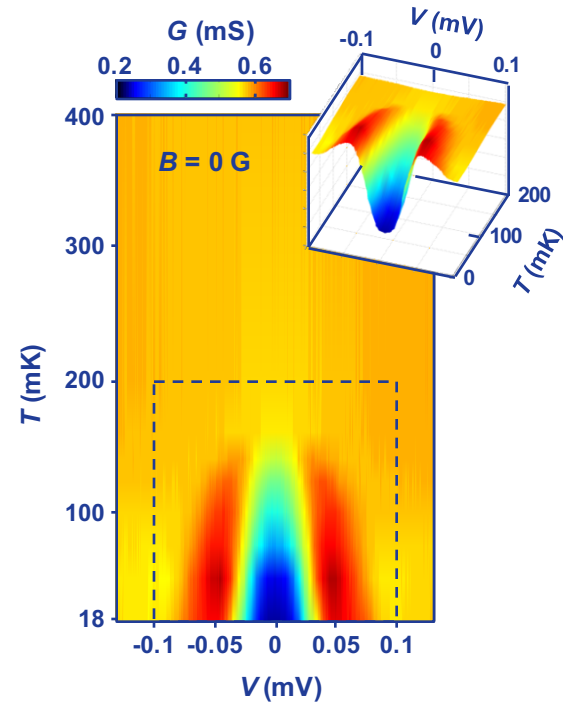
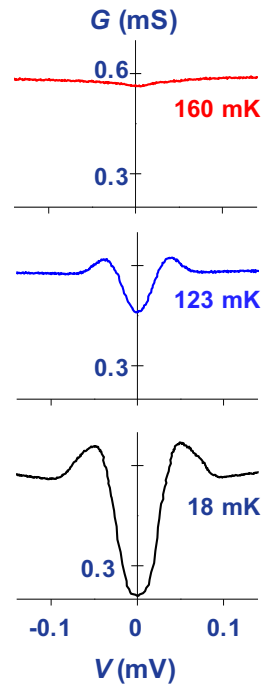
## Tunnelling spectroscopy for Ag-SiO<sub>2</sub>-Si:P



# $T$ -dependent tunneling conductance, $G(T, B=0)$

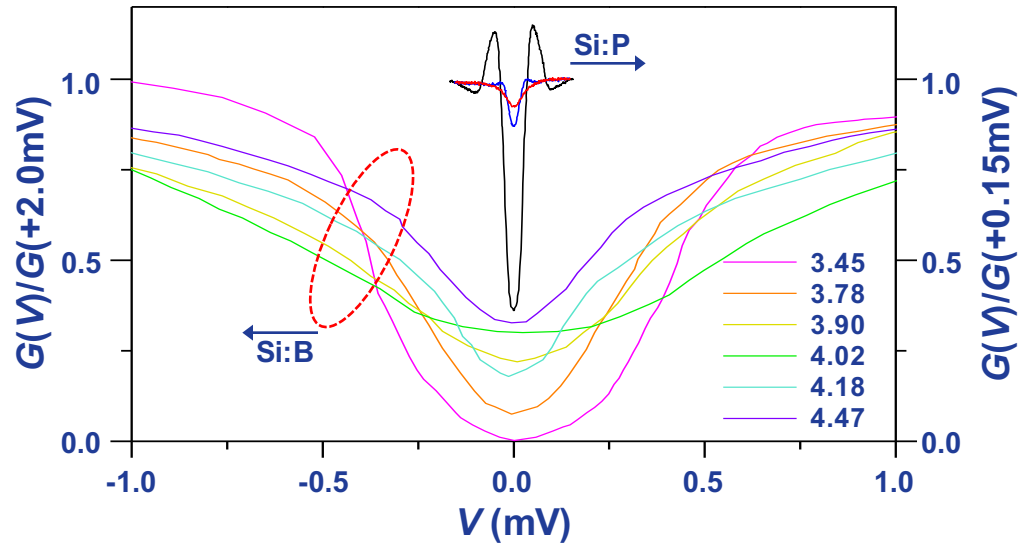


Single-particle  
DOS structure  
in Si:P

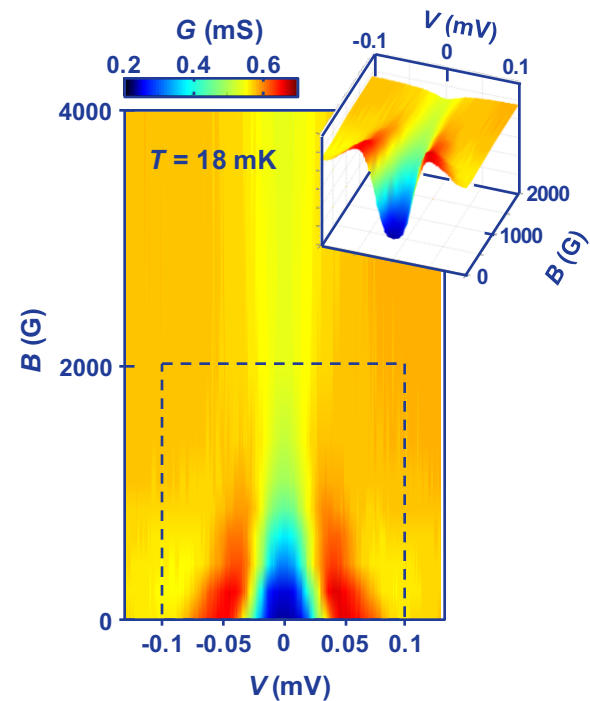
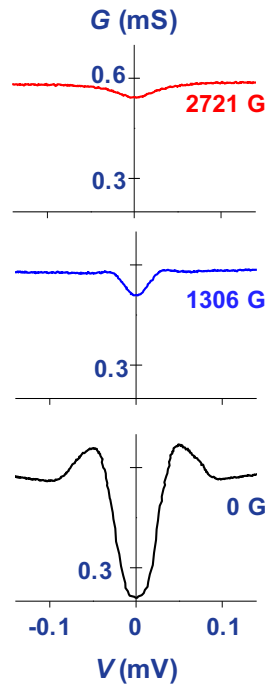
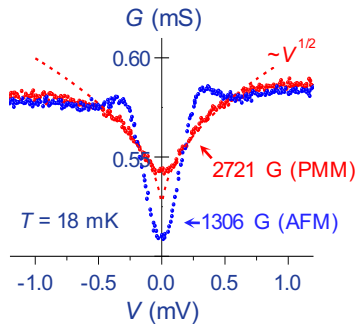
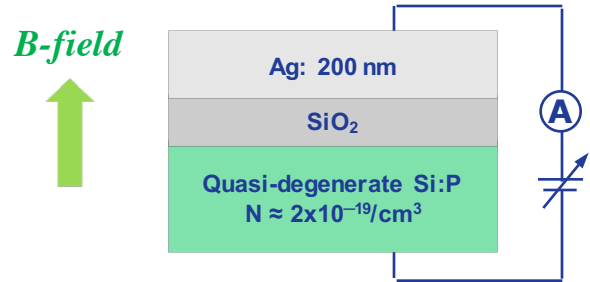




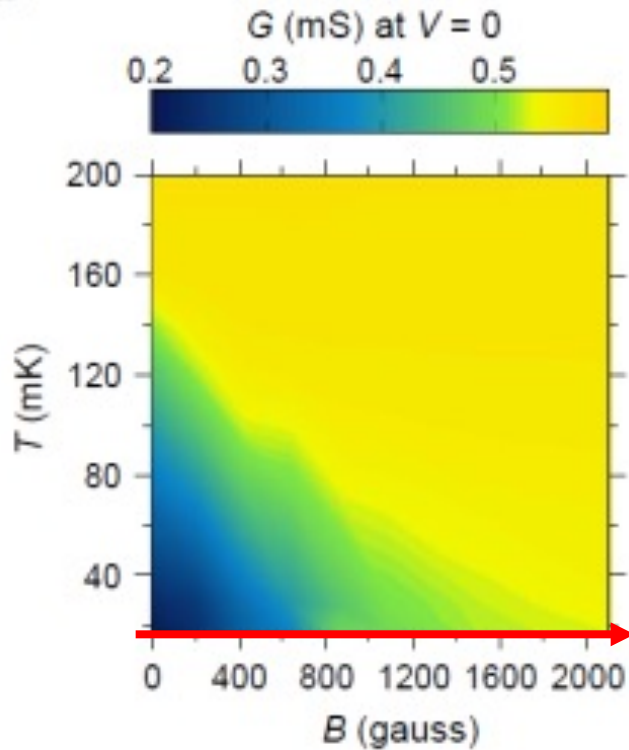
# Comparison: *Coulomb gap near the MIT and our results*



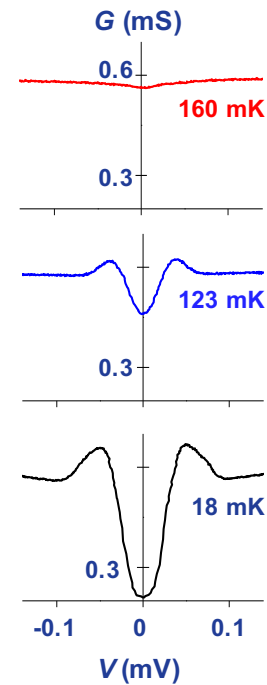
# B-dependent tunneling conductance, $G(T=20\text{mK}, B)$



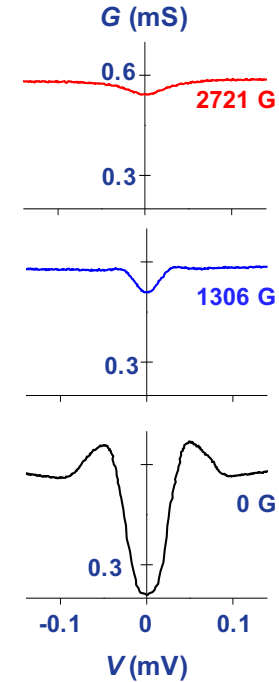
# Quantum phase diagram in Si:P



Intensity plot for the DOS at  $E_F$  in Si:P  
(Quantum phase diagram)



$T$ -dependence @  $B=0$



$B$ -dependence @ 30 mK

# Disordered Hubbard model and Phase diagram



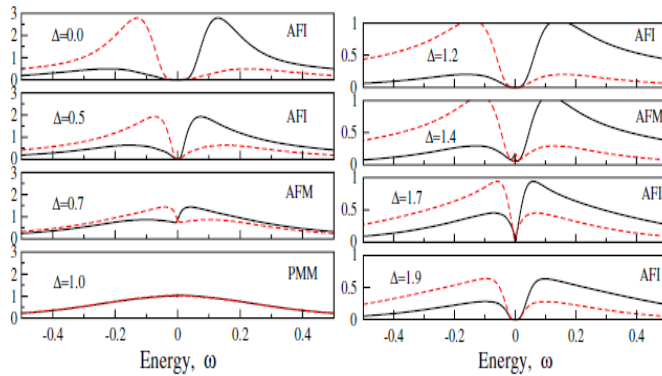
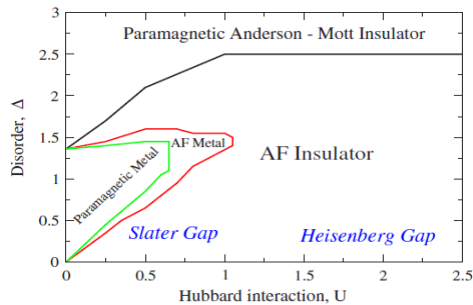
PRL 102, 146403 (2009)

PHYSICAL REVIEW LETTERS

week ending  
10 APRIL 2009

## Competition between Anderson Localization and Antiferromagnetism in Correlated Lattice Fermion Systems with Disorder

Krzysztof Rucznik<sup>1,2</sup>, Walter Hofstadter<sup>3</sup> and Dieter Vollhardt<sup>1</sup>

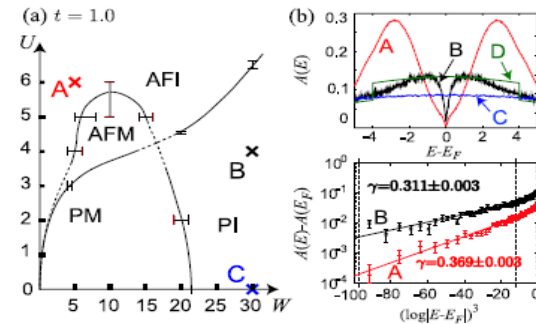


PRL 102, 016404 (2009)

PHYSICAL REVIEW LETTERS

week ending  
9 JANUARY 2009

## Soft Hubbard Gaps in Disordered Itinerant Models with Short-Range Interaction



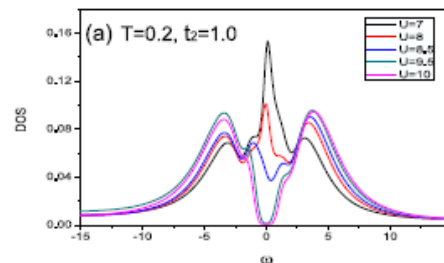
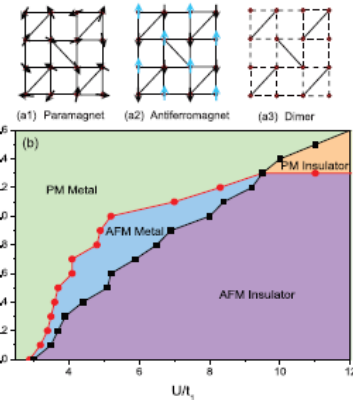
SCIENTIFIC  
REPORTS

OPEN

## Antiferromagnetic Metal and Mott Transition on Shastry-Sutherland Lattice

SUBJECT AREAS:  
PHASE TRANSITIONS  
AND CRITICAL  
SUBSYSTEMS

Hai-Di Lü, Yao-Hua Chen, Heng-Fu Lin, Hong-Shuai Tao & Wu-Ming Liu



# Hubbard model including spin-spin (RKKY) interaction

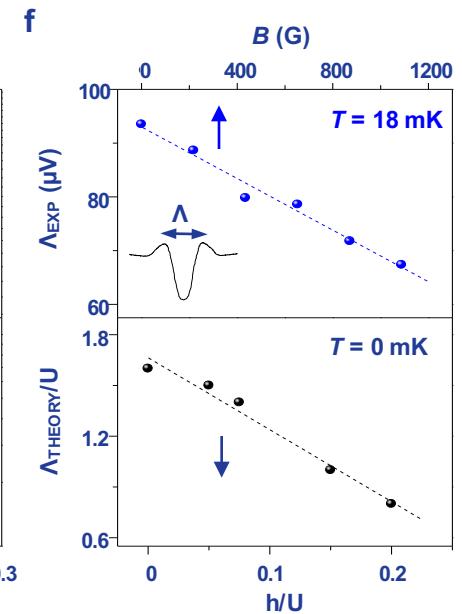
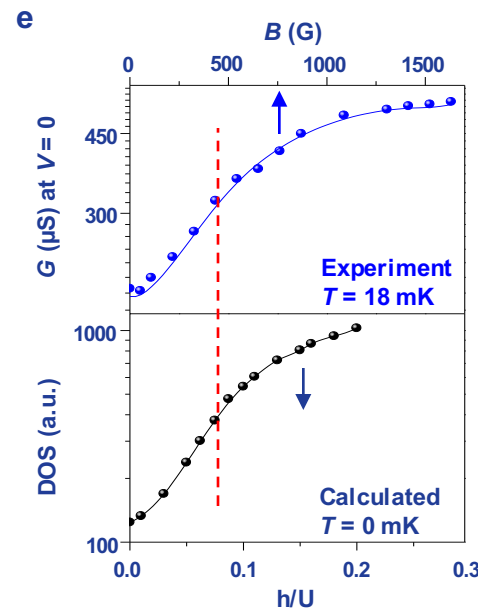
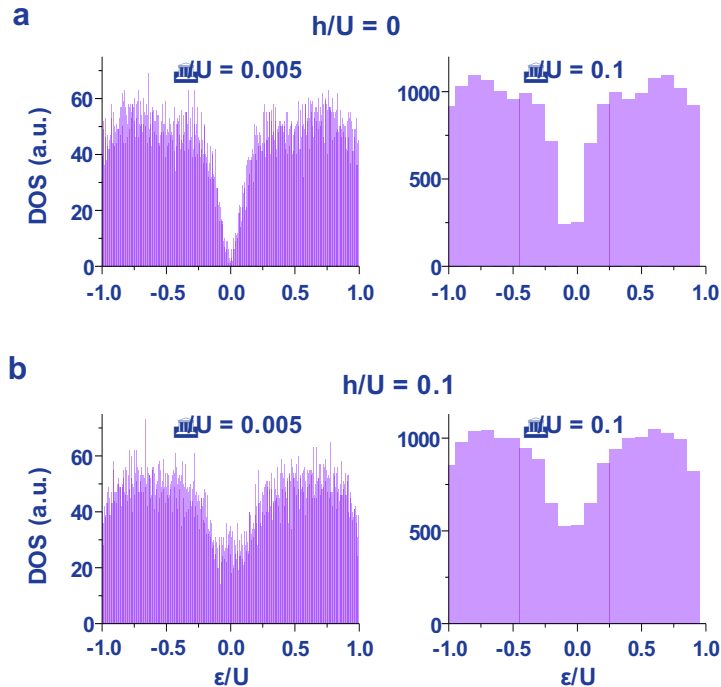
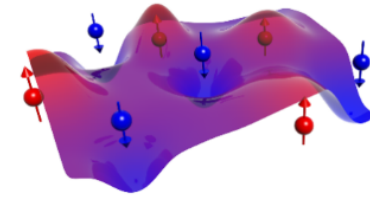


(Eric Yang & GS Jeon)

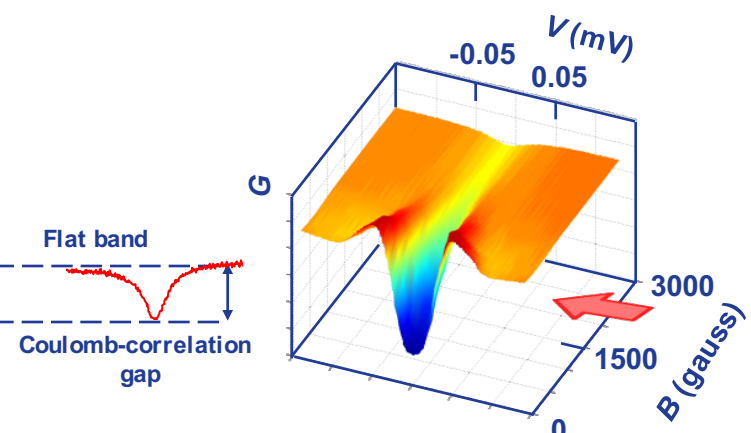
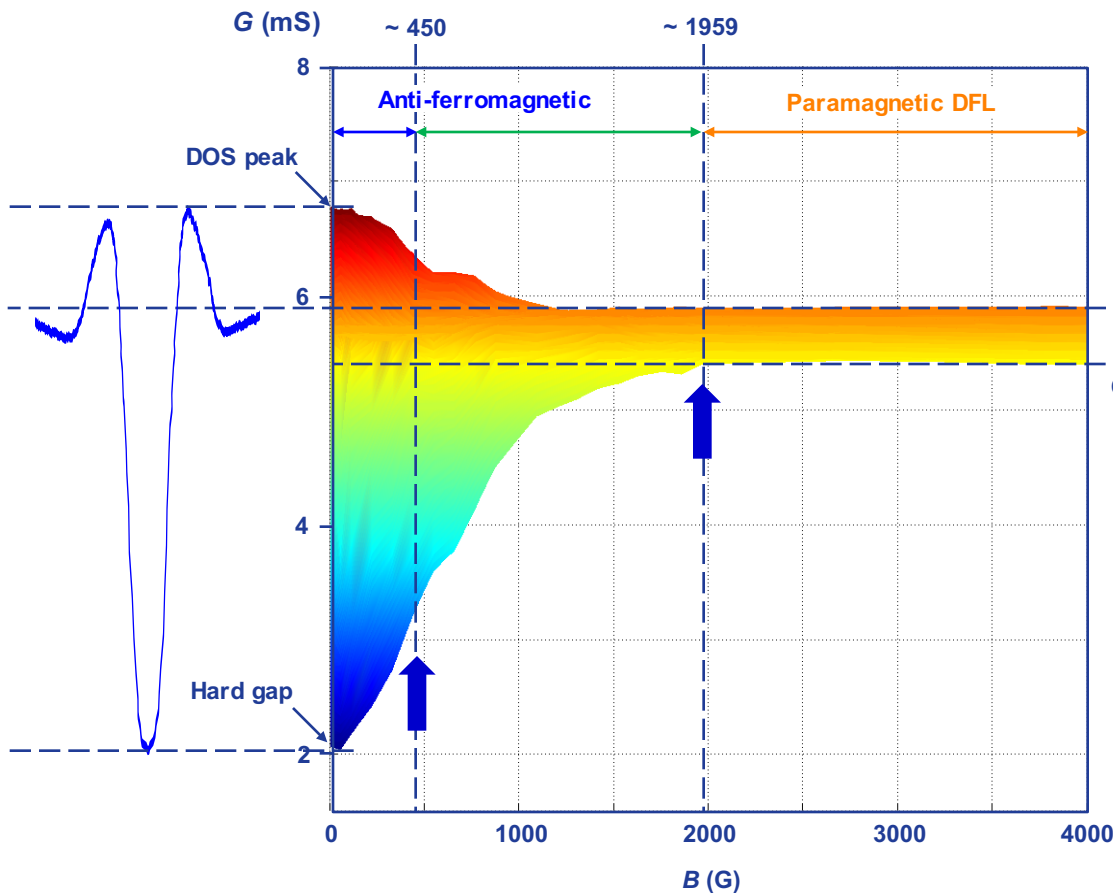
$$H = -t \sum_{\langle i,j \rangle, \sigma} c_{i\sigma}^\dagger c_{j\sigma} + \sum_{i,\sigma} (\epsilon_{i\sigma}^0 - \mu) c_{i\sigma}^\dagger c_{i\sigma} - \hbar \cdot \sum_i \mathbf{u}_i - \sum_{i>j} J_{ij} \mathbf{u}_i \cdot \mathbf{u}_j$$

External B-field

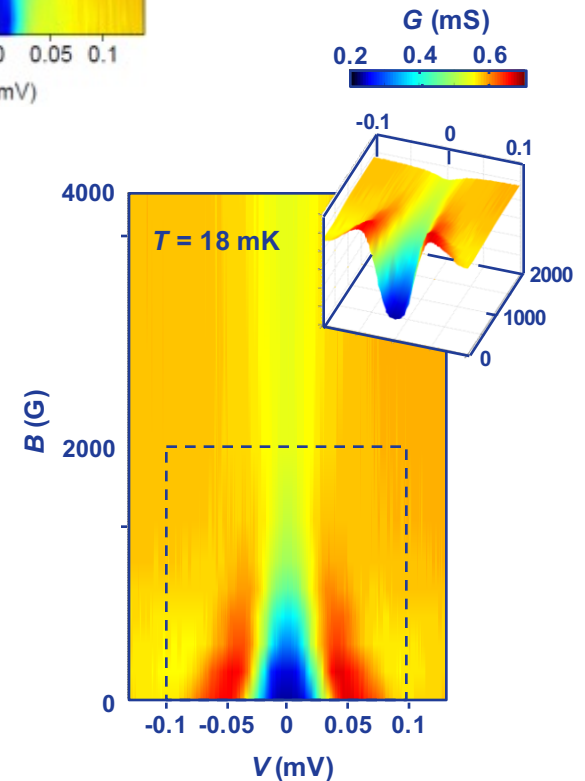
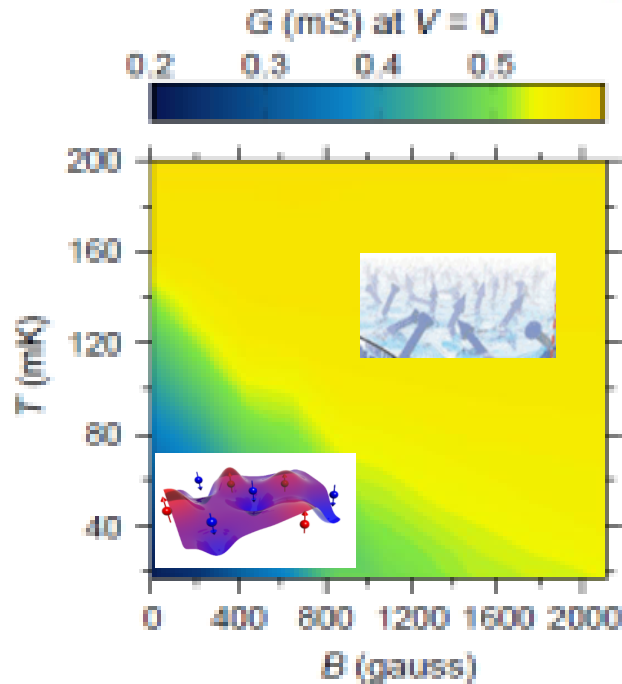
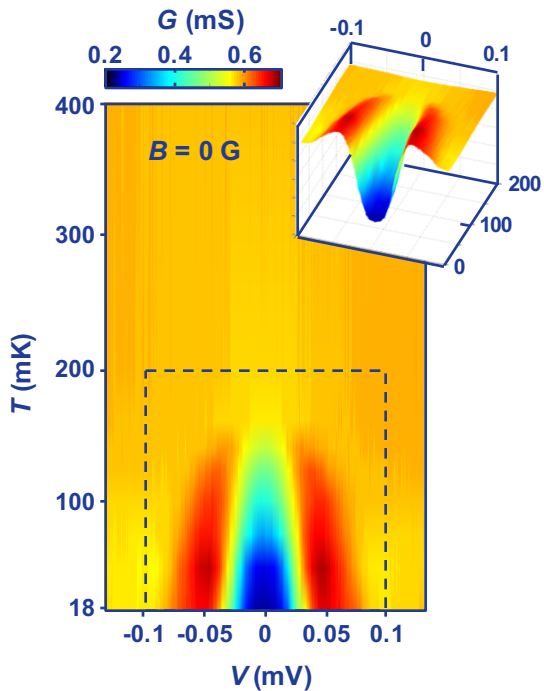
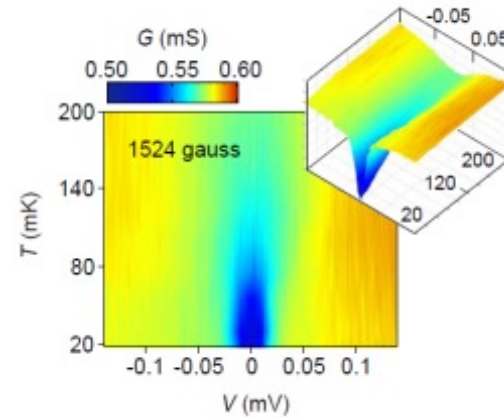
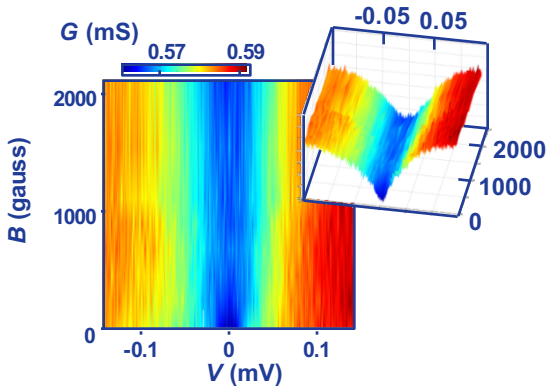
Long-range  
anti-ferromagnetic coupling  
(RKKY spin-spin interaction)



# Determining Phase boundary (magnetic & non-magnetic)



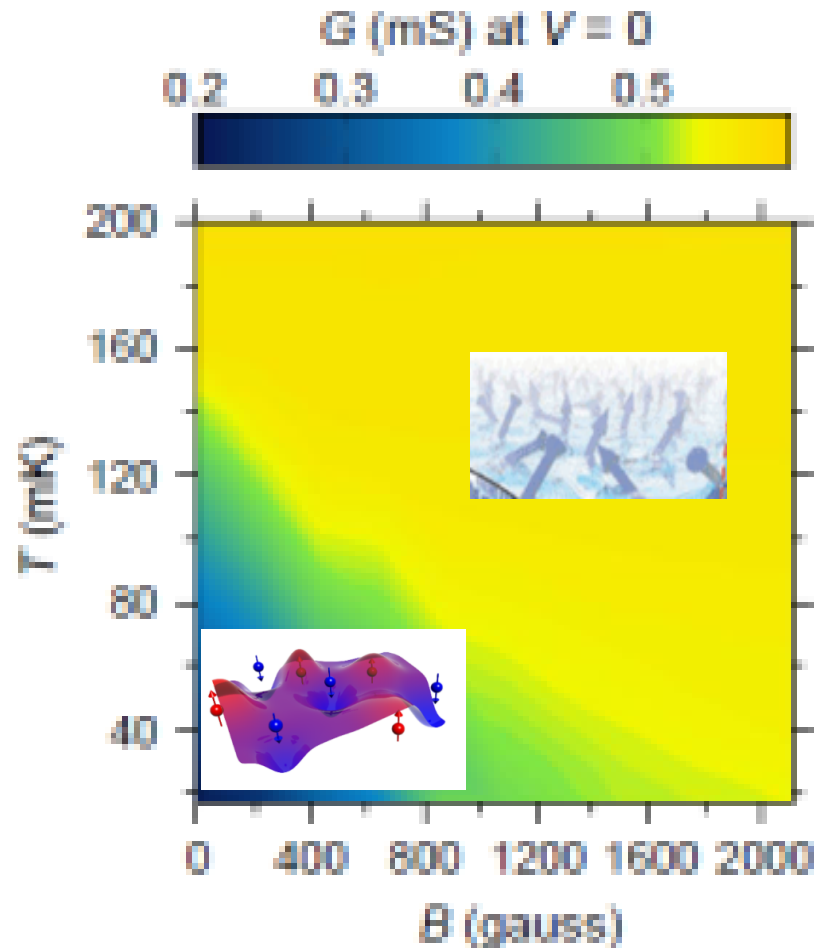
# Quantum Phase diagram



Quantum Phase Transition

# Origin of insulating phase in Si:P

Interplay between disorder, on-site repulsion, spin-spin interaction

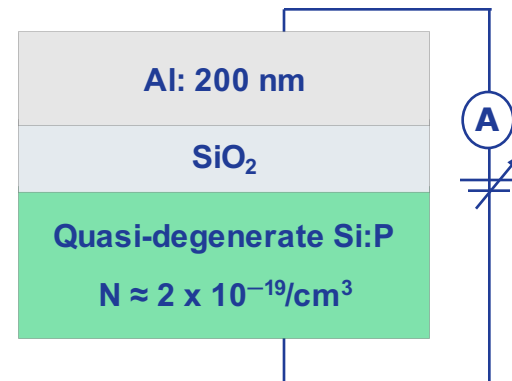
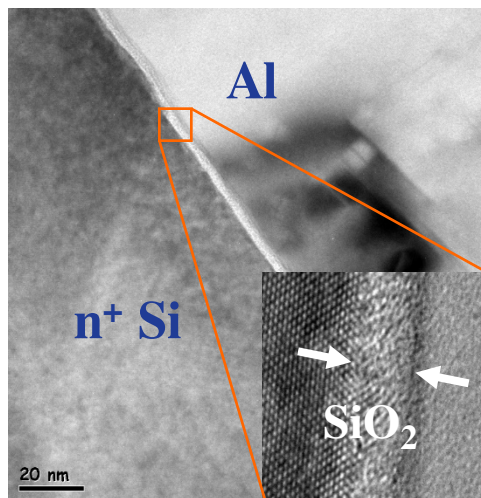
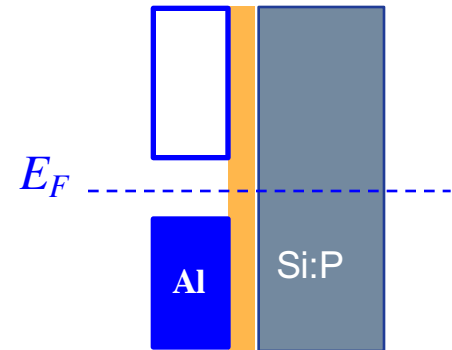




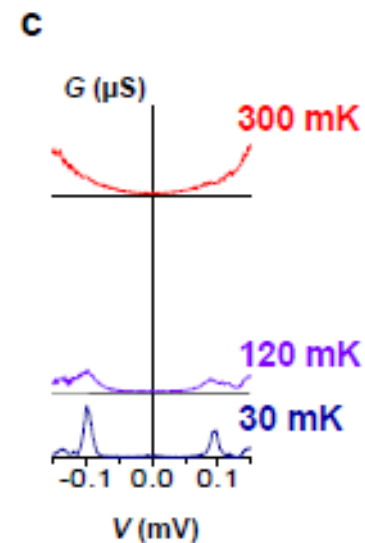
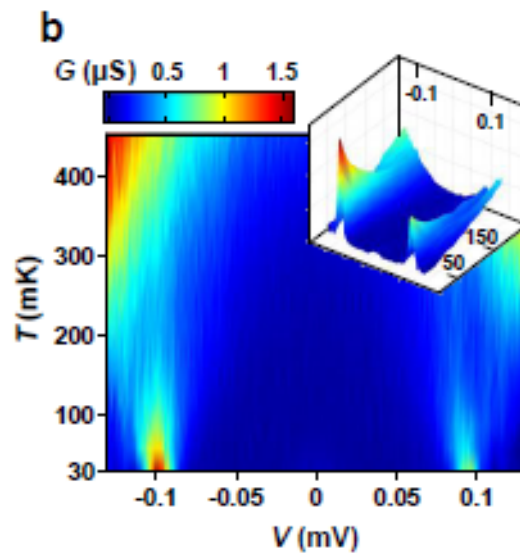
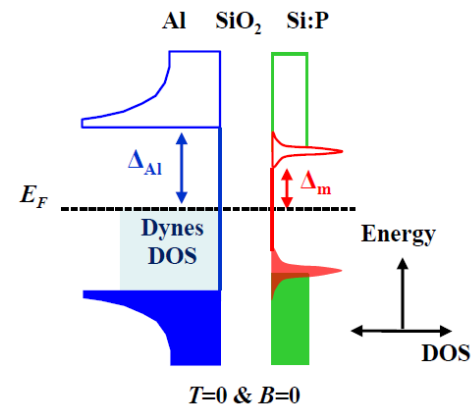
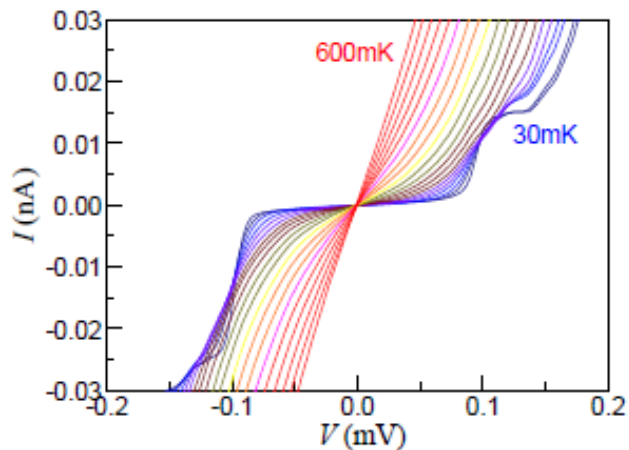
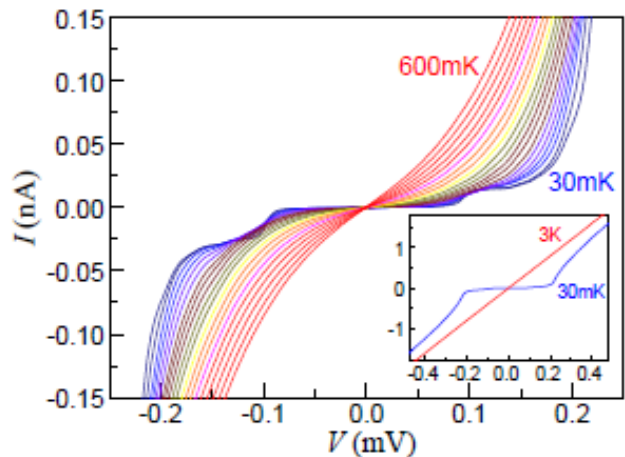


## Tunnelling spectroscopy for Al-SiO<sub>2</sub>-Si:P

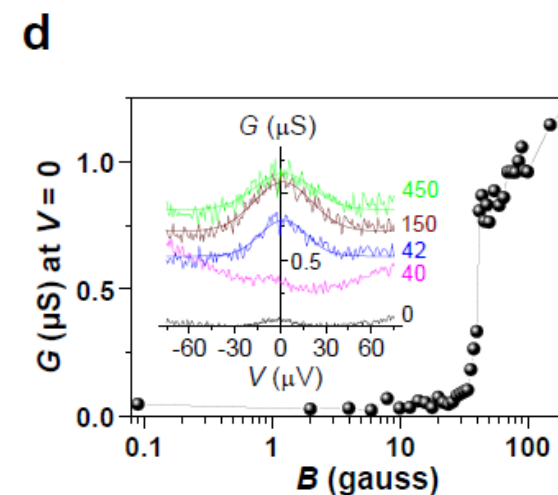
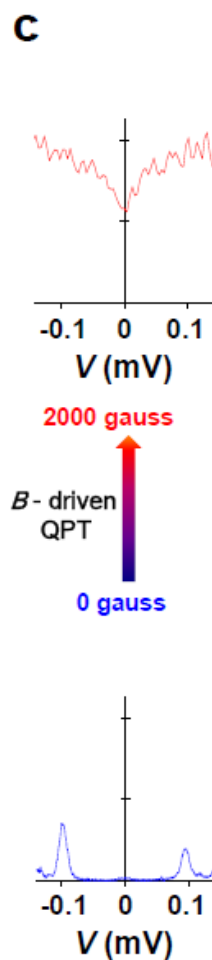
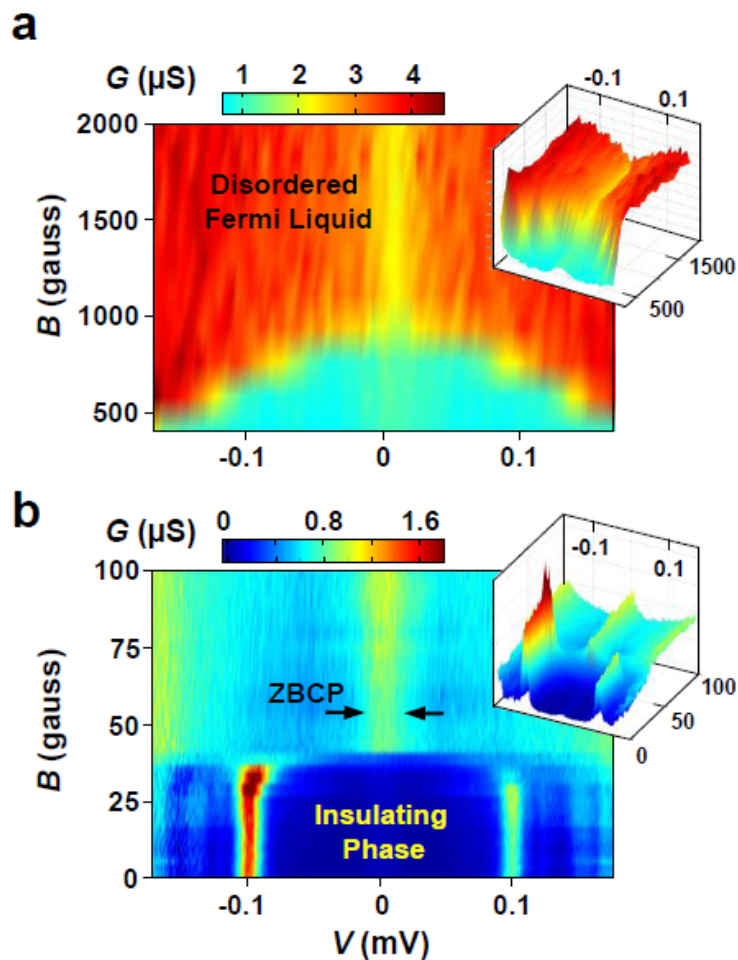
*Note that Al is a superconducting electrode.*



# $T$ -dependent tunneling conductance, $G(T, B=0)$

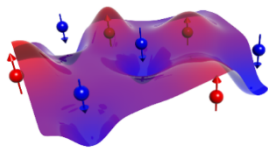
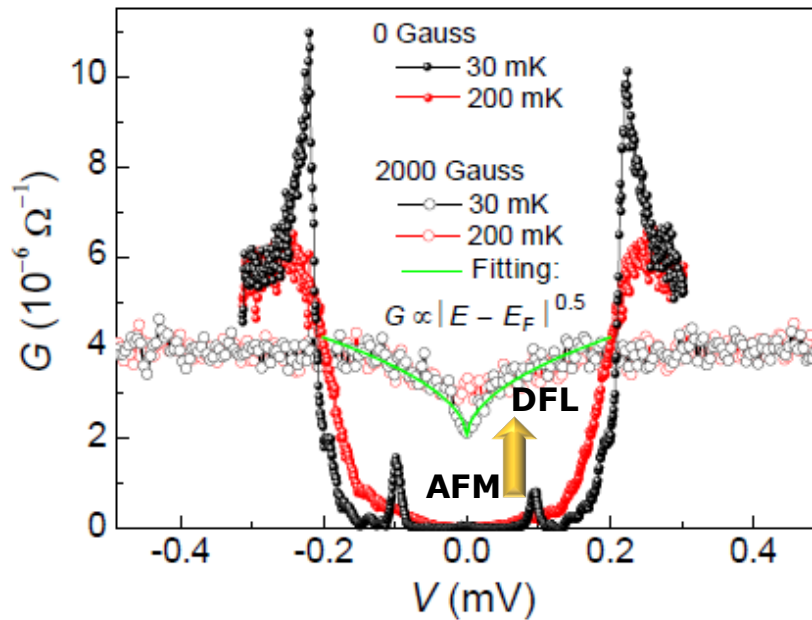


# $B$ -dependent tunneling conductance, $G(T = 30\text{mK}, B)$

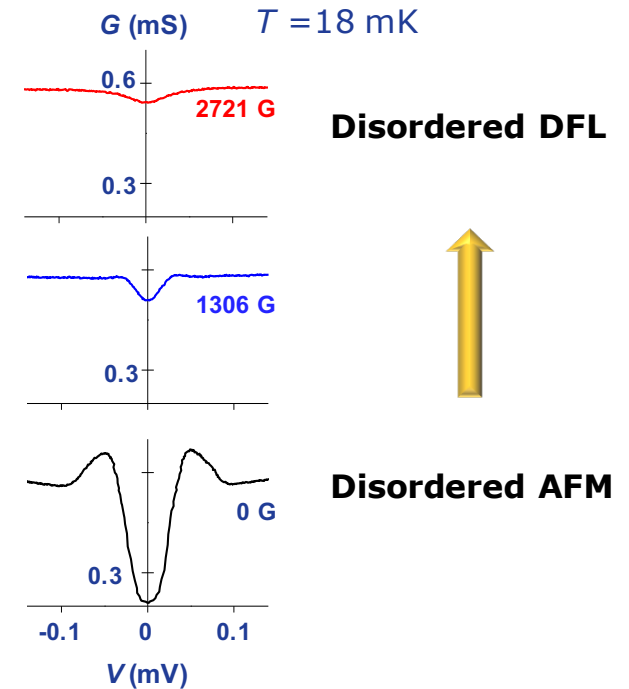


# B-driven quantum phase transition

**Al-SiO<sub>2</sub>-Si:P**



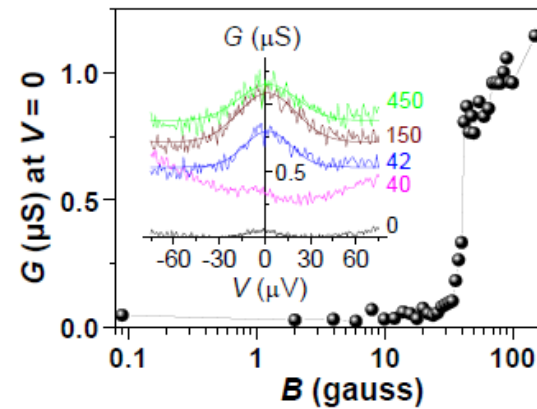
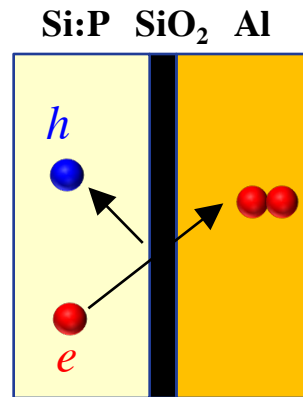
**Ag-SiO<sub>2</sub>-Si:P**



**Disordered Antiferromagnetic Insulator (AFM)  $\rightarrow$  Disordered Fermi Liquid (DFL)**

# Role of superconductor electrode Al in QPT ?

⦿ Andreev reflection causes hole injection into Si:P.



Open question :

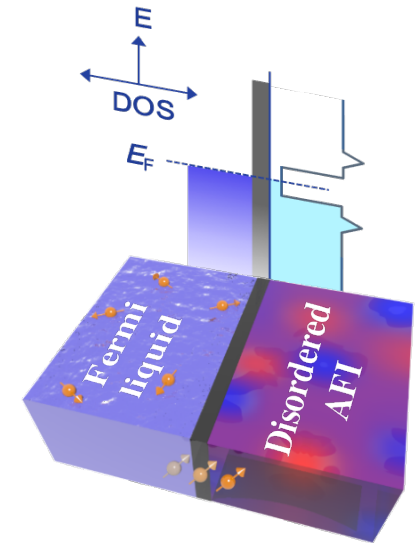
What happens if holes are present in Si:P ?

# Summary

- ▶ We have used **tunneling DOS spectroscopy** to study the nature of various disordered electronic systems in quasi-degenerate metallic Si.
- ▶ Our data are consistent with the  **$B$ -driven Quantum phase transitions** from the disordered AFM to the paramagnetic DFL phases (for the Ag-SiO<sub>2</sub>-Si:P sample).

For the Al-SiO<sub>2</sub>-Si:P sample, the observed QPT is under analysis.

- ▶ The various physical properties of these new phases result from the delicate **interplay between disorder, on-site repulsion, weak magnetic field, and spin-spin (RKKY) interaction.**



## *Challenging issues*

- ▶ *Thermodynamic DOS versus Single particle tunneling DOS*
- ▶ *Direct detection of Spin Density Wave (Neutron scattering)*
- ▶ *Scalability*

# Collaborators

**Eric Yang (Physics in Korea University, Theory)**

**HS Kim (Physics in Dongguk University)**

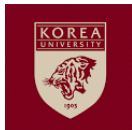
**EK Kim, DU Lee (Physics in Hanyang University, Fabrication)**

**YU Chung (KRISS in Korea)**

**GS Jeon (Physics in Ewha Woman's Univ, Theory)**

**Yuri Pashkin (Physics in Lancaster Univ. & Lebedev Physical Inst. Moscow)**

**Shen Tsai (RIKEN in Japan)**





Thank you for your attention

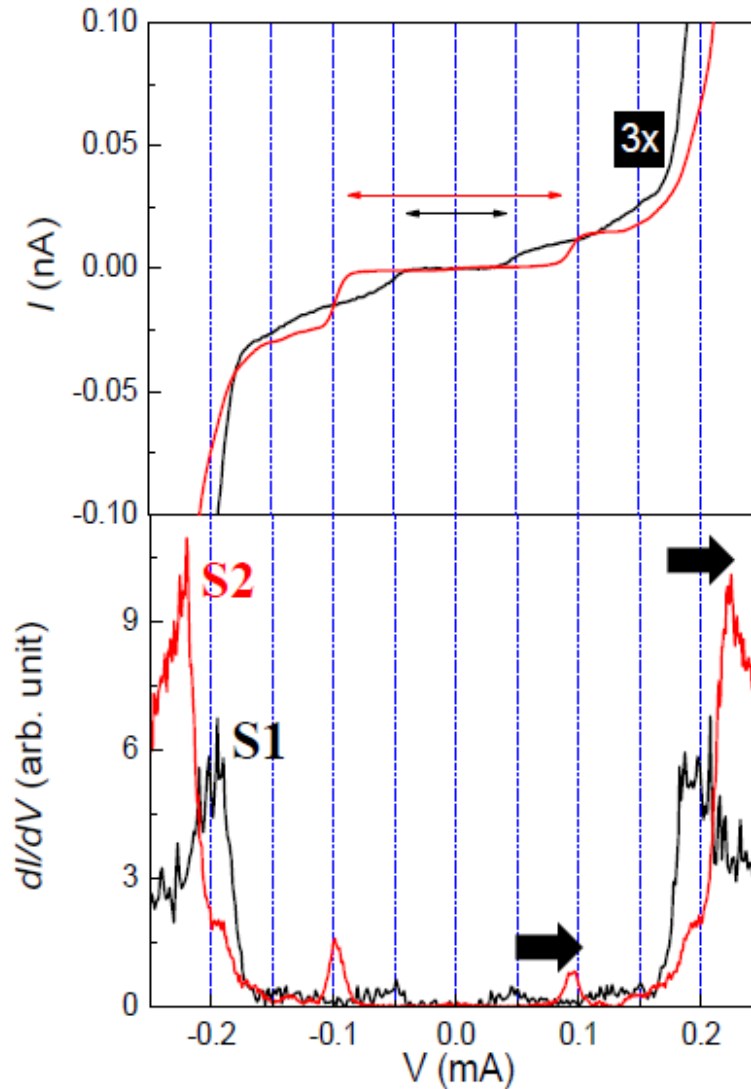


# Long-range and short-range $e-e$ interactions in Si:P

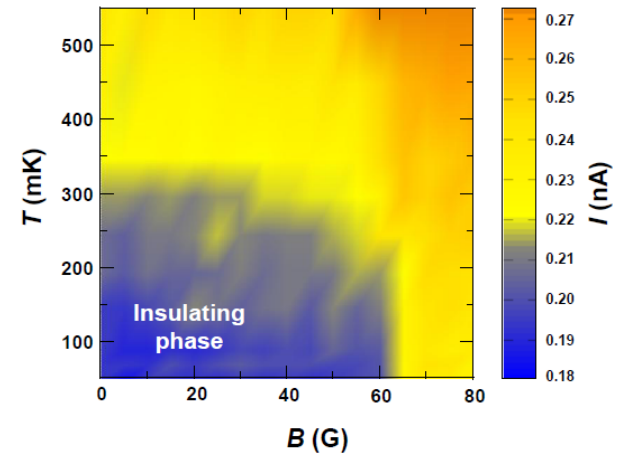
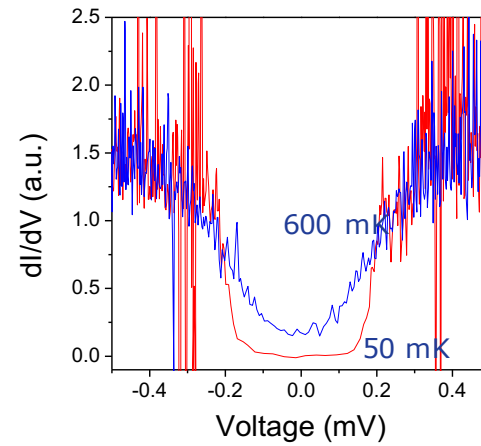
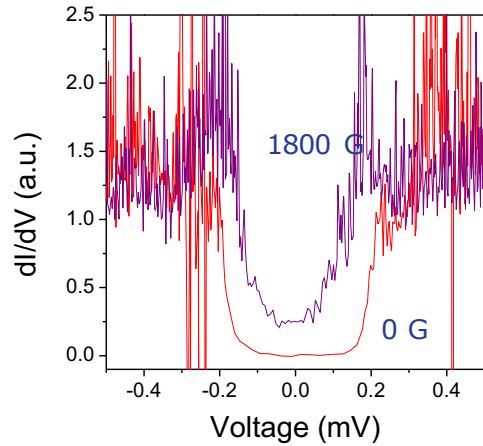
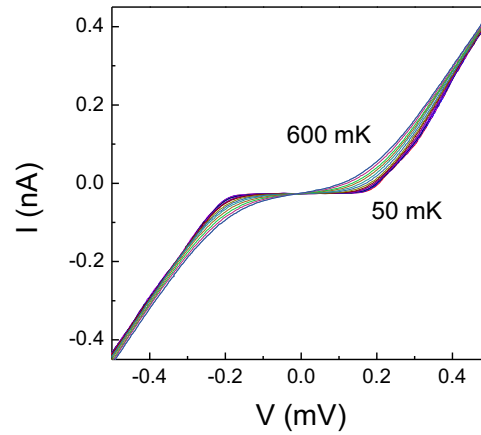
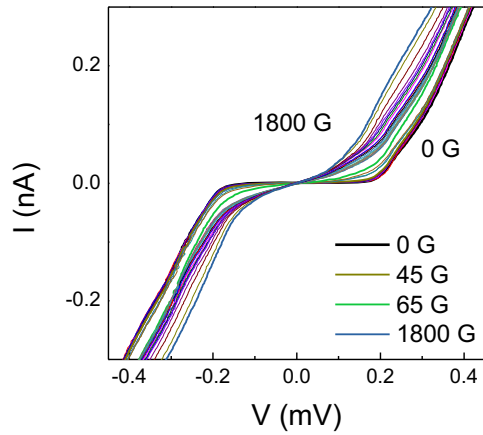


long-range	loss of screening due to diffusive electron motion arising from disorder
	<b>metal:</b> Altshuler-Aronov anomalies in DOS and $\sigma(T)$
	<b>insulator:</b> soft Coulomb gap, Efros-Shklovskii VRH
	Anti-ferromagnetic spin-spin interaction (RKKY interaction): Our case
short-range	on-site Hubbard $U$
	<b>metal:</b> formation of magnetic moments, Kondo effect
	<b>insulator:</b> Hubbard splitting of $1s(A_1)$ impurity band

# Superconductor gap voltage ( $\frac{\hbar\Delta}{e}$ ) shifts due to the DOS gap in Si:P



# Another Al device 1



# Another Al device 2

