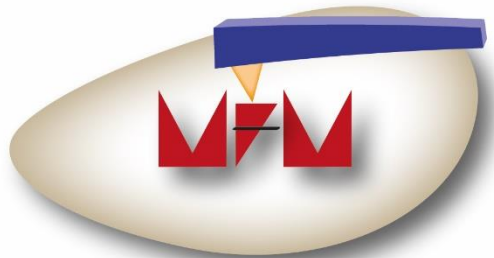
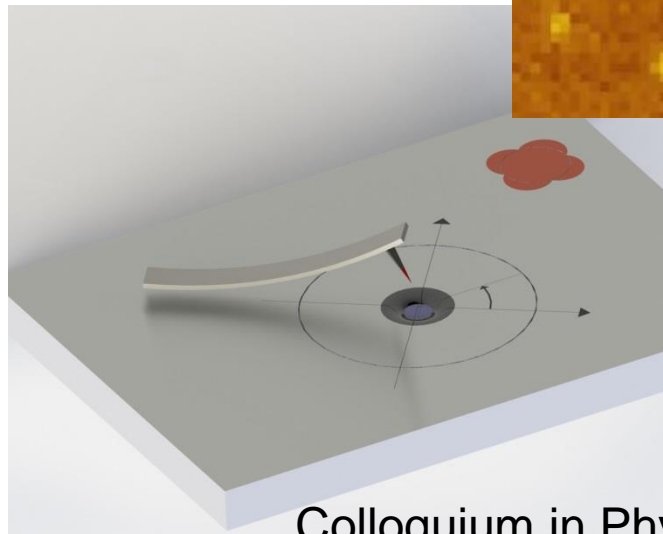
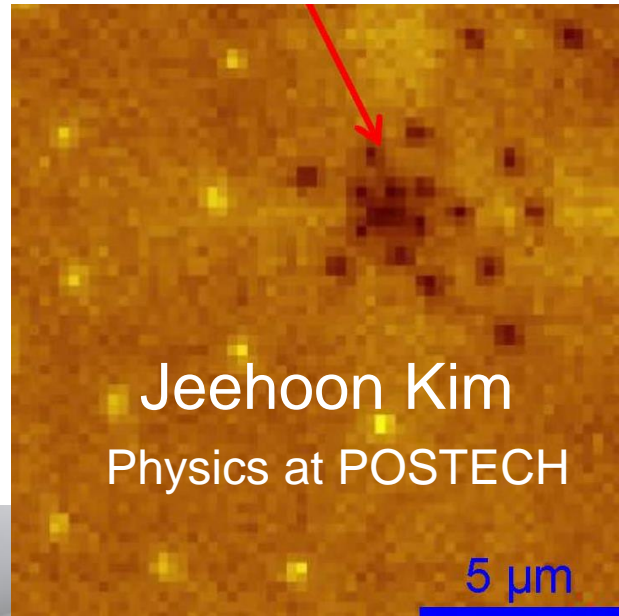


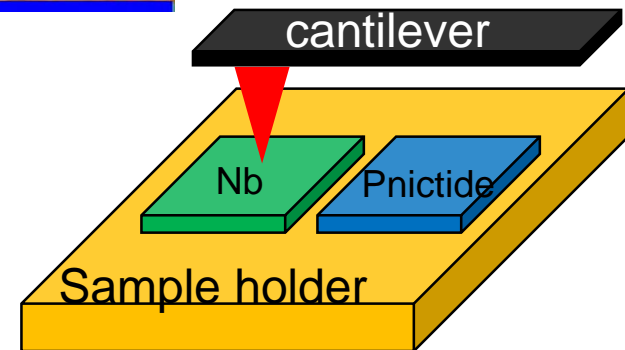
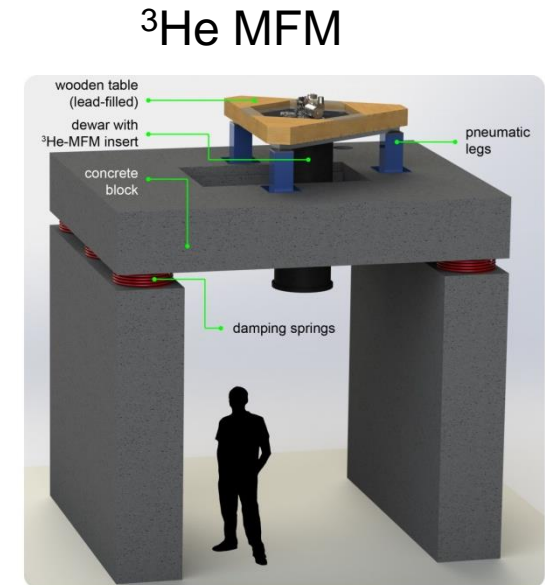
# Investigation of superconductivity by MFM



MAGNETIC FORCE MICROSCOPY LAB



Colloquium in Physics  
Korea University



April 12, 2017

# Acknowledgement

## POSTECH Researchers

Dr. Wulferding



Dr. Yang



Jinho Yang



Juyoung Jeong



Dongwoo Shin



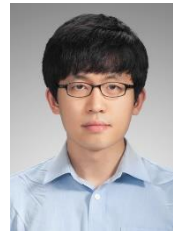
Geunyoung Kim



Jungsup Lee



Hyeongrae Noh

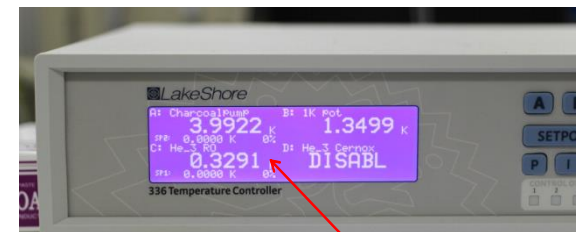
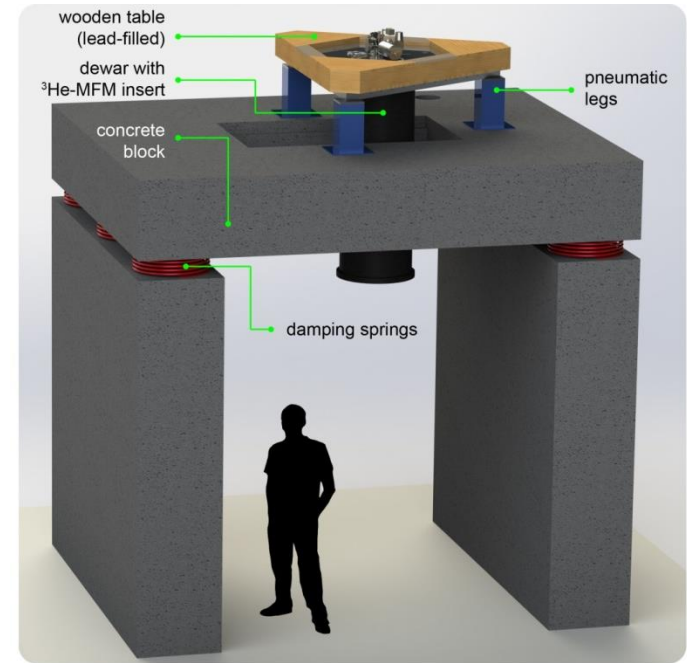
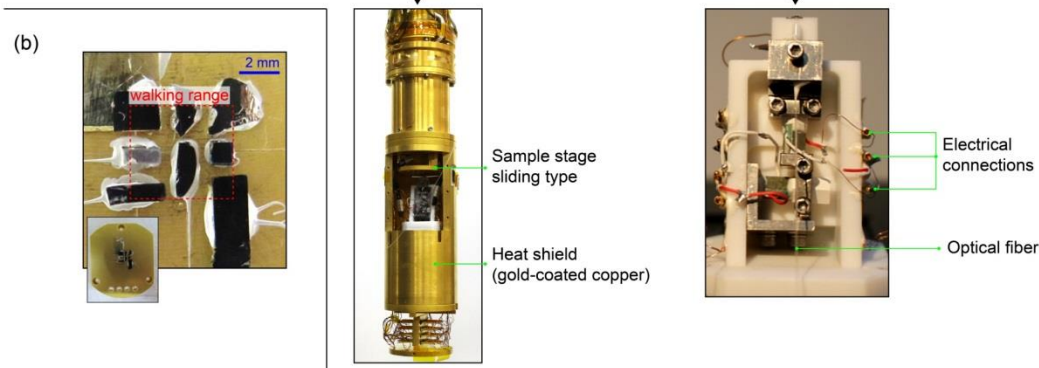
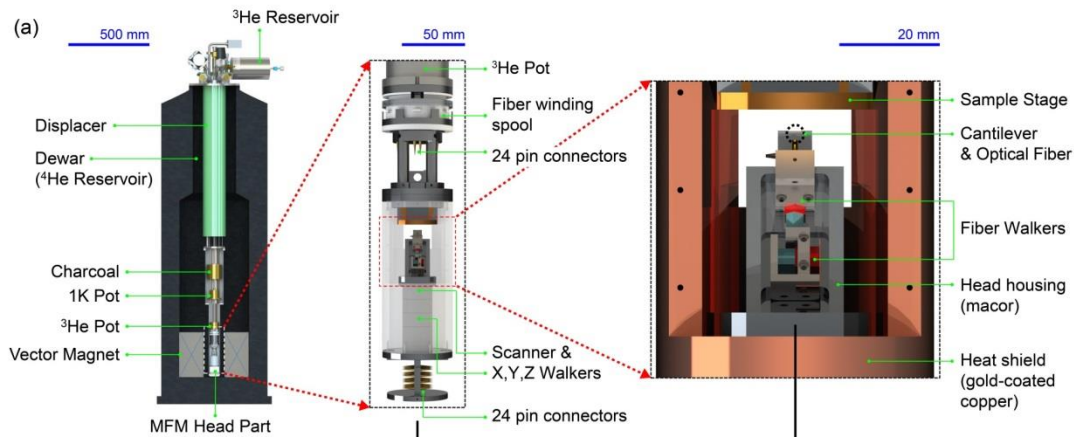


Jinyoung Yun



Samples from Dr. Bauer (LANL) and Prof. Cava (Princeton)

# $^3\text{He}$ MFM: $T = 0.3 \text{ K}$ and $\mathbf{H}_{xyz} = 2-2-9 \text{ T}$



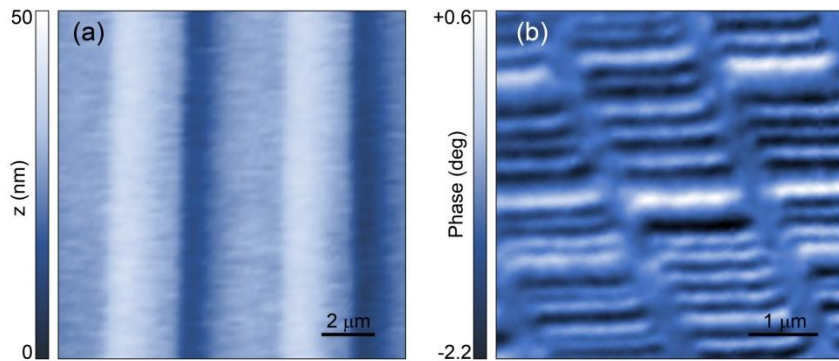
Sample temperature

Base temperature: 0.3 K ( $^3\text{He}$ )  
 3D vector magnet:  $\mathbf{H}_{xyz} = 2\text{T}-2\text{T}-9\text{T}$   
 Anti-vibration room

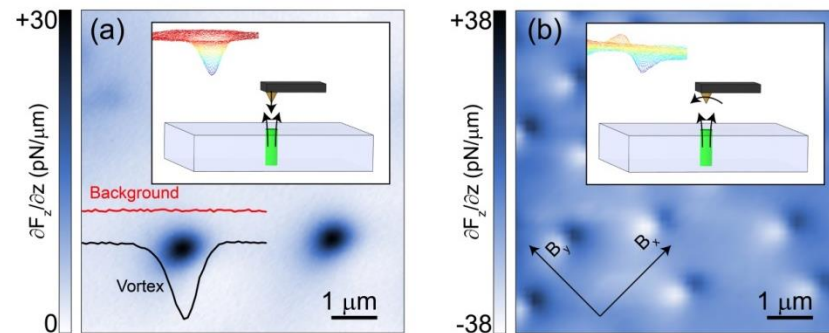
# $^3\text{He}$ MFM: Test results

AFM

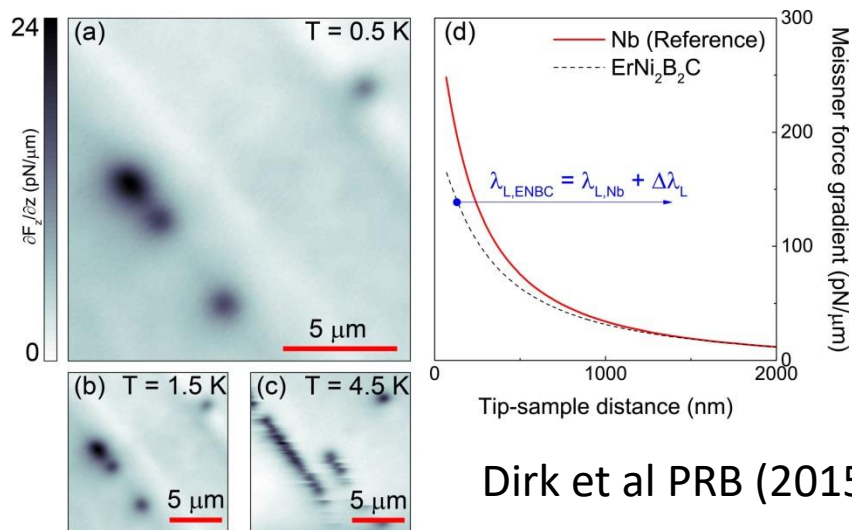
MFM



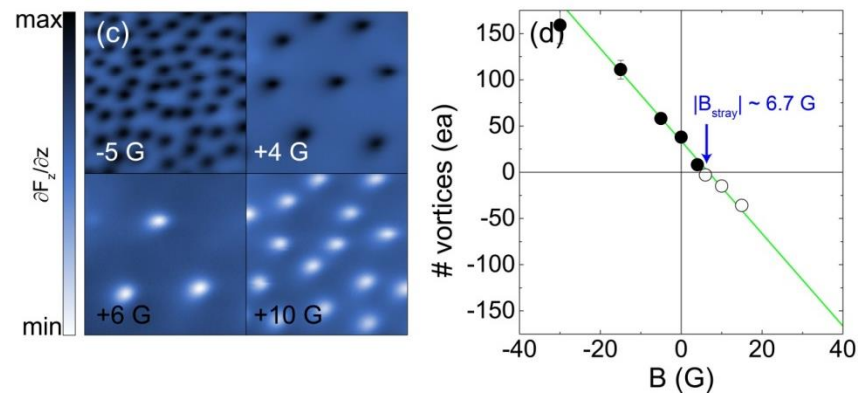
## Demonstration of a vector field in Nb



## Vortices and FM in $\text{ErNi}_2\text{B}_2\text{C}$



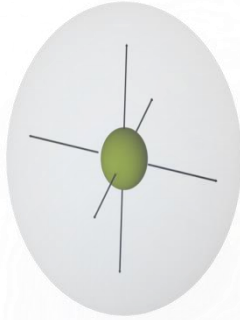
Dirk et al PRB (2015)



Yang et al RSI (2016)

# Confinement in Vortices

3 D



1 D

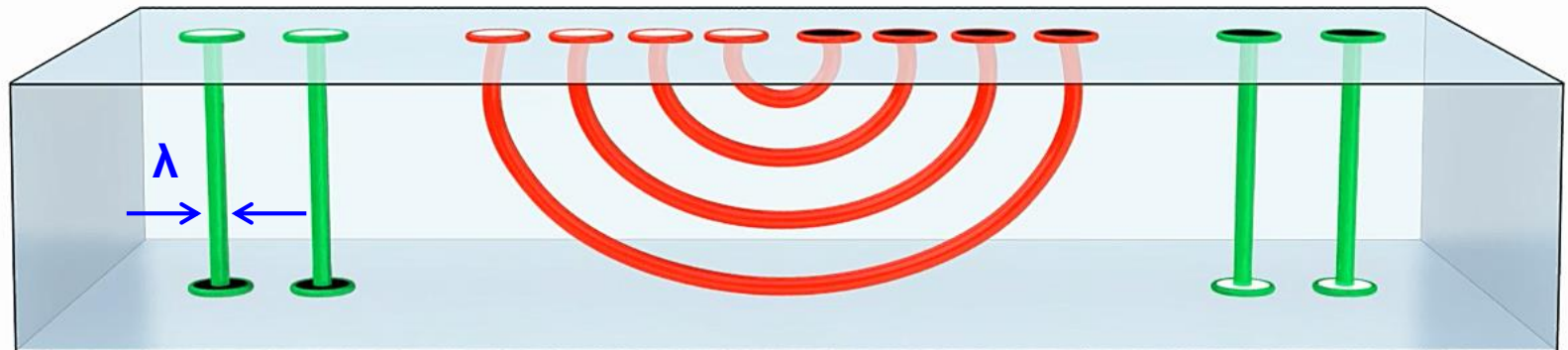


isolated

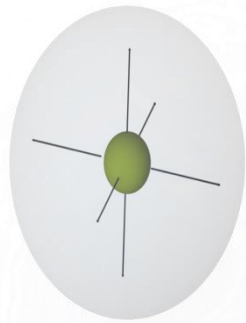
confined

isolated

$T = 4 \text{ K}$



# Potential form in 3d, 2d, and 1d from Gauss's law



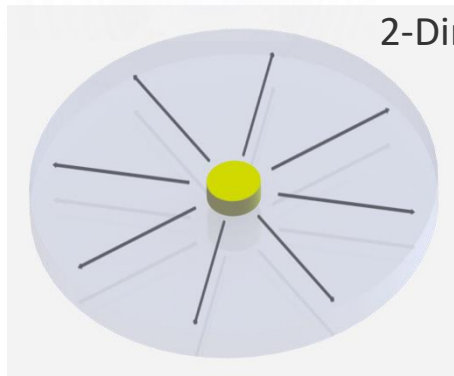
3-Dimension

$$\int \vec{E} \cdot d\vec{s} = \frac{Q}{\epsilon_0}$$

$$E \cdot 4\pi r^2 = \frac{Q}{\epsilon_0}$$

$$E = \frac{Q}{4\pi\epsilon_0} \frac{1}{r^2}$$

$$V = \frac{Q}{4\pi\epsilon_0} \frac{1}{r}$$



2-Dimension

$$\int \vec{E} \cdot d\vec{s} = \frac{\sigma}{\epsilon_0}$$

$$E \cdot 2\pi r = \frac{\sigma}{\epsilon_0}$$

$$E = \frac{\sigma}{2\pi\epsilon_0} \frac{1}{r}$$

$$V = -\frac{\sigma}{2\pi\epsilon_0} \ln r$$

1-Dimension



confinement

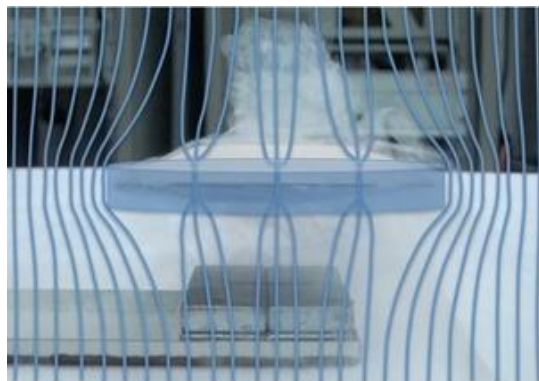
$$\int \vec{E} \cdot d\vec{s} = \frac{\lambda}{\epsilon_0}$$

$$E = \frac{\lambda}{\epsilon_0}$$

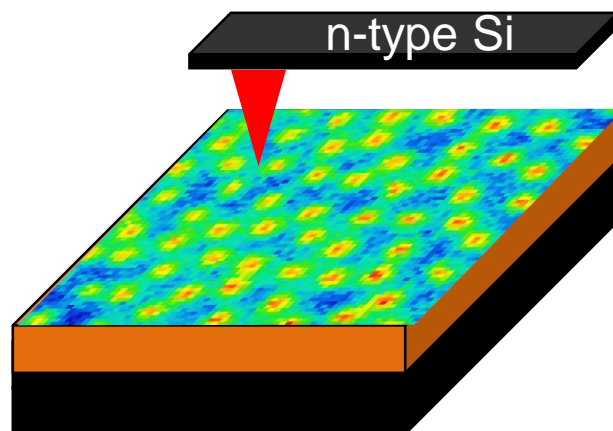
$$V = -\frac{\lambda}{\epsilon_0} r$$

# Linear potential in condensed matter

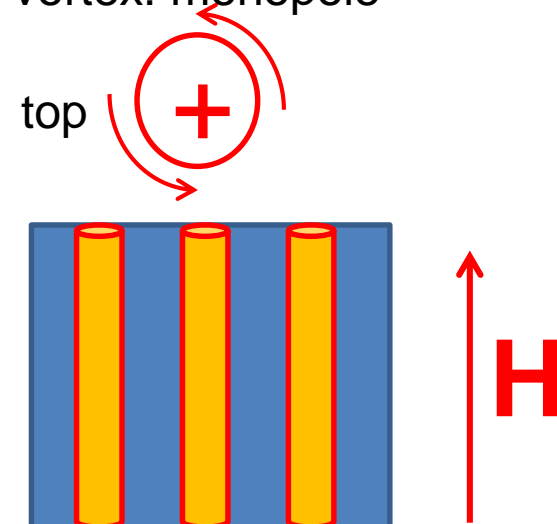
Meissner force: levitation



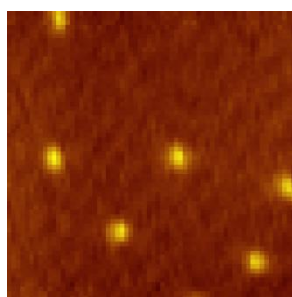
MFM: tip and magnet



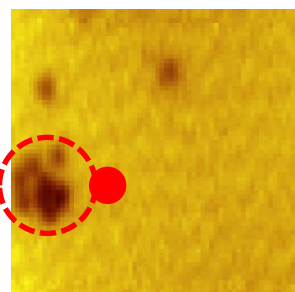
vortex: monopole



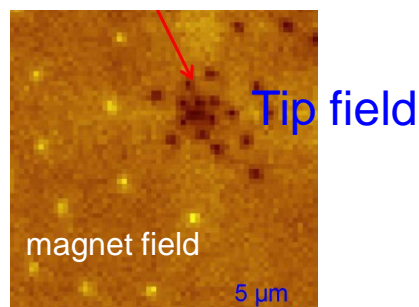
external field



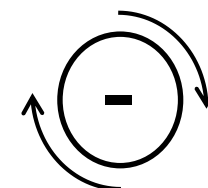
Tip field



Coexistence of V-AV



bottom



antivortex: anti monopole

Why do we see vortices below  $H_{c1}$ ?

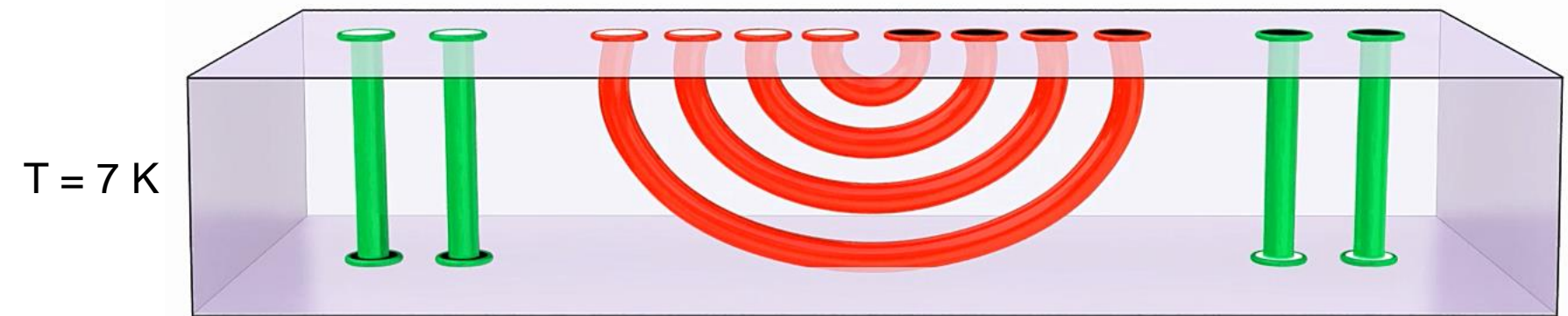
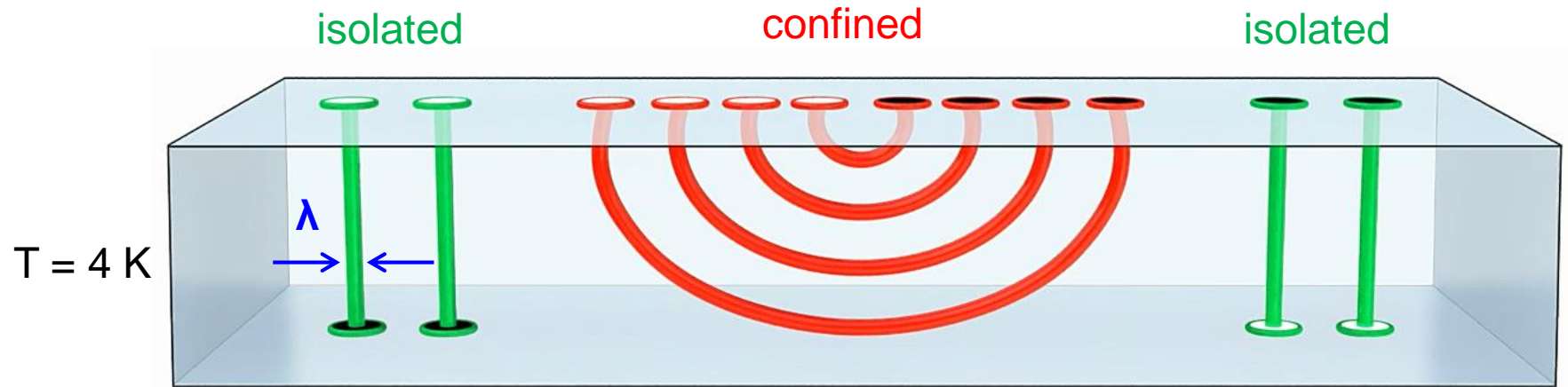
Pinning from imperfections

Vortex itself is a V-AV pair!

What is force between them?

How can you observe and measure?

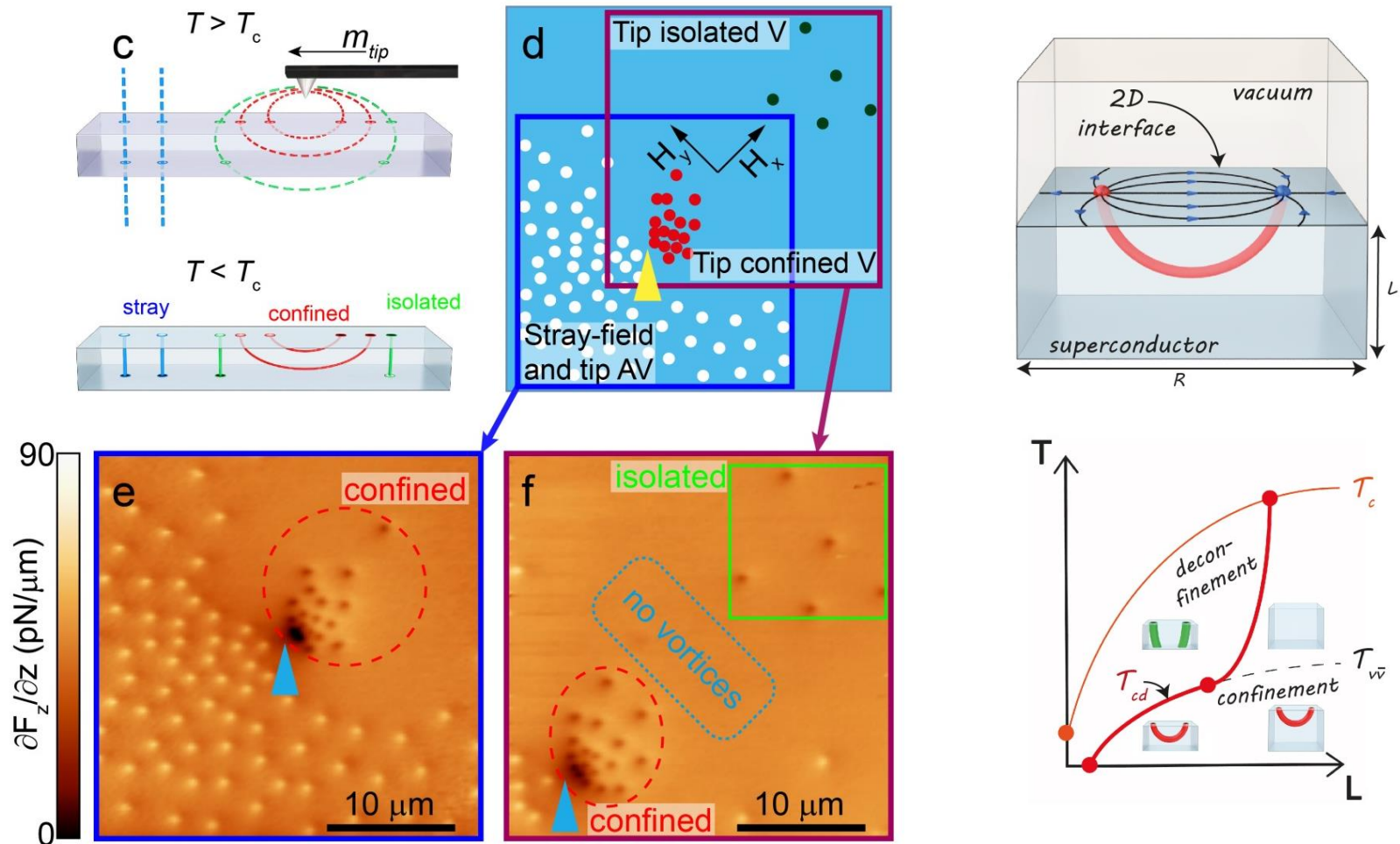
# Isolated vortices vs. Confined vortices





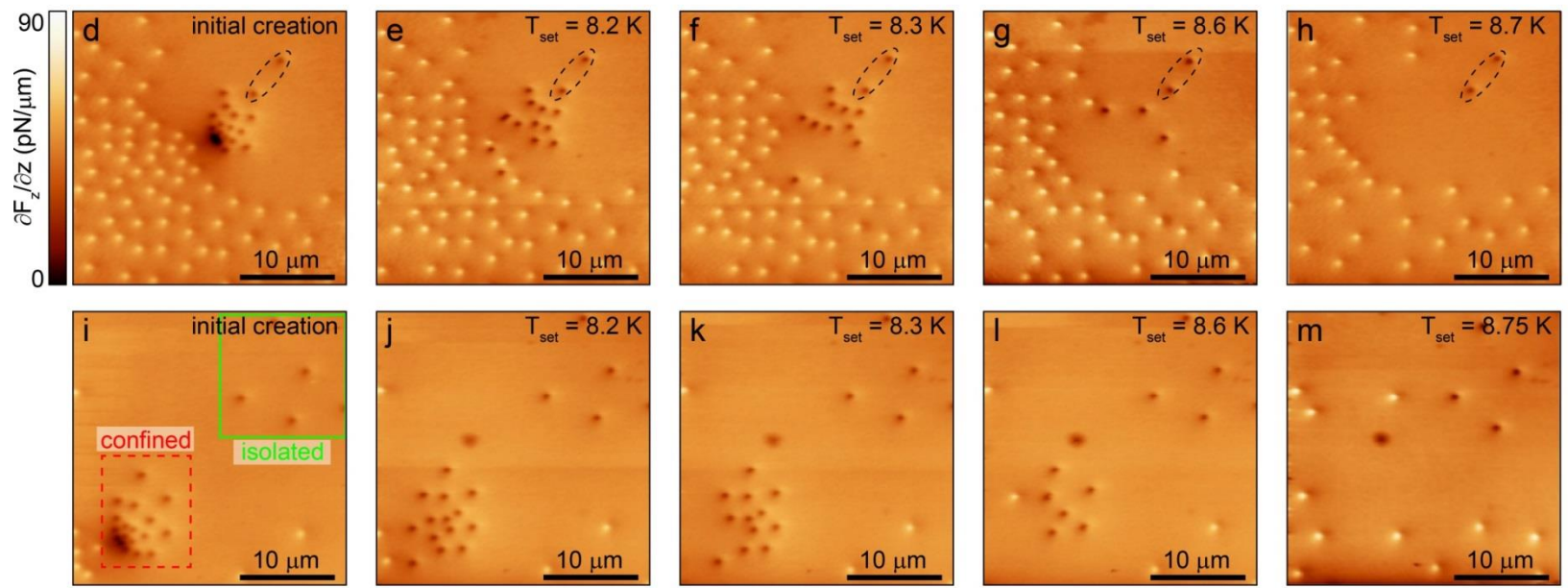
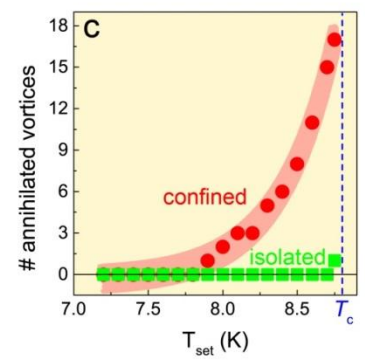
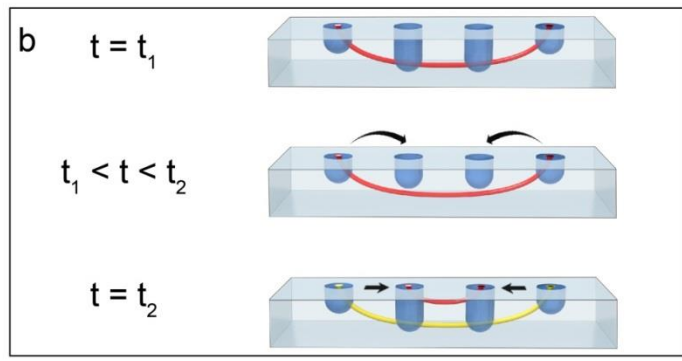
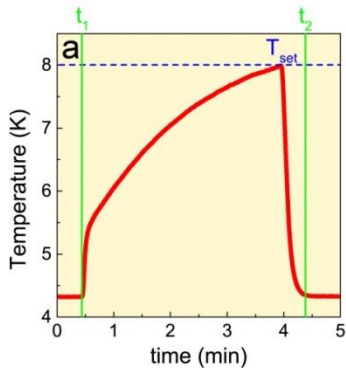
# Creation of confined vortices: Animation

# Creating confined by an in-plane tip moment: Exp.



1. External antivortices
2. **Confined** vortices and antivortices
3. **Isolated** vortices and antivortices : different interactions among them

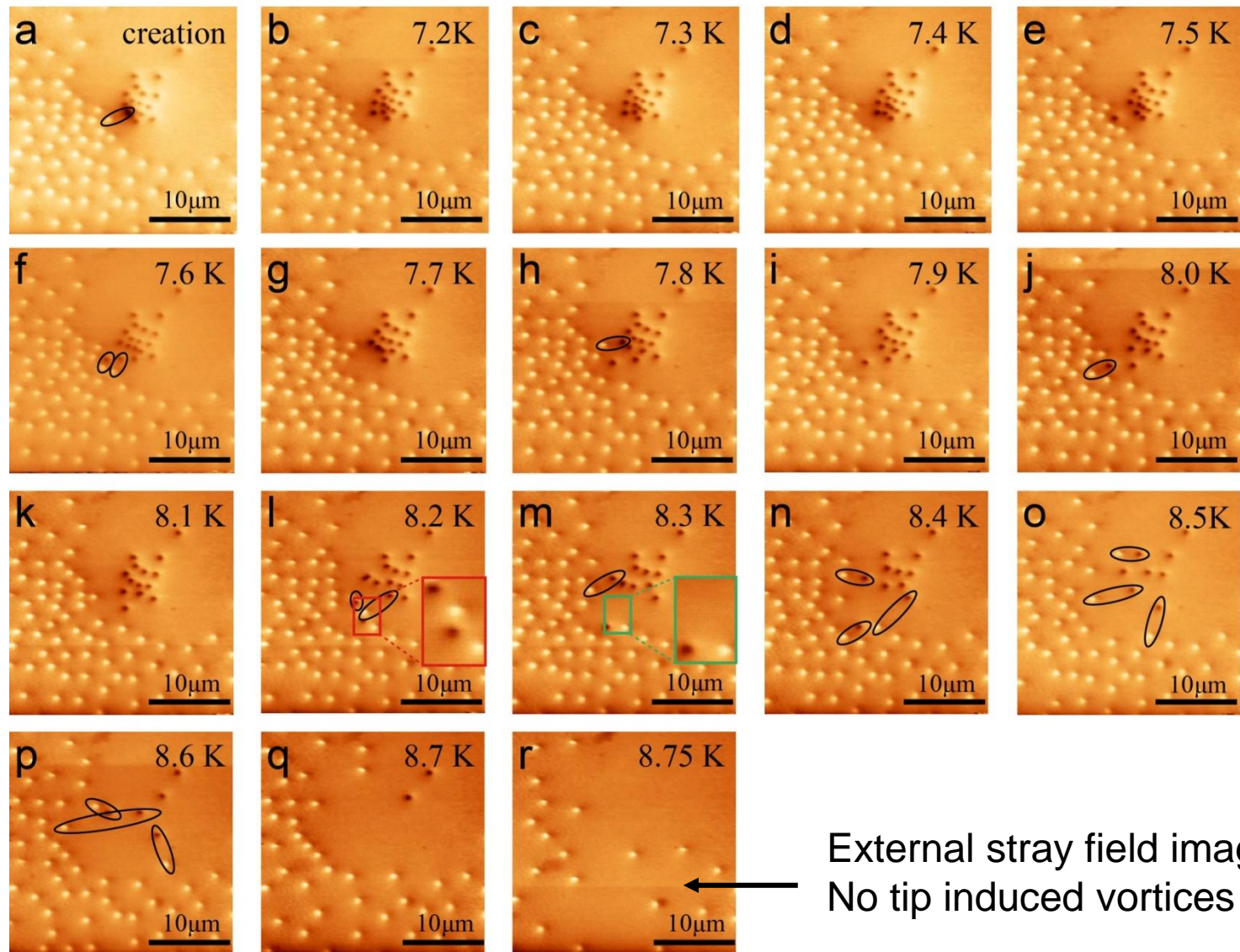
# Isolated vs. Confined: Temperature dependence



Confined: unidirectional motion

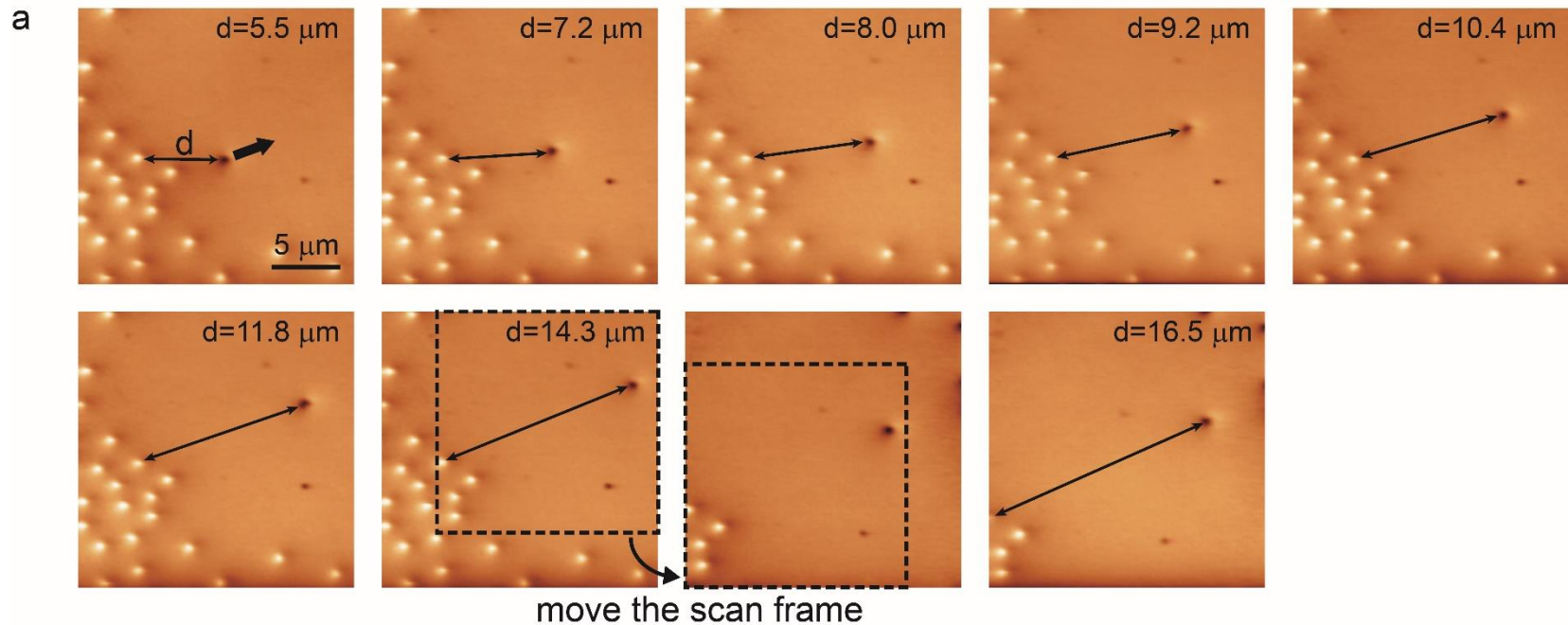
Isolated: no motion

# Temperature dependence of Confined: Full data set

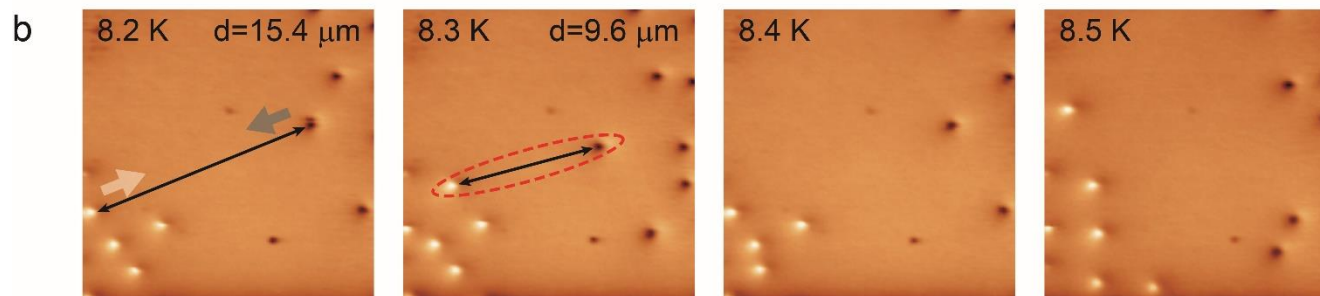


# Confined single vortex: Manipulation and $T$ dependence

## Manipulation



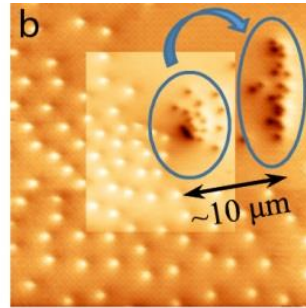
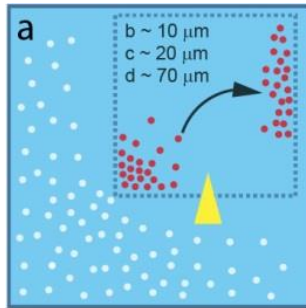
## Temperature evolution



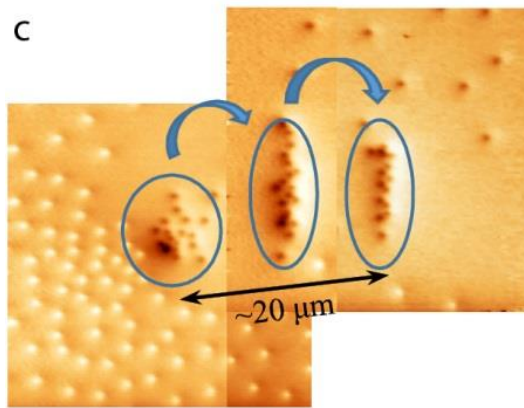
# Manipulation of Confined vortices: Animation



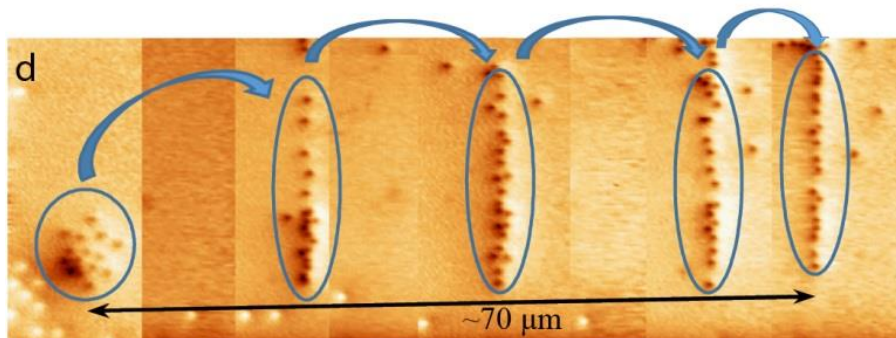
# Manipulation of Confined vortices: Experiment



10- $\mu\text{m}$  manipulation

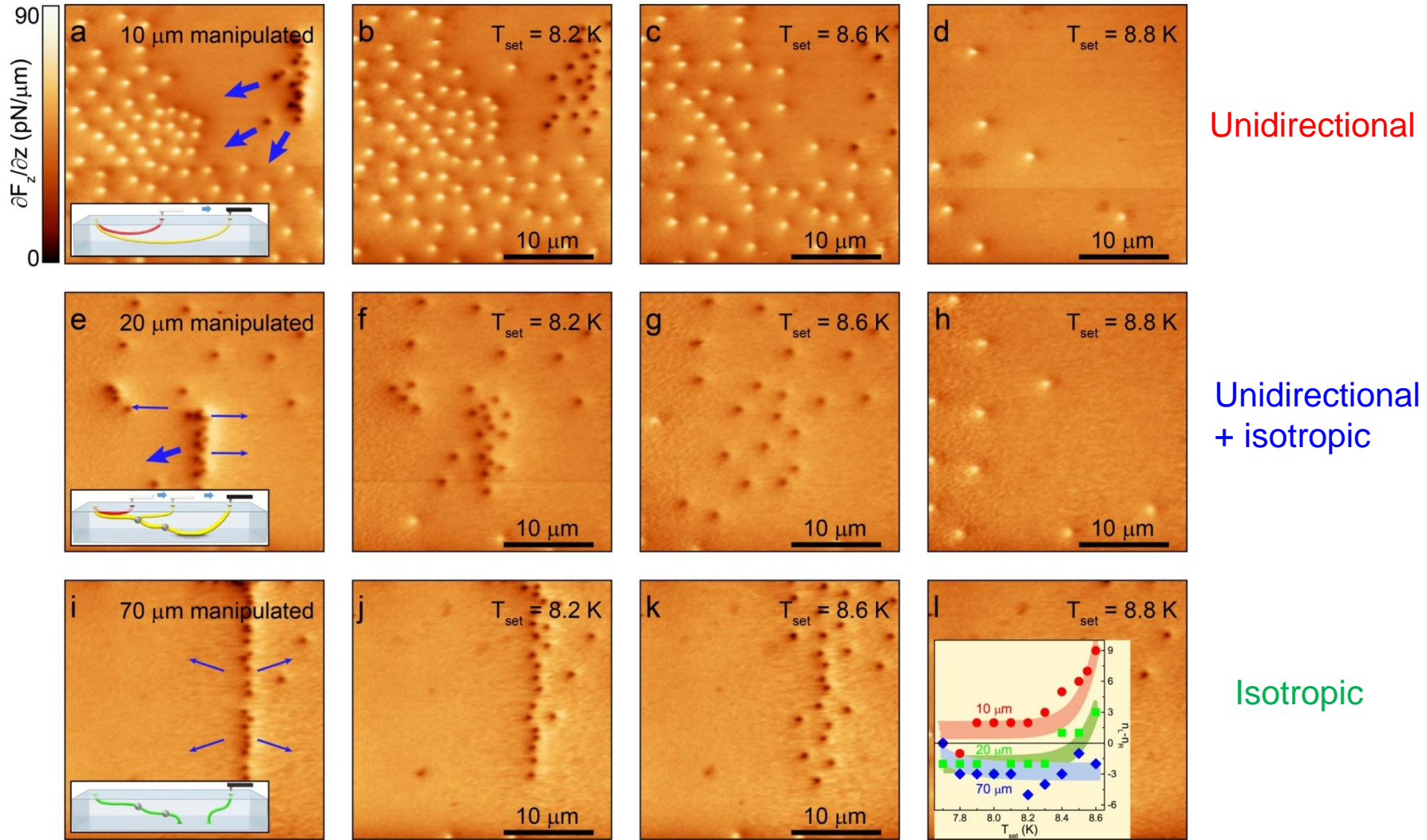


20- $\mu\text{m}$  manipulation



70- $\mu\text{m}$  manipulation

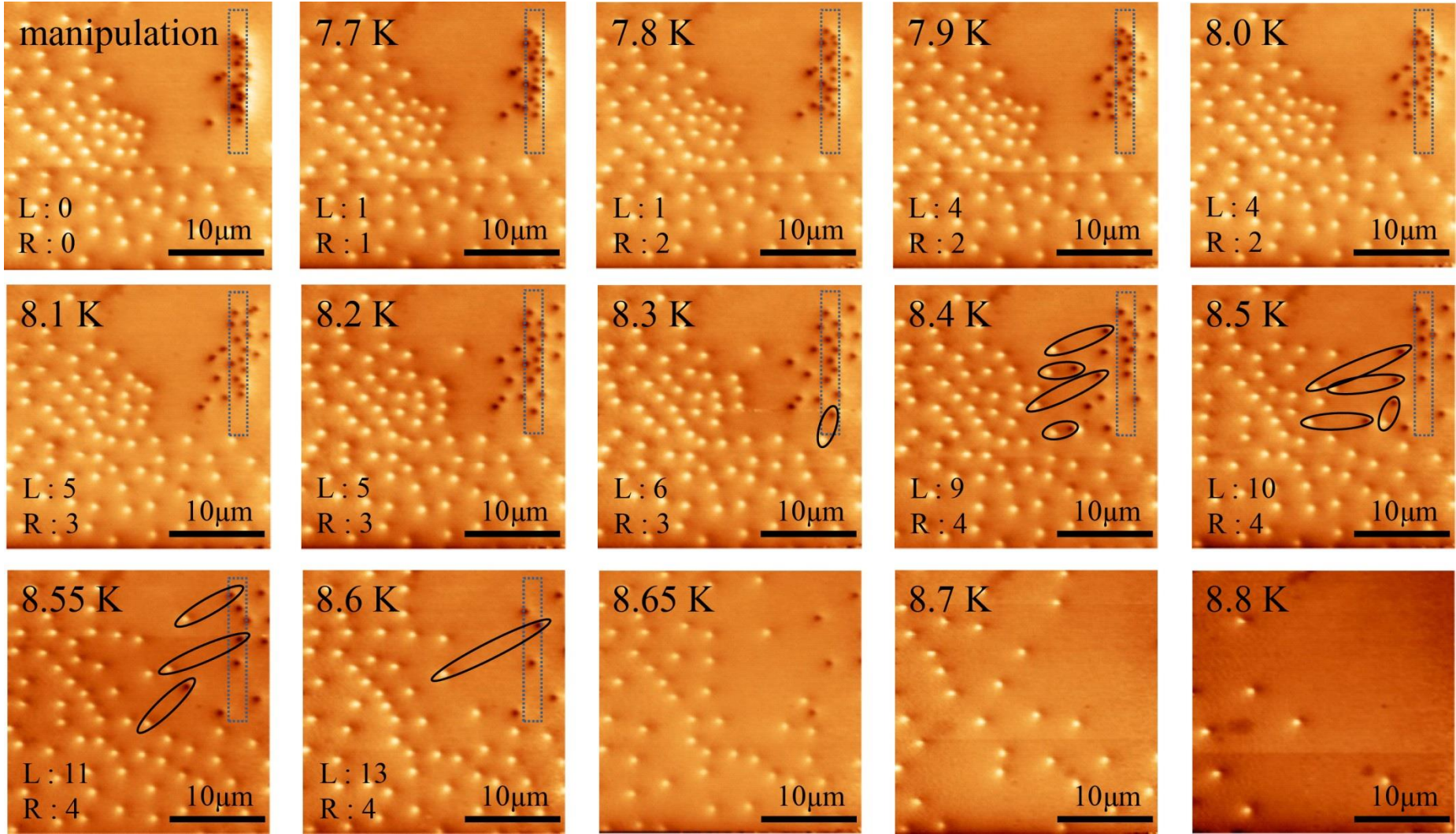
# Manipulation of Confined vortices: Experimental data



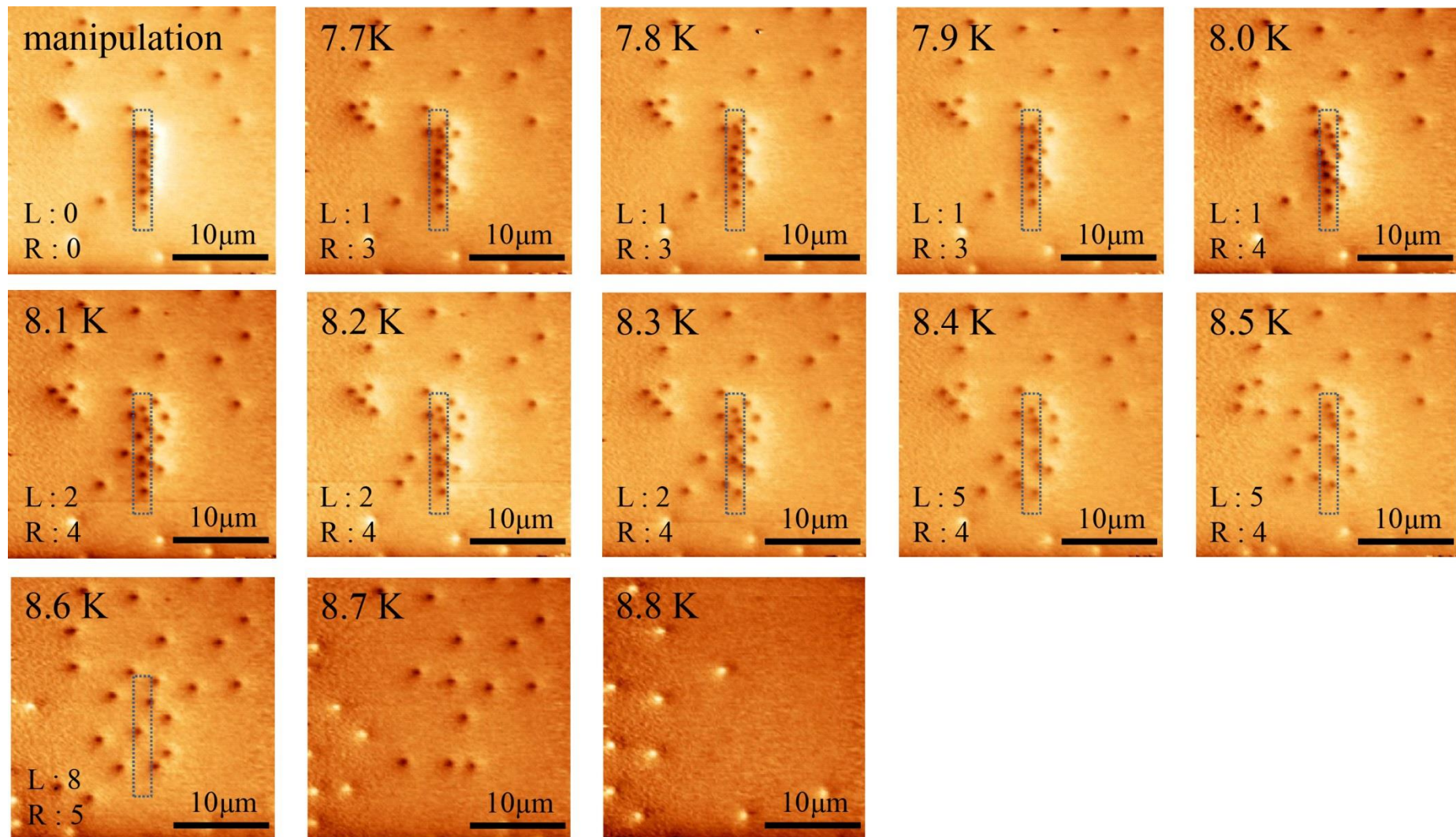
Phase transition from confined to deconfined!



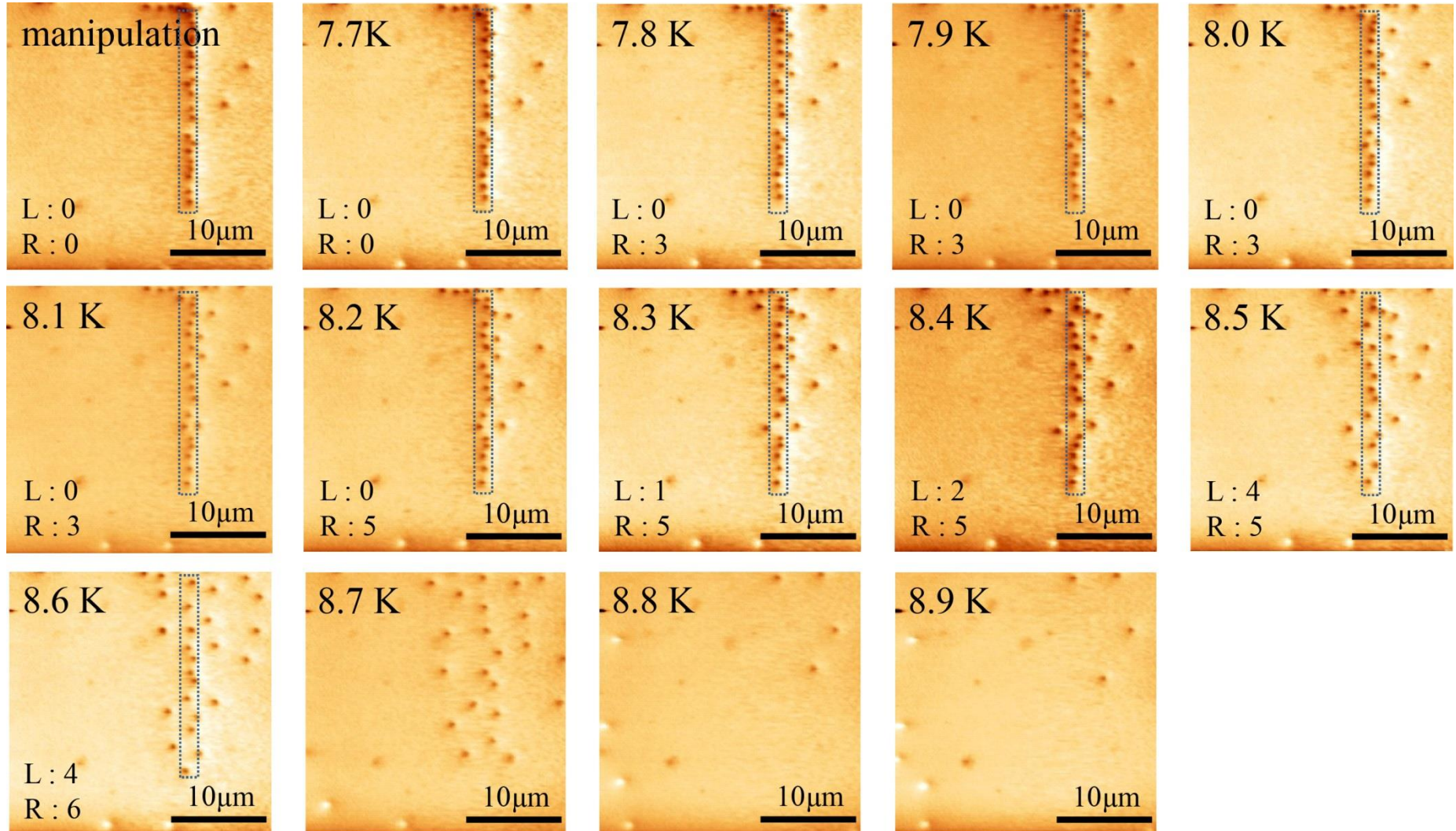
# 10- $\mu\text{m}$ Manipulation: Unidirectional



# 20- $\mu\text{m}$ Manipulation: Directional + Isotropic



# 70- $\mu\text{m}$ Manipulation: Isotropic



# Theoretical calculation: Linear potential

$$G = F_{n0} + \int_0^L dz \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} dx dy \left[ \alpha |\psi|^2 + \frac{\beta}{2} |\psi|^4 + \frac{1}{2m^*} \left| \left( \frac{\hbar}{i} \nabla - \frac{e^*}{c} \mathbf{A} \right) \psi \right|^2 + \frac{\hbar^2}{2\mu_0} - \mathbf{h} \cdot \mathbf{H}_a \right]$$

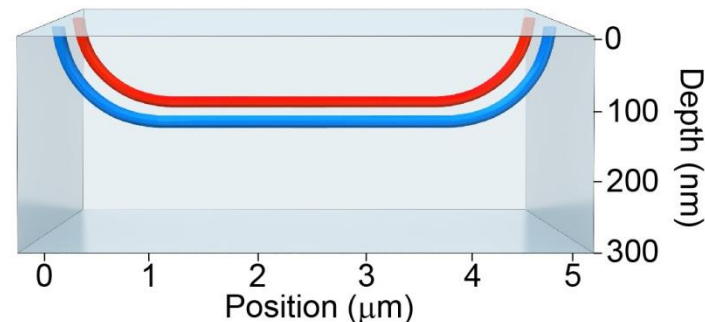
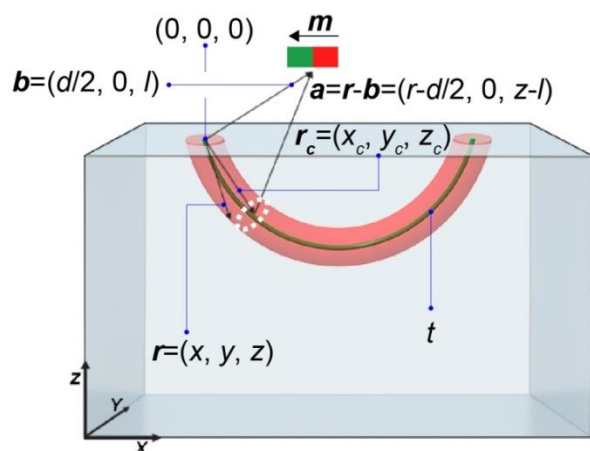
$$G_s^1 = F_{n0} + \int_0^L dz \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} dx dy \cdot \text{Single vortex}$$

$$\cdot \left[ \alpha |\psi|^2 + \frac{\beta}{2} |\psi|^4 + \frac{\hbar^2}{2\mu_0} + \frac{1}{2m^*} \left| \left( \frac{\hbar}{i} \nabla - e^* \mathbf{A} \right) \psi \right|^2 - \mathbf{h} \cdot \mathbf{H}_a \right]$$

$$G_s^0 = F_{n0} + \int_0^L dz \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} dx dy \left[ \alpha |\psi|^2 + \frac{\beta}{2} |\psi|^4 \right] \cdot \text{No vortex}$$

$$G_v^1 = \iint_A \left[ \frac{\hbar^2}{2\mu_0} + \frac{\lambda^2}{2\mu_0} |\nabla \times \mathbf{h}|^2 - \mathbf{h} \cdot \mathbf{H}_a \right] dA dt \approx \int \frac{\pi \lambda^2 C_0^2 \xi}{\mu_0 \lambda} K_0 \left( \frac{\xi}{\lambda} \right) K_1 \left( \frac{\xi}{\lambda} \right) dt = \epsilon_v \int dt$$

constant

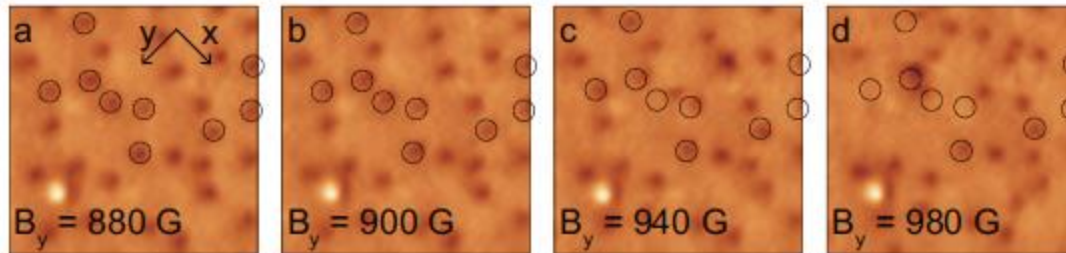


Vortex free energy  $\propto$  arc-length of vortex trajectory: Linear potential

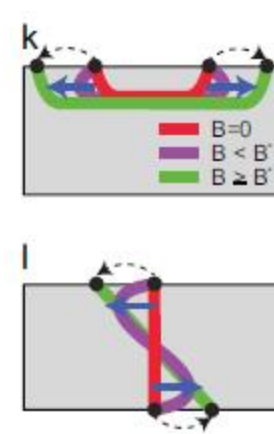
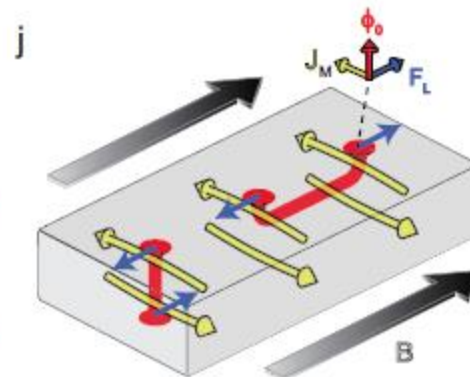
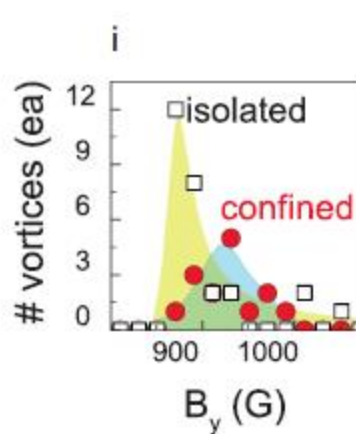
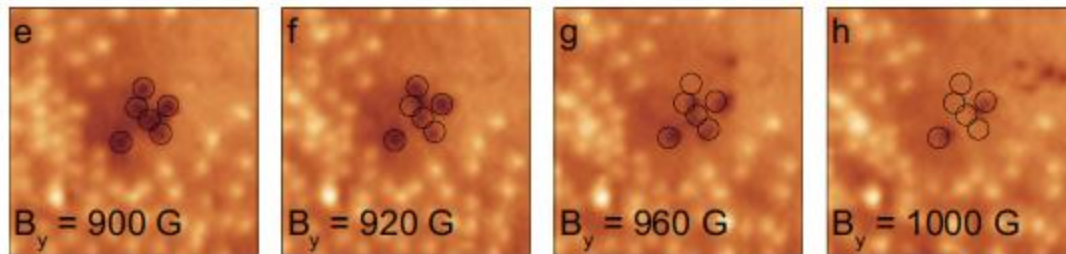
# Confinement force measurement

**Meissner current induced manipulation:** local pinning force measurement

isolated



CVAVP



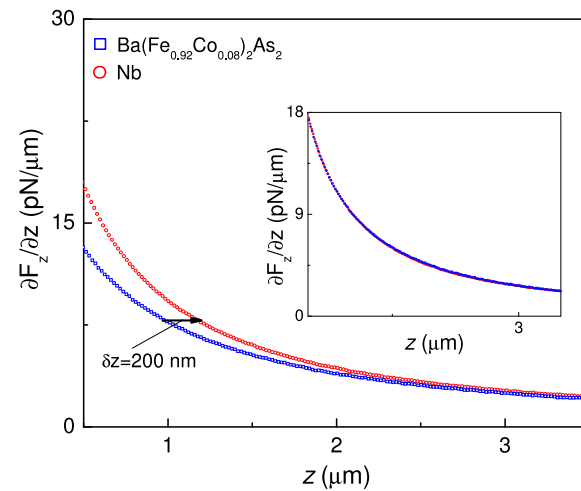
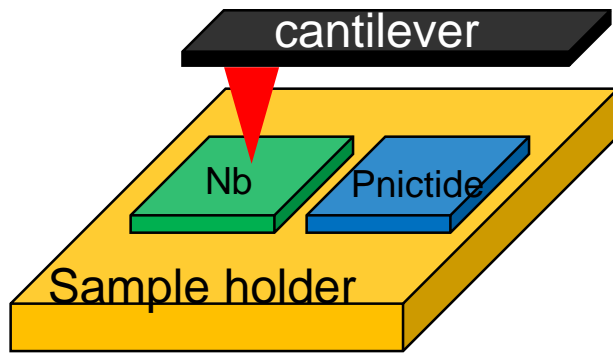
$$\mathbf{J}_M = -\frac{B_{ext}}{\mu_0 \lambda_L \cosh(a/\lambda_L)} \sinh(z/\lambda_L) \hat{x}$$

$$\mathbf{f}_p = \mathbf{J}_M \times \Phi_0 \hat{z} = \frac{B_{ext} \Phi_0}{\mu_0 \lambda_L \cosh(a/\lambda_L)} \sinh(z/\lambda_L) \hat{y}$$

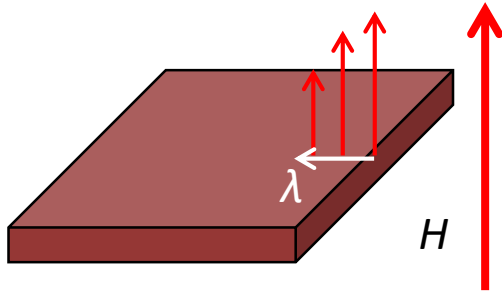
$$F_{exp} = 43 \text{ pN}$$

$$F_t = \frac{\Phi_0^2}{4\pi\mu_0\lambda^2} K_0\left(\frac{\xi}{\lambda}\right) [14], \quad F_{theory} = 48 \text{ pN}$$

# Local magnetic penetration depth in MFM



# Why Care about the Magnetic Penetration Depth?



- Two important parameters in superconductors:  $\lambda$  and  $\xi$
- Superconducting properties:  $H_c$  (rf cavity),  $J_0$ ,  $G_i$  (thermal fluctuations), *etc*

→  $\lambda$  affects more than  $\xi$

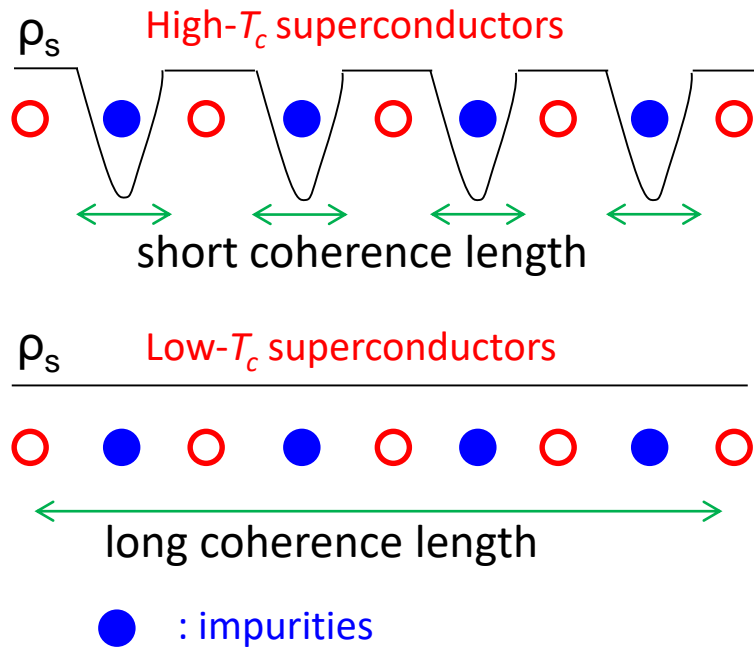
$$H_c(T=0) = \frac{\Phi_0}{2\sqrt{2}\pi\lambda(0)\xi(0)}$$

$$J_0(T=0) = \frac{cF_0}{12\sqrt{3}\rho^2\lambda l^2}$$

$$G_i = \frac{1}{2} \left[ \frac{8\rho^2 g T_c l^2}{\lambda F_0} \right]^2$$

- Paring symmetry via measurement of  $\lambda(T)$ :  
s-wave (exponential), d-wave (power law)
- Kinetic inductance: electronic performance in thin films  
(NbN films for single photon detector)

# Why Care about the Magnetic Penetration Depth?



- $\lambda$  in inhomogeneous superconductivity:  
**Swiss cheese** model ( $T_c$  - little change;  $\lambda$  changes drastically)
- Uemura relation in the dirty limit:

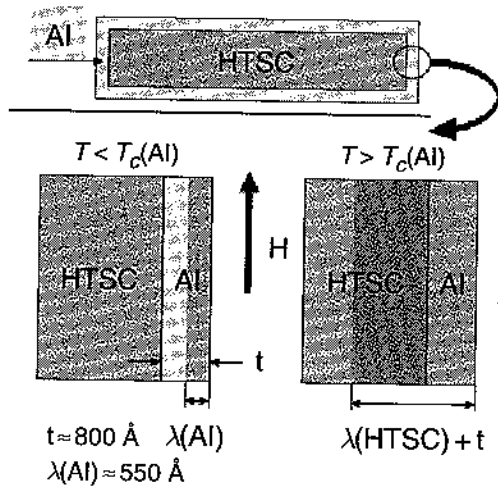
$$\rho_{eff} = \frac{1}{\lambda_{eff}^2} \approx \frac{1}{\lambda_L^2} \frac{l}{\xi_0} \propto \Delta(0) \propto T_c$$

- Paring symmetry from pair breaking:  
 $\lambda$  as a function of a irradiation dose
- Type I or II superconductivity: Pb thin film

In this talk:  $\lambda(\theta)$



# Conventional Techniques for $\lambda$ Measurements



**Figure 14.3** Schematics of the experiment used to measure the absolute value of the penetration depth by coating a high- $T_c$  superconductor with low- $T_c$  (Al in this case) material.

Figure courtesy of Prof. Poole, in Superconductivity

- Mutual inductance technique: **drive and pickup coils on opposite sides of the film. (only works for films)**
- $\mu$ SR: measures second moment of the magnetic field distribution around a vortex, related to  $\lambda(0)$ . **(the vortex lattice and muon locations; only works for bulk samples)**
- Reversible magnetization (SQUID): **for clean samples**
- Infrared reflectivity: **measures anisotropy**

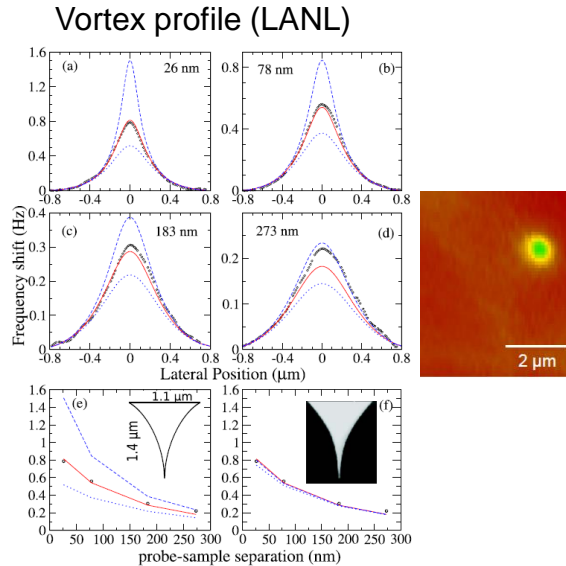
$$\lambda(\omega) = 4\pi\omega\sigma(\omega) / c^2$$

- Tunnel-diode resonator : **coat with Al film (reference)**

$$\lambda(HTSC) = \lambda(Al) + \frac{\Delta\lambda^{Al}(T_c) - t}{1 - \exp(-t / \lambda(Al))}$$

# $\lambda$ Measurement by MFM

## Previous techniques by MFM



Nazaretski et al., APL 2009

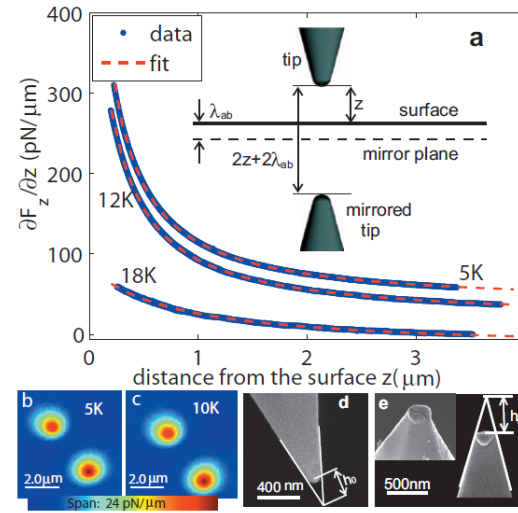
- Analysis of a single vortex profile for  $\lambda$  in MFM: requires an extensive numerical analysis for modeling the tip.

$$\frac{\partial f_z}{\partial z} = A \frac{M_{tip} \Phi_0}{(z + \lambda_{ab})^3}$$

A: Tip geometry,  $M_{tip}$ : Tip moment

- How would you measure  $\lambda$  without vortices?

## Meissner (Stanford)



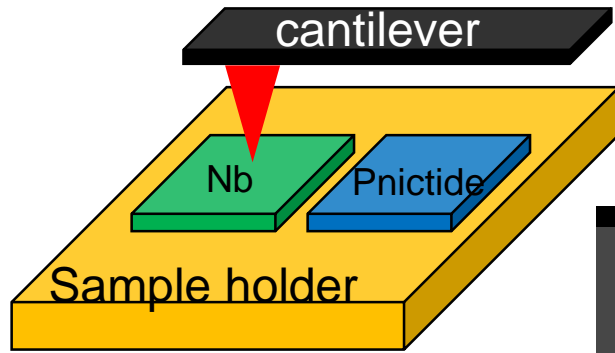
Luan et al., PRB 2010

$$\frac{\partial f_z}{\partial z} - \frac{\partial f_z}{\partial z} \Big|_{z=\infty} = A \left( \frac{1}{z + \lambda_{ab}} + \frac{h_0}{[z + \lambda_{ab}]^2} + \frac{h_0^2}{2[z + \lambda_{ab}]^3} \right)$$

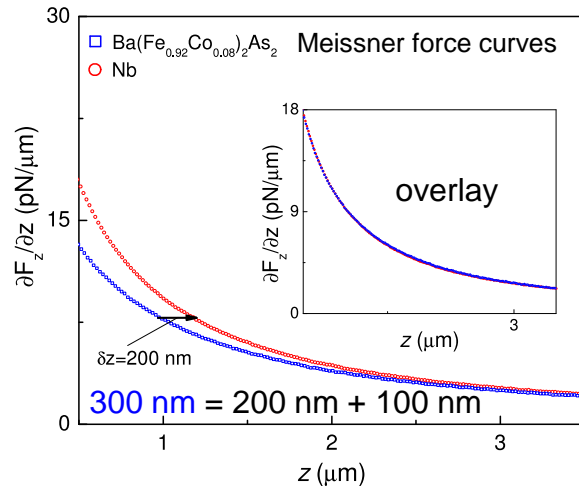
Successfully applied for  $\Delta\lambda$  measurements, but still use the fit (modeling of the tip geometry) to extract the absolute  $\lambda$  value.

Our strategy: avoid modeling the tip and develop a reliable method.

# Our approach: a comparative Meissner force experiment



Our  $\lambda$  measurements are featured in SuST



## Comparative experiment in MFM

$$F'_{Nb} = \frac{\partial f_z}{\partial z} = A \frac{M_{tip} \Phi_0}{(z_{Nb} + \lambda_{Nb})^3}$$

$$F'_{pnictide} = \frac{\partial f_z}{\partial z} = A \frac{M_{tip} \Phi_0}{(z_p + \lambda_{pnictide})^3}$$

$$F'_{Nb} = F'_{pnictide} \text{ if } z_{Nb} = z_{pnictide} + \Delta z$$

$$\text{: Then } \lambda_{pnictide} = \lambda_{Nb}(100 \text{ nm}) + \Delta \lambda (= \Delta z)$$

- No modeling of the tip
- Direct measurement
- Fast measurement
- Reliable measurement
- Measure 10 samples in a few hours

J. Kim et al., Supercond. Sci. Technol. **25**, 112001 (2012)

Direct, local – Inhomogeneity, High throughput

# Summary of Techniques for $\lambda$ Measurements

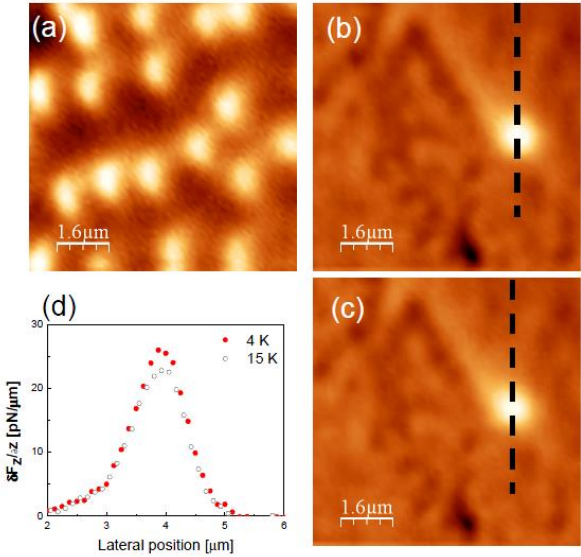
Technique	Absolute value of MPD	Sample shape bulk/film	Local probe	Temperature range	Number of samples measured	National facility or "table top"	Time per experiment
$\mu$ SR	yes	bulk	no	> 50 mK	one	NF	weeks
Resonant cavity	no	bulk	no	> 1.2 K	one	TT	weeks
Scanning SQUID	no	bulk to thin film	yes ( $\sim\mu\text{m}$ )	> 1.2 K	one	TT	weeks
TDO	no	bulk	no	> 50 mK	one	TT	weeks
Mutual inductance	yes (fitting)	thin film	no	> 1.2 K	one	TT	weeks
Existing MFM "Meissner"	yes (fitting)	bulk	yes ( $\sim\text{nm}$ )	> 4 K	one	TT	weeks
<b>Kim MFM "Meissner"</b>	Yes (direct)	bulk to ultrathin film	yes ( $\sim\text{nm}$ )	> 0.5 K	more than ten	TT	few hours

We can work on more than 10 samples in few hours!  
 Comparative method: doping or irradiation dependence: draw correlations among samples of interest.

# Results of $\lambda$ measurements: One

## MgB<sub>2</sub>film (STI): dirty limit

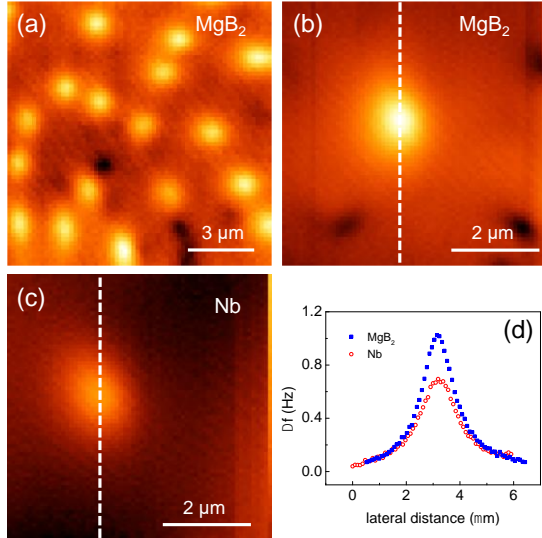
(Made by reactive evaporation)



●  $\lambda(0)=200$  nm: dirty  $\pi$  band

## MgB<sub>2</sub>film (Temple U.): clean limit

(Made by hybrid physical chemical vapor deposition)



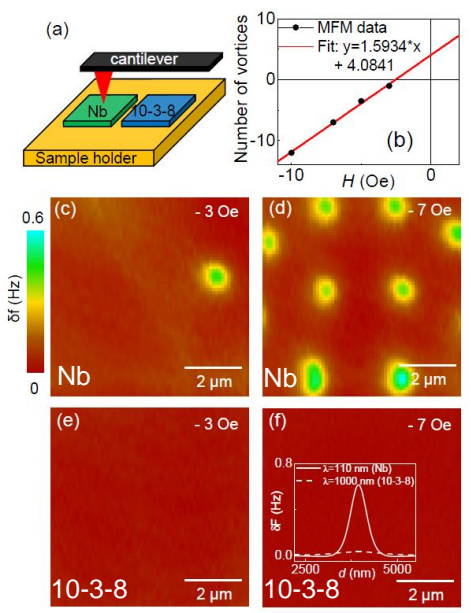
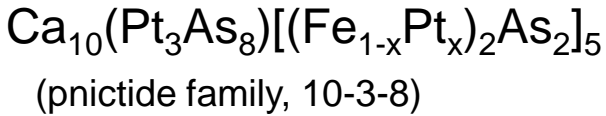
●  $\lambda(0)=50$  nm: clean  $\pi$  band

Provide a potential venue for understanding multiband superconductivity (pnictides).  
 The degree of cleanness in the  $\pi$  band results in a drastic change of  $\lambda$ , and thus for vortex dynamics.  
 $H_{c2}$  changes drastically from 10 T up to 60 T due to the two band nature.

J. Kim, N. Haberkorn et al., PRB **86**, 024501 (2012)

J. Kim, N. Haberkorn et al., arXiv:1303.0352: SSC (2015)

# Results of $\lambda$ measurements: Two



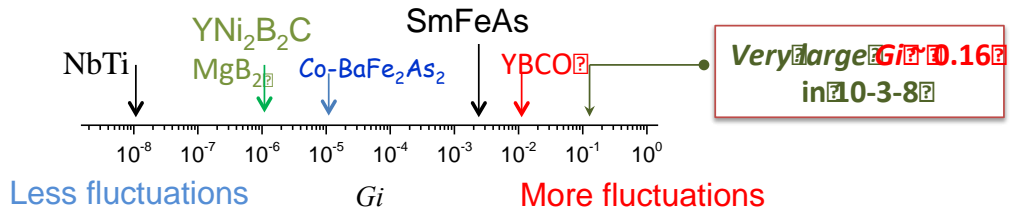
$$Gi = \frac{1}{2} \left[ \frac{8\rho^2 g T_c l^2}{\chi F_0} \right]^2$$

Thermal fluctuations ( $G_i$ ):

- produce flux creep & vortex liquid phases
- bad for applications

- $\lambda(0)=1000$  nm: no vortices
- Large thermal fluctuations

J. Kim, N. Haberkorn et al., PRB **85**, 180504 (R) (2012)



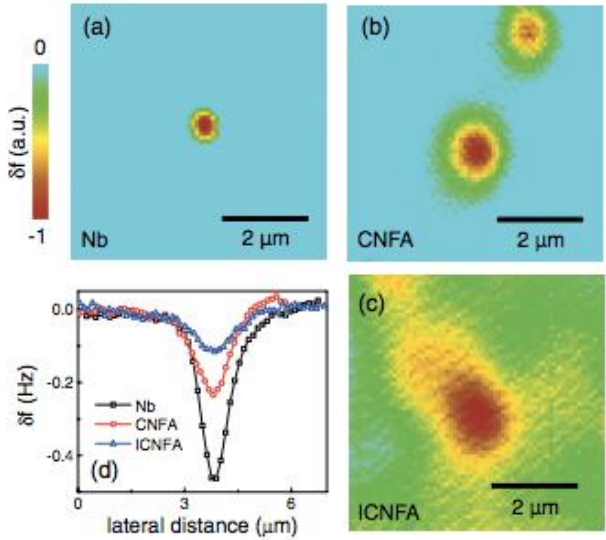
$\text{Ba}(\text{Fe}_{0.86}\text{Co}_{0.14})_2\text{As}_2$   
( $x=0.14$ , Heavily overdoped)

- Superconducting only after annealing
- $\lambda(0)=600$  nm
- Nanoscale inhomogeneities

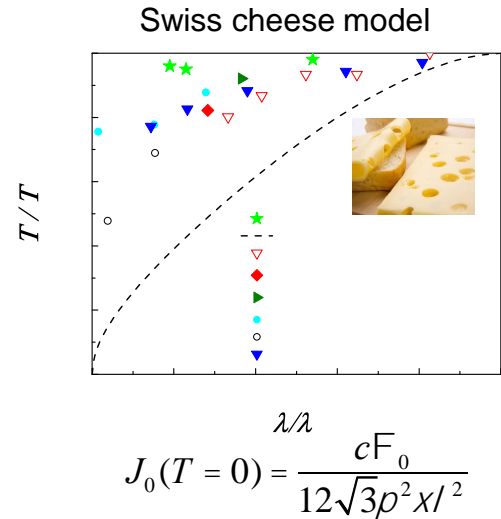
J. Kim, N. Haberkorn et al., SSC (2015)

# Results of $\lambda$ measurements (Swiss cheese)

## Ca<sub>0.5</sub>Na<sub>0.5</sub>Fe<sub>2</sub>As<sub>2</sub>



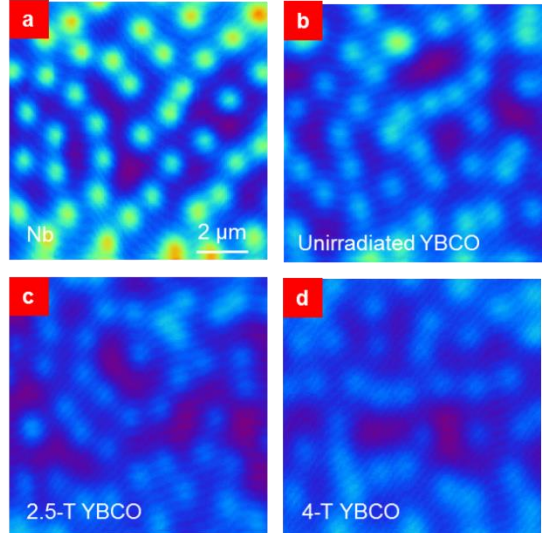
## Irradiation dependence



$J_0$ , pinning, creep, vortex dynamics are directly related to  $\lambda$ , however no systematic studies have been made so far due to difficulty of  $\lambda$  measurement.

YBCO: NP or CD for  $J_c$ ? Think about Balance between pinning and intrinsic properties!!!

## YBCO films



Heavy ion irradiated: correlated defects

	$\lambda$ (nm)	$T_c$ (K)
unirradiated	200	90.5
irradiated	320	87

in-preparation

Proton irradiated: random point defects

	$\lambda$ (nm)	$T_c$ (K)
unirradiated	260	19.4
irradiated	430	17.8

J. Kim et al., PRB 86, 144509 (2012)